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MICROELECTRONIC DESIGN WITH INTEGRATED MAGNETIC AND PIEZOELECTRIC STRUCTURES

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Esame finale anno 2016

Dedicated to my family and to my sweet love Greta

Antonio Camarda, March 2016

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Abstract

This thesis investigates the possibility of integrating the standard CMOS design process with additional microstructures enhancing circuit functionalities. More specifically, the thesis faces the problem of miniaturization of magnetic and piezoelectric devices mostly focused on the application field of EH (Energy Harvesting) systems and ultra-low power and ultra-low voltage systems.

It shows all the most critical aspects which have to be taken into account during the design process of miniaturized inductors for PwrSoC (Power System on Chip) or transformers. Furthermore it shows that it is possible to optimize the inductance value and also performances by means of a proper choice of the size of the planar core or choosing a different layout shape such as a serpentine shape in place of the classic toroidal one. A new formula for the correct evaluation of the MPL (Magnetic Path Length) was also introduced.

Concerning the piezoelectric counterpart, it is focused on the design and simulation of various MEMS PTs based on a SOI (Silicon on Insulator) structure with AlN (Alluminum Nitride) as active piezoelectric element, in perspective of having a SoC with embedded MEMS devices and circuitry. Furthermore it demonstrates for the first time the use of a PT (Piezoelectric Transformer) for ultra-low voltage EH applications. A new boost oscillator based on a discrete PZT (Lead Zirconate Titanate) PT instead of a MT (Magnetic Transformer) has been modelled and tested on a circuit made up by discrete devices, showing performances comparable to commercial solutions like the LTC3108 from Linear. Furthermore this novel boost oscillator has been designed in a 0.35µm technology by ST Microelectronics, showing better performances as intuitively expected by the developed mathematical model of the entire system.

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State Of Art of miniaturized systems with magnetic and piezoelectric devices

The scaling of dimensions in IC processes has led towards a continuous reduction of the power required by electronic systems. The advantages of this relentless shrinking of dimensions are numerous. First of all, shrunk systems allow a lower production cost. Furthermore, power requirements are in general directly linked to the volume of transducers/devices exploiting some physical effects such as the *electromagnetic* transduction or the *piezoelectric* transduction. As a matter of fact, the most frequently used devices in power conversion systems are inductors (as well as transformers) or piezoelectric-transducers, given that the power delivered by such devices is proportional to their dimensions.

Integrated magnetic devices such as inductors and transformers for power applications are more common but piezoelectric devices have the advantage of the absence of EMI and higher quality factors, given that the electromechanical transduction is much more efficient than the electromagnetic one. Hence magnetic and piezoelectric devices can be considered dual, since piezoelectric elements are more similar to a variable capacitance, whereas the most used magnetic device is the inductor. As a matter of fact, the energy conversion from magnetic to electric (for inductors) and from mechanic to electric (for piezo-devices) can be modelled through an equivalent lumped parameter circuit which is pretty useful to assess the behavior and the performances of such devices when they are embedded in a power system.

However, devices exploiting both magnetic and/or piezoelectric effects are essential not only for power and ultra-low power systems, but also for many application fields such as sensing, transduction and actuation, and overall both devices offer the possibility to be integrable at package or wafer level together with the dedicated IC (Integrated Circuit) through MEMS (Micro Electro-Mechanical Systems) technologies and techniques.

Thanks to this potential integrability, market drivers are pushing towards the direction of new miniaturized platforms like Power Supply in Package (PwrSiP) and Power Supply on Chip (PwrSoC) technologies.

In PwrSiP the magnetic (or potentially piezoelectric devices) are put in the same package together with the integrated power converter, whereas in PwrSoC these devices are generally integrated at chip level and placed on the top of the IC. Generally speaking, the integration at wafer level of magnetic and/or piezoelectric elements is theoretically possible but not always practically feasible. Although the production of miniaturized piezoelectric and magnetic devices exploits IC compliant techniques, the integration at wafer level might bring some production issues. A first production issue that needs to be solved is the presence of unusual chemical elements in clean room environment, which need to be properly managed to prevent contaminations in other stages of the process. To cite an additional example, using several mm² in a 180nm technology to make the transducer might not be economically viable, because the IC is likely to be much smaller than the device itself, thus increasing the whole cost. So an alternative idea could be processing separately the chip and device, or producing the device (or transducer) as a post-processing on top of the chip (multi-chip integration).

Generally speaking, the most efficient power conversion systems cannot exclude the use of magnetic devices such as inductors and transformers [1] [2]. Designers often prefer to use discrete versions of these components because standard integrated circuit (IC) processes like BCD (Bipolar, CMOS, DMOS) or CMOS have never been intended to produce high-performance magnetics (nor piezoelectric devices). As a matter of fact, even if MEMS technology is considered nowadays something quite compatible with standard CMOS technology, it is actually something which is derived as "spin-off" technology from CMOS processes at the beginning of 80s'. The first inspiring papers by Roylance [3] (1979) and Petersen [4] (1982) are regarded as the first significant reviews on MEMS technology and its applications. Although the word "MEMS" can make the reader think about a real moving structure, actually this is not strictly necessary, given that, for example, a solenoidal inductor can be produced as a suspended structure [1] in the same way of MEMS piezoelectric cantilevers.

The primary target of a power conversion system is providing the highest efficiency conversion possible from input to the output. Linear regulators, do not use magnetic components, hence they are easily integrable. However the drawback of such regulators is the low efficiency, intended as the ratio between the output power and input power, which drops substantially when there is a significant difference between the input voltage and the output voltage.

Switching capacitor circuits [5] [6] [7] (also known as charge pumps or voltage multipliers) can achieve an efficiency higher than that of linear regulators. Furthermore they are easily integrable. The problem is that, every time a switched capacitor is clocked a fraction of power is lost. Considering that a charge pump is made by a series of switched capacitors, the power lost is given by $P_{lost}=\frac{1}{2}C(\Delta V)^2 f$, where f is the switching frequency, C is the capacitance, and ΔV is the difference across the switched capacitor.

DC-DC converters (buck, boost, buck-boost, flyback) make use of magnetic components: in general to provide a voltage regulation, the energy is exchanged in a proper way between a magnetic field (inductor or transformer) and an electric field (capacitor). Along with dimensions scaling and advances in IC technologies, frequencies have been increased as well, given that this allows to theoretically shrink also the value as well as dimensions of passive components (L,R,C) used in the circuit. Figure I.1 shows the trend of link between the size of magnetic components and frequency [2], whilst Figure I.2 [2], shows the evolution of systems from PCB to PwrSoC. In a conventional low frequency converter (f < 1MHz), all components stand together on a simple PCB, given that in general both capacitors and inductors are too big for being packaged together with the IC. In the range $1 \le f \le 10$ MHz, the inductor can be co-packaged with the IC, but still has a huge profile to be stacked. At frequencies beyond 10MHz, $10 \le f \le 20$ MHz, inductors can be stacked on the top of the chip, but some components still require to be outside. At frequencies approaching 100MHz, all components can stand together on the same chip [8]. Unfortunately, at frequencies in the range of 1-10MHz, integrated passive components have not the same performance, considering the same footprint area, of external passive devices:

STATE OF ART OF MINIATURIZED SYSTEMS WITH MAGNETIC AND PIEZOELECTRIC DEVICES



Figure I.1: impact of frequency increase in SMPS on the value of passive components. Graph obtained for a single phase buck converter with 5V in input, 1V in output, 2% voltage ripple and 0.3 peak to peak ripple current ratio [2] (© 2012, IEEE).



Figure I.2: Evolution of PwrSoC technology [2] (© 2012, IEEE).

from this problem comes the major challenge in further shrinking the dimensions. At frequencies beyond 10MHz up to 50MHz, the inductance value is so small that even air-core inductors (that is without the use of a magnetic core) can be used [9]. The elimination the magnetic core, can avoid one of the major losses in the system. However, in this case, even if theoretically integrable, problems of area usage arise because around these frequencies, integrated inductors can have footprint area of various mm² [2]. Furthermore Electro-Magnetic Interference (EMI) problems can arise, due to the fact that the magnetic field is not anymore confined. In addition it seems that placing air-core inductors on chip leads to lower efficiencies compared to

systems with off-chip inductors. This can lead to the conclusion that small and efficient PwrSoC or PwrSiP cannot exclude the presence of magnetic materials [2] [10].

Moore's law states that the number of transistors in CMOS (Complementary MOS) systems approximately doubles every 18-24 months. Generally speaking, this rule can be applied only to digital systems, whereas analogue or mixed systems follow a very different trend. However, as a matter of fact, Moore's trend can have some intrinsic limits. To cite an example, even if the increase of switching frequencies can lead to have smaller passive devices, a capacitor cannot be further shrunk without the discovery of new dielectric materials, hence even if there is some technology improvement in terms of dimensions scaling, capacitors will not be able to follow Moore's law. Furthermore too much thin oxide layers may be more sensitive to high voltages, thus limiting the applications. This statement is valid for inductors as well, which cannot be shrunk until new performant IC-compliant magnetic materials are discovered. Furthermore, to cite some other examples, high voltage devices and power devices as well have self-defining sizes, generally dictated by the laws of physics (for example heat dissipation) and they scale very poorly; as a matter of fact the majority of analog applications fall in the technology node of $0.13\mu m$ and above, given that when a certain technology is considered to be "mature" for producing digital systems, generally other three to five years are needed for using that particular technology with analogue circuits with these new embedded "functions". In this context, the integration of the chip together with specific devices or transducers (e.g. magnetic or piezoelectric) leads towards the so-called "more than Moore" trend (MtM), in which new functions can be embedded in a single (analogue) system in order to perform certain activities for specific applications.

Many works in literature [2] [9] [10] focus on the possibility of making integrated (at chip level) magnetic devices, via post-processing techniques like sputtering or evaporation but there is not any methodology to optimize the inductance value nor any work taking into account the most critical aspects in terms of performance and functionality which have to be considered during the design process of such magnetic components. This implies that, in order to overcome the limits of the Moore's trend, another approach of further shrinking dimensions of certain devices, could be the optimization of the performances of the devices themselves given a certain footprint area. Hence, in this field of applications the major challenge that is still present is the integration at die level, of magnetic devices such as inductors and magnetic transformers.

Concerning the dual piezoelectric counterpart, the analysis regarding integration can be considered valid for it as well. As a matter fact, the power delivered by a piezoelectric transducer is strictly dependent by its volume; given that the power requirements are linked by the particular application, it follows that the possibility of integration at wafer-level is mainly application dependent. To cite an example, MEMS for energy harvesting purposes are generally much larger than a single chip. A piezoelectric resonator instead, could be very small, in the order of hundreds of μm^3 [11].

A recent way of integrating piezoelectric materials together with Si-based CMOS process could be exploiting the piezoelectric properties of GaN (Gallium Nitride) [12]; even if the lattice constants between Si and GaN are pretty different, using some buffer layers can improve the growing of such materials on a Si substrate, thus reducing strain and leakage currents [13], and hence improving the performance of devices.

Generally speaking, the way of integrating MEMS piezoelectric devices together with ICs is the same as previously seen with magnetic devices: 1) with separate processes and then including devices as well as ICs in the same package (SiP), or 2) integration at wafer level (SoC) [14]. However, piezoelectric materials are one step forward compared to magnetic materials. To cite an example, inductors typically require windings, which pose fabrication constraints. Although air-core inductors can be directly integrated in both ways, generally inductors with magnetic materials as core are produced with several post-processing steps after the IC, given that many magnetic materials are not fully clean room compliant. On the other way, there are a lot of piezoelectric materials such as AlN (Aluminum Nitride), ZnO (Zinc Oxide), SiN (Silicon Nitride), fully compatible and compliant with IC techniques and clean rooms [14]. Furthermore, piezoelectric devices do not require windings, and are typically composed on patterned planar layers, which simplify their production. In general, these materials are deposited with techniques like sacrificial surface micromachining, because the devices are produced on the top of the wafer, via subsequent deposition of different materials, using the so-called *sacrificial layers*, which are particular layers (e.g. photoresist) used as base for the deposition of the materials constituting the structural layer, and then removed to obtain free standing devices, such as piezoelectric cantilevers or membranes; whereas MOS transistors are produced "within silicon", through the definition of the active area. Another technique for producing MEMS piezoelectric devices is *bulk micromachining*, by which devices are produced within the Si substrate, by a real "digging" of the substrate [15].

In this "piezoelectric" context as well, we fall again in the MtM trend, because piezoelectric devices can be fully integrated with the IC. Before, we talked about compact power systems such as PwrSiP or PwrSoC mainly focusing on magnetic devices. If we contextualize these systems in the application field of Power conversion or Energy Harvesting (EH), we realize that a challenge arises. Energy Conversion can be performed by using piezoelectric transformers, which offer better performance than their magnetic counterparts, but require specific design efforts in conversion control. If we want to power some Wireless Sensor Nodes (WSN), it would be desirable if such systems could be fully autonomous by harvesting the energy present in the environment, given that battery replacement can require too much effort in many application scenarios. The challenge here is power conversion from piezoelectric harvesters with output voltages in the order of few tens of mV, thus insufficient to overcome the threshold voltage of power devices in a typical PwrSiP or PwrSoC.

Then, the study of application of miniaturized piezoelectric devices, like transformers, can also benefit this type of applications. In order to exploit and step-up the ultra-low voltage coming from harvesters such as TEGs (ThermoElectric Generators) or PhotoVoltaic Cells (PV-C) into a usable voltage, it is necessary to overcome the threshold voltage of the power devices in power converters, as previously stated. Until now this was accomplished by means of the so-called boost (or step-up) oscillators which make use of low-threshold (typically normally-on) transistors such as Depletion MOSFETs or JFETs coupled with a magnetic transformer in the classic Armstrong oscillator topology. Then, voltage rectifiers amplify and rectify the generated growing oscillations. However in the perspective of having more and more efficient as well as more and more compact systems following the Moore than Moore's philosophy, a new type of oscillator made with PTs

(Piezoelectric Transformer) was modelled and tested, showing that it is possible to reach very low values of minimum activation voltages (the one provided by the harvester), if the system is integrated. Furthermore, the application of harvesting systems falls in the μ W range, hence the dimensions of the PT as well can be shrunk down to few mm³, given that discrete PTs are designed and optimized to handle power in the range of few W and voltages up to hundreds of V. In this context, MEMS PTs might be useful and integrated at package level with the IC, in order to make a fully autonomous PwrSiP for EH purposes, since the piezoelectric transduction can be much more efficient than the electromagnetic one as stated before. However discrete PTs, are generally made of PZT (Lead Zirconate Titanate, which is not truly piezoelectric but rather electrostrictive), which is not compatible with IC techniques and processes, because of the presence of the lead. Alternatively, MEMS PT can be successfully made in ZnO or AlN, which unfortunately have not a piezoelectric effect as strong as the PZT. Furthermore, the number of interleaved layers at the primary side in a PT acts like the turn ratio in a MT (Magnetic Transformer), so the possibility of having multiple piezoelectric layers in a MEMS process could be worth future investigations.

This PhD Thesis faces the problems of integration and application of magnetic and piezoelectric devices, in order to complement the design of CMOS integrated circuits.

This first section is a brief introduction to current state of art (SoA) of MtM systems which exploit magnetic and piezoelectric devices.

Chapter 1 gives a brief summary of magnetic properties of materials, as well as some examples of SoA of integrated magnetic inductors and transformers.

Chapter 2 deals with the physics of magnetic field and makes an analysis of how micro-magnetic inductors and transformers can be modelled, in order to extrapolate some basic equations useful to assess the performance of magnetic devices. The chapter gives also some new considerations of the so-called *Magnetic Path Length* for square planar toroidal inductors, and gives a new formula for the correct estimation of its value (from which the inductance value depends) without the aid of time consuming FEM (Finite Element Methods) simulators.

Chapter 3 deals with the optimization of planar square integrated inductors for on-chip integration.

Chapter 4 deals with the physics of direct and inverse piezoelectric effect, and with the equivalent lumped electro-mechanical circuit of PTs.

Chapter 5 describes a new type of step-up oscillator which uses discrete PTs in place of MTs and which can be, in perspective, shrunk in dimensions and improved in performances if dedicated ICs and MEMS PTs are used, in order to achieve a full and autonomous PwrSiP or PwrSoC.

Chapter 6 shows the design, fabrication and characterization of MEMS PTs in AlN performed at the TUW (Technische Universität Wien) during the internship from February 2015 to August 2015.

Chapter 7 concludes the dissertation with some considerations on the magnetic and piezoelectric technologies.

Chapter 1

Magnetic materials and applications

The miniaturization of electronic systems, together with the increase of functionality and performance, from portable electronics to high-end computing, is providing extremely important challenges for engineers and power converters designers, since in a typical power management system, magnetic components such as inductors and transformers are still the bulkiest parts.

This chapter presents a brief overview on the magnetic materials, figures of merit and techniques in order to produce integrated and miniaturized magnetic components for power applications.

1.1 Properties of magnetic materials

A magnetic material is a material that is able to *sense* the effect of an external applied magnetic field. This *sensing* capability is represented by the so called magnetic permeability μ_r which can be considered the dual of the dielectric permeability ε_r which represents the capability of a material to sense and amplify an electrostatic field. To amplify the electric capacitance, materials with $\varepsilon_r > 1$ must be

used, and in general to make inductors for power applications, materials with $\mu_r > 1$ must be used. The sensing capability, is essentially due to the fact that magnetic materials present *magnetic dipoles* that are able to be fully aligned with an external magnetic field, thus resulting in an amplification.

Magnetic materials can be divided in two main groups: *hard* and *soft*. Hard magnetic materials present a B-H static curve which is extremely non-linear, in fact these materials are generally used to make permanent magnets, given that their B-H curve presents an important hysteresis (red and black curve in **Figure 1.1**).

Ideal soft magnetic materials (blue line in **Figure 1.1**) present a B-H curve that is a straight line, however even these materials presents a hysteresis curve that is in general much littler than the hard ones (green curve in **Figure 1.1**).

The major parameters of interest for magnetic materials are:

- Small signal relative magnetic permeability μ_r
- Resistitivity ρ_C
- Losses per unit volume p_V
- Cutoff frequency (bandwith) f_T
- Saturation flux density B_S
- Coercive field H_C

A good magnetic material to be used for inductors/transformers for power applications should have $\mu_r \rightarrow \infty$, $f_T \rightarrow \infty$, $\rho_C \rightarrow \infty$ and $p_V \rightarrow 0$. These quantities are strictly linked together and we will discuss later on how, for example, the finite value of the resistivity limits the bandwidth and increases the losses. Unfortunately, the materials with the highest μ_r present, at the same time, very low values of ρ_C . Nanocrystalline, and amorphous Co-based alloys (e.g. Vitrovac 6025 from Vacuumschmelze) present the highest values of μ_r (up to 10^5 and more), but at the same time a resistivity around $120-140\mu\Omega\cdot cm$. In general, some ferrites (Co based, Mg based, NiZn based) have a resistivity up to $10^7 \ \mu\Omega\cdot cm$. Other types of ferrites (Cu/Mn/MnZn/Zn/ based) have a resistivity ranging from $10^5 \ \mu\Omega\cdot cm$ (Cu based) to $10^2 \ \mu\Omega\cdot cm$ (Zn based). The Fe-based ferrite has a $\rho_C \approx 4 \cdot 10^{-3} \mu\Omega\cdot cm$. Alloys presents a resistivity ranging from hundred to tens of $\mu\Omega\cdot cm$. Concerning the permeability, **Table 1.1** [1] presents typical values of small signal permeabilities of magnetic materials.



Figure 1.1: Hysteresis cycles: Blue line: ideal soft magnetic material, black and red: hard magnetic material, green line: real soft magnetic material.

Material	Relative Permeability μ_r
Powder (Iron or iron alloys)	10-60
NiZn ferrite	150
Cobalt	250
Nickel	600
50% Nickel, 50% Fe "orthonol"	2000
MnZn ferrite	1000-4000
0.25% Si iron	2700
48% Ni alloy	4000
2.5% Si steel	5000
4% Si steel	7000
50% Co alloy	10000
Metallic glass	10000
Nanocrystalline	15000-150000
80% Ni, 4% Mo alloy	50000
Mumetal 75% Ni, 5% Cu, 2% Cr	100000
99.96% iron	2800000
79% Ni, 17% Fe, 40% Mo "permalloy"	12000-100000
79%, 5% Mo Supermalloy	1000000

Table 1.1: Relative small signal permeabilities of typical materials used for cores [1].

The saturation flux density B_S is that particular value of magnetic flux density inside the material beyond which the material starts to be transparent to the external applied magnetic fields, because all the magnetic dipoles inside the materials are aligned. Typical values are 0.3T for NiZn ferrites, 0.4-0.8T for MnZn ferrites, 1.2-1.5T for Ni-Fe alloys, up to 2.3T for 50% Co alloys [1].

The coercive field H_C (for hard magnetic) is the particular value of external magnetic field H, that must be applied in order to eliminate any possible stored magnetic moment inside the material.

1.2 Distinction between magnetic materials

From the point of view of interaction with an external magnetic field H, all materials can be divided in five groups: *ferromagnetic*, *antiferromagnetic*, *ferrimagnetic*, *diamagnetic* and *paramagnetic* materials.

Ferromagnetic materials, like iron, nickel, cobalt are materials with $\mu_l >>1$ (much higher than unity) [1]. Their permeability can reach up to 10^6 like Mo-Ni super-permalloys. In general they can present a net magnetization due to a partial alignment of all its magnetic domains below their Curie temperature (that is the temperature above which they cease to exhibit a ferromagnetic behaviour). Antiferromagnetic materials are materials with $\mu_{r} > 1$ (slightly greater than unity): in this type of materials not all the magnetic domains are able to be aligned in the same way of the applied magnetic field, and so the net magnetization is not high as ferromagnetic ones. In the absence of an external magnetic field, the net magnetization is zero. For diamagnetic materials (bismuth, copper, diamond, lead, mercury, silver and silicon) the magnetic permeability is slightly lower than unity: $\mu_r = 1 - \varepsilon$, where $\varepsilon \approx 10^{-5}$. For example for copper $\mu_r = 0.99999$, or $\mu_r = 0.99998$ for silver. Paramagnetic materials (aluminium, calcium, chromium, magnesium, platinum, titanium, tungsten) are the dual of diamagnetic materials: the amplification is extremely weak: $\mu_r = 1 + \varepsilon$, where $\varepsilon \approx 10^{-5}$. Ferrimagnetic materials have a relative magnetic relative permeability $\mu >>1$. They have a population of atoms with opposing magnetic moments, as in antiferromagnetic ones; however, in ferrimagnetic materials, the opposing moments are unequal and a spontaneous magnetization is still present due to a partial alignment of some of the magnetic domains.

1.3 Deposition processes for thin film integrated micro-magnetic components

In literature [2], the most diffused techniques for the deposition of thin (from hundreds of nm up to several μ m) magnetic films on chip are: *screen printing*, *sputtering* and *electrodeposition*.

The screen printing is suitable for the deposition of non-metallic films with a thickness higher than 1µm. NiZn and MnZn are typical soft magnetic materials deposited through this technique. In general the material that has to deposited is as the core materials issuspended in a polymer matrix. This technique has been proved to be suitable for the microfabrication of core inductors, presenting a good compromise between core resistivity (>1 Ω ·m) and process simplicity. However, because of the very high temperatures involved during the process, it is not compatible with CMOS (Complementary MOS) or MEMS (Micro-Electro-Mechanical Systems) processes.

The **sputtering** process is fully compatible with IC processes. Furthermore it has the advantage of a proper control of the surface and thickness of material that has to be deposited. A wide range of materials, including oxides and alloys can be deposited on the chip via this technique, which theoretically allows also the formation of laminated cores, given that, as said before, oxides as well can be sputtered. Unfortunately this technique is suitable for the deposition of only few hundreds of nm of thickness, because beyond this thickness, the technique starts to be slow and too much expensive.

The **electroplating** deposition process can provide films with a controlled thickness; furthermore the process is not expensive and relatively fast compared to the sputtering process. The most frequently electroplated material is the permalloy [2] (81% Fe and 19% Ni). Supermalloys and other alloys as well have been reported to be deposited via this technique [2]. In general materials deposited through this technique present high saturation flux density (around 1.8T), very high permeability, but unfortunately very low resistivity. Furthermore [2] presents a brief overview of materials deposited in literature, including the used technique, permeability, thickness and resistivity of the material used for the fabrication of micro-inductors.

1.4 Integrated/MEMS compatible inductors and transformers

Advances in technology dimensions scaling together with increasing switching frequencies in power converters, is leading towards further miniaturizations of electronic circuits. However, in this field of applications the major challenge that is still present is the integration at die level of magnetic devices such as inductors and magnetic transformers.

Integrated inductors can be made by exploiting the metal layers available in IC processes. These processes, depending on their complexity, can have from three to eight different metallization levels. The thickness of each layer may typically vary from ~0.5µm to ~4µm, with the last one being the thicker among the others. The last metal level of an IC process thus can be theoretically used to make inductors or transformers due to its lower sheet resistance (less than $10m\Omega/\Box$). To cite an example, on-chip planar air-core inductors can be simply made with a spiral metallization, generally the thicker metal layer of an integrated circuit (IC), in order to reduce the DC series resistance, as said before. Their applications usually fall in the RF range, whereas for frequencies under 100 MHz, inductors with a magnetic core are still more performant than air-core inductors [2], since the AC losses due to skin depth in the core grow very fast with f^b (Steinmetz equation), where f is the frequency and b is a coefficient ranging between 2 and 3 [9] [10]. Hence at high frequencies the losses due to the magnetic core become more dominant.

Typical geometries of such type inductors can include the Meander inductor, the spiral or the single turn planar inductor. These geometries [16] [17] [18], shown in **Figure 1.2**, are lacking a magnetic core and are in general used for RF applications, as stated before. In general the width and the distance between two adjacent stripes in such inductors must follow certain design rules. These geometries are not intended for use as power inductors for PwrSoC, because the achieved inductance values are pretty low and the resistance is very high. Even if a magnetic sheet is deposited on top the metal, because of the demagnetization of the sheet (cfr. Chapter 2), the inductance enhancement is very low. In addition, the produced magnetic field goes through the entire circuit causing possible problems of EMI. Transformers can be formed by



Figure 1.2: Top view of shapes of inductors used in RF applications.

using a lower metal line, or a metal at the same level with an interleaved geometry. In [19] a 20mm^2 power IC was produced with a "sandwich" spiral inductor with metal of huge thickness of 35µm and 9µm of magnetic layers. The achieved inductance is about 0.96µH at 0.35A of current and 3MHz switching frequency. The achieved efficiency is around 83%.

In [20] a boost converter with micro-machined inductor was presented. The inductance was obtained through a MEMS-LIGA (Lithographie, Galvanoformung, Abformung - Lithography, Electroplating, and Molding) process, which allows producing structures with a very high aspect ratio. The switching frequency was varied from 3MHz to 10MHz.

In [21] an inductor exploiting bondwires (**Figure 1.3**) for making closed currents turns was presented. The winding is embedded in a glob of magnetic epoxy core that can be formed to cover the bondwires during the SoC packaging process by various techniques such as brushing, squeegeeing, dripping, inking, etc. In perspective the presented device, based on the use of ceramic magnetic material to achieve low losses and hence good quality factors, is combined with the standard packaging of ICs. The extreme simplicity of the structure allows a powerful integration for system on chip (SoC), because an entire circuit such as DC/DC converter, can be integrated with standard Si technology, whereas the magnetic component is stacked above the chip.

In [22] (cfr. **Figure 1.4**) a flat toroidal inductor with a laminated $Ni_{80}Fe_{20}$ magnetic core was presented. The metal turns are pretty thick (20µm) and obtained via Electro-Chemical Deposition (ECD). The laminated core is obtained via Physical Vapor



Figure 1.3: Bondwire winding embedded in glob of magnetic epoxy core [21]. (© 2010, IEEE).



Figure 1.4: Toroidal MEMS microinductor [22] (© 2006, IEEE).

Deposition (PVD) and then patterned with wet etching. The process fabrication is MEMS-oriented and fully compatible with IC processes. The design is focused towards a maximization of L/R_{DC} ratio, with L as the inductance and R_{DC} as the DC series resistance of the inductor for a given footprint area. In fact, the low frequency quality factor of an inductor is proportional to this ratio unless skin depth in the core and in the winding lowers the inductance value and raises the equivalent series resistance. In [23] toroid and solenoidal inductors were presented, with the main target to minimize the footprint area. The conductors were deposited via electroplating, whereas the core made in CoTaZr was deposited via sputtering and then patterned through etching. This inductor as well, is fully compatible with IC

processes. About 70nH were realized with a 34X enhancement factor with respect to the same inductor with no core. The footprint area is 1mm^2 , and the DC resistance is lower than 1Ω . However, because of magnetic losses, the maximum usable frequency is around 10MHz.

Other geometries include race-track shaped (pot-core) micro-inductors (cfr. **Figure 1.5**) in which, instead of wrapping a conductor around a magnetic core the magnetic material is wrapped around a conductor [24] [25] [26] [27] [28] [29]. In [24] and [25] on-chip micro-inductors made by exploiting advanced CMOS processes (130nm [24] and 90nm [25]) that incorporate high-permeability (850-1100) laminated magnetic materials, and resistivity of about $100\mu\Omega$ ·cm. In both works, a CoZrTa magnetic material was used. This particular material has been proved to be usable to frequencies up to 9.8GHz in case of small inductors [24] with a single lamination placed above a spiral conductor. In this particular case, the inductance enhancement with respect to the air-core inductor is only of 10%-30% because of demagnetization of the material. However, when a sandwich structure is used, depending on magnetic material thickness, enhancement of 16X-19X can be achieved. The drawback is that the bandwidth is reduced.

In [26] a micro-fabricated transformer consisting of a racetrack shaped copper winding of 30µm of thickness is presented. The structure is always a pot-core type with a magnetic material made up by two layers of Ni₄₅Fe₅₅ (~4.5 µm thick). The bottom magnetic layer is deposited through electroplating and patterned on native oxide insulated silicon wafer. The copper electrodes are electroplated on a patterned BCB which serves as insulation layer between the winding and the bottom magnetic layer. The upper magnetic layer is deposited and patterned using the same electroplating process as the bottom one, on a patterned on an epoxy type photoresist (Su-08), which is 50 µm thick, insulating the top layer from the winding. Both single (SLM) and double layer (DLM) copper winding were reported. To cite an example, the DLM presents a magnetizing inductance of 210nH at 20MHz and ~1 Ω of DC resistance. The gain is about -1dB at 50 Ω load in the range 5MHz-50MHz. The footprint area is less than 4mm².

In [27] footprint areas below 3mm^2 were achieved, according to the space used to make the metallization. 160nH were obtained in 2.5mm^2 with a DC resistance of about ~0.45 Ω and tested with a converter operating at 30MHz, with input voltage of



Figure 1.5: cross section (top) and top view (bottom) of a racetrack pot-core spiral micro-inductor.

1.8V and output voltage of 1V and 500mA of output current, showing a global efficiency of 74%. However the estimated inductor efficiency (considered as the ratio of converter output power to output power plus inductor loss) is more than 90% at 150mA current load, suggesting that the majority part of losses are due to the DC resistance of the inductor (more than 75%). In [28] the presented micro-inductor has a peak efficiency of 93% and performances comparable to commercial solutions; however the occupied area, about 7.5mm², is the main drawback. In [29] inductors and transformers for power applications were presented, using always the pot-core structure. The performance of the devices, were quite good, with efficiencies up to 94%. The main drawback is the footprint area of several tens of mm².

On-chip inductors can be also fabricated by exploiting structures and components already available in CMOS technology and packaging, such as integrated metal layers for the lower metallization level and bonding wires for upper metallization or through flip-chip bonding combined with microelectromechanical system (MEMS) oriented processes [30]. Bonding wires, usually made up of gold due to its high conductivity (about $4.5 \cdot 10^7$ S/m at room temperature), are normally used as chip interconnections in speed circuits, because even few additional nH can affect performances in high-clock applications, *e.g.* tens of GHz; where flip-chip bonding is a preferable

alternative due to the shorter interconnections between chip and package. Typical inductance of bonding wires is about 1-2nH for every mm of length [29] and they can be used also as standalone inductors.

Other types of micro-fabricated magnetic devices, fully compatible with IC processes, include bondwires inductors/transformers [32] [33] [34] (cfr. Figure 1.6 and Figure 1.7). In this kind of implementation the toroidal core is placed between the lower metal lines (that could be either on PCB or exploiting the metal levels of an IC process) and bondwires which are used to close the current turns. In such a way, inductances up to 315μ H [33], with DC resistance of 4.3Ω were obtained in a footprint area of about 24 mm². These structures have been proved to be useful for micro-power conversion such as boost converters for ultra-low voltage step-up purposes. In [34], an on-chip bond wire transformer for MHz frequency range is presented, with a Low Temperature Co-fired Ceramic (LTCC) core and in a footprint area of about 15 mm².

1.5 Summary

This chapter has presented a brief introduction to the magnetic materials, their most important parameters like resistivity and relative permeability. Additionally a short overview on the most diffused techniques used to produce integrated and miniaturized magnetic components, together with some examples of the state of art of miniaturized magnetic devices was presented.



Figure 1.6: A 315µH bondwire microtransformer [33] (© 2014, IEEE)



Figure 1.7: An LTCC based 29μH bondwire microtransformer integrated at die level on a 0.35μmST Microelectronics BCD technology [34] (© 2014, Procedia Engineering)

Chapter 2

Modelling of integrated magnetic components

Magnetic components are devices which make use of the magnetic field in order to store or transfer energy (or power). A typical element which stores the energy in a magnetic field is the inductor whilst a typical element which transfers/stores energy is the magnetic transformer, which converts electric energy in the form of a magnetic field and then back again to electric field. Almost all electronic circuits, such as power converters or harvesting systems require the use of such magnetic components which in general are extremely difficult to integrate, and are the bulkiest and most expensive part of the whole circuit.

In order to understand the behaviour of such components a review of magnetic properties is needed, in order then to extrapolate basic equations and relationships useful for the design and optimization of such components.

2.1 Overview on Magnetic relations

The first equation to introduce is one of Maxwell's equations: the Ampère's law:

$$\oint_{C} \mathbf{B} \cdot d\mathbf{r} = \mu_{0} \mu_{r} \iint_{S} \mathbf{J} \cdot d\mathbf{S} = \mu_{0} \mu_{r} \mathbf{I}_{enc}$$
(2.1)

which states that the line integral of the magnetic **B**-field density (measured in Tesla, T) around the closed curve C is proportional to the current I_{enc} passing through a surface S (enclosed by C). The equation can be used to find the value of inductance of a closed core toroid with magnetic permeability $\mu_r \gg 1$ and N turns, in this case (2.1) becomes:

$$\oint_{C} \mathbf{B} \cdot d\mathbf{r} = \mathbf{B} \cdot 2\pi \mathbf{r} = \mu_{0} \mu_{r} N \mathbf{I}_{enc}$$

$$\Rightarrow \mathbf{B} = \mu_{0} \mu_{r} \frac{N \mathbf{I}_{enc}}{2\pi \mathbf{r}} = \mu_{0} \mu_{r} \frac{F_{MM}}{l_{C}} = \mu_{0} \mu_{r} H$$
(2.2)

in (2.2) the term $F_{MM}=N\cdot I_{enc}$ is the MagnetoMotive Force (A·turns), $l_C=2\pi r$ is the Magnetic Path Length (MPL), whereas the quantity H is the magnetic field intensity. The quantity μ_0 ($4\pi \cdot 10^{-7}$ H/m) is the vacuum magnetic permeability.

Combining the electromagnetic induction's law with (2.2) then we have:

$$\mathbf{E}_{EM} = \left| \frac{d\Phi_B}{dt} \right| = \left| \frac{dB}{dt} \right| \cdot A_C = A_C \cdot \frac{\mu_0 \mu_r}{l_C} \frac{dF_{MM}}{dt} = A_C \cdot \frac{N\mu_0 \mu_r}{l_C} \frac{dI_{enc}}{dt} = L \frac{dI_{enc}}{dt}$$
(2.3)

The parameter A_C in (2.3) is the cross section of the closed toroid whereas the quantity $L = A \cdot N \mu_0 \mu_r / 2\pi r$ is called *self-inductance* (H), and indicates the capability of a conductor to produce an electromotive force across its edges when an AC current flows into it.

Figure 2.1 shows the relationship in a ferromagnetic piecewise linear (ideal) material, between the B field and H field. Every hard magnetic material has a value of magnetic field intensity H_s , and hence of current, beyond which the material starts to behave like the vacuum. At this value corresponds a value $B_s = H_s/\mu_r$ of saturation flux density. Since the value of H is also proportional to the turn number *N*, the higher



Figure 2.1. Relation between magnetic flux density and magnetic field intensity.

number of turns in an inductor should carry less current in order to prevent core saturation, because H is related to the MagnetoMotive Force F_{MM} .

2.2 Magnetic circuits

In case of inductance cores with a very high magnetic permeability, it could be useful to deal with them through the so-called Hopkinson's law (see **Figure 2.2**), that can be considered the dual of the Ohm's law for the electric circuits. In this case we can speak about magnetic circuits. As for electric circuits we can define the electric resistance $R=l/\sigma \cdot A$, and the Ohm's law as $V=R\cdot I$, we can substitute the ElectroMotive Force with the MagnetoMotive Force F_{MM} , the current with the magnetic flux Φ_M , the electric conductivity σ with the magnetic permeability μ the and the electric resistance R, with the *Reluctance* \Re , which is given by the following equation [1]:

$$\Re = \frac{l_c}{\mu A_c} \tag{2.4}$$

Hence the Hopkinson's law [1] is defined as:



Figure 2.2. Magnetic circuit.

$$F_{MM} = \Re \Phi_M \tag{2.5}.$$

The Reluctance \Re then is a measure of how much the magnetic flux encounters a "resistance" in flowing in a magnetic core, once a current has been applied to the inductor's terminals, as the electric resistance *R* measures the resistance encountered by the current in flowing in an electric circuit once a voltage has been applied. Furthermore, as it can be seen from (2.4), the electric resistance and magnetic reluctance have a very similar expression. The inverse of the reluctance $\wp = 1/\Re$ is called *Permeance*.

2.2.1 Air gaps

Generally, inductors are not used in a closed core configuration. This is because the inductance value is strictly dependent on the magnetic permeability which in turn is dependent on frequency, losses, temperature, current value, etc. A way to make the inductance independent from the magnetic permeability of the material is to introduce a small air gap of length $l_G \ll l_C$. In order to find the effective inductance, we can use the similarity between the reluctance and electric resistance. In this case, we have two reluctances in series, the one of the core, and the one given by the small air gap, hence [1]:

$$\mathfrak{R}_{eff} = \frac{l_C - l_G}{\mu_o \mu_r A} + \frac{l_G}{\mu_o A_C} \cong \frac{l_C}{\mu_o A_C} \left(\frac{1}{\mu_r} + \frac{l_G}{l_C}\right) = \frac{l_C}{\mu_o A_C} \left(\frac{l_C + \mu_r l_G}{\mu_r l_C}\right) = \frac{l_C}{\mu_o A_C} \frac{1}{\mu_{eff}}$$
(2.6)

The quantity μ_{eff} , given by the following expression:

$$\mu_{eff} = \frac{\mu_r l_C}{l_C + \mu_r l_G} = \frac{\mu_r}{1 + \mu_r \frac{l_G}{l_C}}$$
(2.7)

is called *effective magnetic permeability*, in fact, if $l_C/l_G \ll \mu_r$, then $\mu_{eff} \cong l_C/l_G$, hence it depends only by the ratio between the core length and air gap length. In addition, the presence of the air gap acts like a feedback in the magnetic reluctance, making the overall reluctance independent from the material parameters.

Once the value of the effective reluctance is known, then the *effective inductance* is given by:

$$L_{eff} = N^2 / \Re_{eff}$$
(2.8)

However it is worth noting that the concept of the reluctance remains valid only for closed cores with an eventual very small air gap. The air gap essentially takes into account the demagnetization factor of the material, which is strictly dependent on the shape the core. As a matter of fact, considering two cores, with same cross section, length and magnetic permeability, but with different layout like toroidal configuration and solenoid configuration, will produce extremely different results in terms of inductance. Furthermore, as the gap length l_G increases, the *fringing flux* leaking outside the core cross section becomes more and more important, thus partially invalidating the previous equations. This also happens for capacitor, as a matter of fact the formula of a two parallel plates capacitor $C=A\varepsilon_0\varepsilon_r/l_p$ (resembling the formula
of a magnetic permeance) is valid only when l_p is small enough such that there is not any fringing electric field.

2.3 Modelling of inductors

The self-inductance of a closed toroid inductor or an infinite length core solenoidal inductor, have the same inductance value, which is given by:

$$L|_{l_{C\to\infty}} = \frac{A_C \mu_0 \mu_r N^2}{l_C} = \frac{N^2}{\Re} \,.$$
(2.9)

However, in general, finite-length solenoids suffer from demagnetization of the core, which lowers the effective magnetic permeability. This happens because the magnetic flux density, assuming for simplicity a cylindrical core, along its axis x of simmetry is not uniform, and has the following expression [35]:

$$B(x) = \frac{\mu_0 \mu_r nI}{2} \left[\frac{l_c + 2x}{\sqrt{(l_c + 2x)^2 + 4r^2}} + \frac{l_c - 2x}{\sqrt{(l_c - 2x)^2 + 4r^2}} \right]$$
(2.10)

In (2.10), *n* is the linear turn density wrapped around the core, *r* is radius of the core. **Figure 2.3** shows the distribution of the axial magnetic flux density as a function of distance between the core centre, with various ratios between the core radius and length. The B field has been normalized versus the maximum field that is $B_{\text{max}} = \mu_0 \mu_r nI.$

Furthermore, to cite an example, for a small cylindrical bar with a radius of the cross section which is smaller than the longitudinal length ($r < 1.25l_c$), the inductance value can be approximated by the expression [1]:

$$L_{eff} = \frac{A\mu_0\mu_r N^2}{l_c + 0.9r} = \frac{A\mu_0\mu_r N^2}{l_c \left(1 + 0.9\frac{r}{l_c}\right)},$$
(2.11)

meaning that the effective permeability for relatively short solenoids, is given by:



Figure 2.3: Magnetic flux density distribution along the axial direction of the core.

$$\mu_{eff} \cong \frac{\mu_r}{\left(1 + 0.9\frac{r}{l_c}\right)} \tag{2.12}$$

2.4 Magnetic Path Length (MPL)

In all the previous expressions the parameter l_c was taking into account the so called magnetic path length (*MPL*). The reluctance formula (2.4) gives information about the mean magnetic path length. In literature, in general, a way to find this value was to simply make the arithmetic average between the internal and the external perimeter of the core.

Although this can give numerically correct results in many practical cases, the procedure is conceptually and mathematically wrong because there is the implicit assumption that the magnetic flux density B is uniform along the entire core cross-section. Nevertheless, the magnetic flux density follows the lowest reluctance path (as electric currents follow the paths with the lowest electric resistance [1]), and since in a small neighborhood of the internal perimeter, the path length is the shortest, the magnetic flux density will be much more concentrated closer to the internal perimeter of the core. This means that the magnetic flux density is not uniform along the entire cross section of the core, and intuitively the geometric average between

internal and external perimeter should better predict the magnetic flux density preferred path.

To cite a simple example, for a cylindrical toroid (Fig. 2.4), with internal radius R_1 , and external radius R_2 , the mean MPL can be found through averaging of the Ampère's law:

$$\overline{B} = N \cdot I \frac{\mu_0 \mu_r}{2\pi} \frac{\int_{R_1}^{R_2} \frac{dr}{r}}{R_2 - R_1} =$$

$$= N \cdot I \frac{\mu_0 \mu_r}{2\pi} \frac{\ln\left(\frac{R_2}{R_1}\right)}{R_2 - R_1} = N \cdot I \frac{\mu_0 \mu_r}{2\pi r}$$
(2.13)

This means that the average MPL for a toroid with cylindrical symmetry is given by:

$$MPL_{Circ} = \frac{2\pi \left(R_2 - R_1\right)}{\ln \left(\frac{R_2}{R_1}\right)} = \frac{P_{EXT} - P_{INT}}{\ln \left(\frac{P_{EXT}}{P_{INT}}\right)}$$
(2.14)

The truncated Taylor series expansion of (2.14) when $P_{EXT} \cong P_{INT}$ is $MPL \approx \pi(R_2 + R_1)$, which can correspond either to the arithmetic or geometric average between external and internal perimeter: as a matter of fact both of them have the same truncated Taylor series. Besides, if we cut in *j* extremely small concentric slices a circular crown, thanks to the symmetry of the structure, the magnetic flux density as well has a cylindrical symmetry and this means that the *j* small concentric slices can be considered as *j* reluctances in parallel because there is not any interaction between them, that is to say that both the reluctances and the magnetic flux density have the same cylindrical symmetry.

Let's consider for simplicity a square shaped toroidal core (SSTC) like the one in **Figure 2.5**. Be L_A and L_B the internal and the external sides of the square core respectively. $P_A = 4 \cdot L_A$ is the internal perimeter, whilst $P_B = 4 \cdot L_B$ is the external perimeter, and W is the core width: obviously it holds that $W = (P_B - P_A) / 8$. Now the core width can be divided in several *j*+1 slices as shown in **Figure 2.5**. The value of *j* is big enough such that the ratio between the external and the internal perimeter of the *i*-th slice is $P_{B,i} / P_{A,i} \approx 1 + \Delta P$, with $\Delta P \ll 1$.

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Figure 2.4. Top view of a toroidal core divided in several slices [36] (© 2015, IEEE).



Figure 2.5. SSTC divided in several slices [36]. (© 2015, IEEE).

The perimeter length of the *i*-th slice can be written as:

$$P_i = P_A + \frac{8W}{j}i \tag{2.15}$$

The variable *i* assumes all the j+1 integer values between 0 and *j*. Thus the reluctance of the independent *i*-th slice is:

$$\Re_i = \frac{P_i}{A_{C,i} \cdot \mu_0 \cdot \mu_r}$$
(2.16)

In (2.15), $A_{C,i} = W/j$ is the normalized cross section against the core thickness *t* of the *i*-th slice.

According to the Hopkinson's law, more reluctances can be considered in parallel if the same MagnetoMotive force (F_{MM}) is applied over them. However, due to the corner effect ([37] [38] [39]), the magnetic flux in each slice is round in the corners and not right: this means the j+1 slices cannot be considered in parallel because a small amount of the magnetic flux (arrows in **Figure 2.5**) flowing in the *i*-th slice, leaks in the [*i*–1]-th slice, because it is not physically able to follow the right angles of the corners.

Now let's assume that the j+1 reluctances are all in parallel, then the total reluctance would be:

$$\Re_{TOT} = \Re_{0} / / \Re_{1} / / \Re_{2} / / ... / / \Re_{j} = \frac{1}{A_{C,i} \cdot \mu_{0} \cdot \mu_{r}} \times \frac{\prod_{i=0}^{j} P_{i}}{\prod_{i=0}^{j} P_{i} + \prod_{i=0}^{j} P_{i}} = \frac{1}{W \cdot \mu_{0} \cdot \mu_{r}} \times \frac{j}{\sum_{i=0}^{j} \frac{1}{P_{i}}}$$
(2.17)

In the previous equation, the operator "//" means a parallel combination of two elements (*e.g.* $a//b = (a \cdot b) / (a+b)$). From (2.17) we can state that the effective mean *MPL* is:

$$MPL_{eff} = \lim_{j \to \infty} \frac{j}{\sum_{i=0}^{j} \frac{1}{P_i}} = \lim_{j \to \infty} \frac{j}{\sum_{i=0}^{j} \frac{1}{P_A + \frac{8W}{j}i}}$$
(2.18)

As *j* approaches infinity, the quantity $8(W/j) \cdot i$ varies with continuity between 0 and 8 *W*, when *i* varies from 0 to *j*. We can put $8(W/j) \cdot i = x$ and since $\Delta i = 1$, $dx = 8(W/j) \cdot \Delta i = 2 \Delta i = dx / [8(W/j)]$. So we have:

$$MPL_{eff} = \lim_{j \to \infty} \frac{j}{\sum_{i=0}^{j} \frac{1}{P_A + \frac{8W}{j}i}} = \lim_{j \to \infty} \frac{j}{\sum_{i=0}^{j} \frac{\Delta i}{P_A + \frac{8W}{j}i}} = \lim_{j \to \infty} \frac{8W}{\int_{0}^{8W} \frac{dx}{P_A + x}} = \frac{8W}{\ln\left(\frac{P_A + 8W}{P_A}\right)} = \frac{P_B - P_A}{\ln\left(\frac{P_B}{P_A}\right)}$$
(2.19)

Equation (2.19) provides the same results obtained for a circular toroid. This confirms that a circular toroid as well can be thought as the parallel combination of smaller concentric reluctances, because (2.19) assumed that there was not any interaction between the magnetic flux flowing in each slice.

However, as stated before, for a square toroid, the slices in Fig. 2.5, cannot be considered in parallel because of the corner effect; so the square toroid has to be transformed into an equivalent circular toroid that includes the corners effect [37], such that (2.19) is still applicable. Now the problem becomes finding the equivalent value of the external perimeter $P_B' < P_B$ of the equivalent round toroid with same internal perimeter P_A . This operation is valid given that the actual value of the *MPL* is closer to that one of the internal perimeter P_A and P_B , for the reasons shown before.

Following [37] [39] it entails that, when $W \rightarrow 0$, for a square magnetic circuit, the actual *MPL* is:

$$MPL = 4 \cdot (L_B - 2 \cdot W + 0.56 \cdot W) = P_B - 5.76 \cdot W = P_A + 2.24W$$
(2.20)

Now we can put $W/P_A = z$ and $P_B' - P_A = a \cdot W$, with a < 8 (according to (2.19)), so the normalized *MPL* can be written as:

$$\frac{MPL}{P_A} \cong \frac{a \cdot z}{\ln(1 + a \cdot z)} \tag{2.21}$$

With $a \approx 5.78$, (2.20) and (2.21) agree pretty well within few percent of difference till very high ratios between external and internal sides ($L_B / L_A < 5$, that corresponds to z < 0.5). However, at much bigger ratios, the effect of the non-uniformity of the flux cannot be neglected anymore and it is summed up with the corner effect. Thus, the effective magnetic path length for a square toroid, thus, can be written as [38]:

$$MPL_{eff} \cong \frac{5.78W}{\ln \frac{P_A + 5.78W}{P_A}}$$
(2.22)

So (2.22) includes the corner effect and the non-uniformity of the magnetic flux density. From (2.22) we find that the square toroid is equivalent, from a reluctance point of view, to a round toroid with internal radius $R_A = P_A / 2\pi$ and external radius R_B ' equal to [35]:

$$R_{B}' \cong \frac{5.78W}{2\pi} + R_{A} \cong 0.92W + R_{A}$$
. (2.23)

Figure 2.6 presents a comparison between the value of *MPL* obtained from (2.20) (blue circles), from (2.22) (red crosses) and from FEM (Finite Element Method, green triangles). As it can be seen, at very high ratios between external and internal sides, the contribution of the non-uniformity of magnetic flux becomes as important as the one due to the corner effect. However for practical cases (generally $L_B < 3L_A$) (2.20) and (2.22) agree pretty well since the corner effect is dominant in general is predominant.

It should be remarked that it makes sense to use the reluctance concept if the core magnetic permeability is very high and if the turns are tightly wound around the core, otherwise the Hopkinson's law and the magnetic Kirchhoff's laws [1] are not satisfied because of flux imbalance due to the flux leaking outside the core, because it is not



Figure 2.6. Comparison between equations and FEM [36]. (© 2015, IEEE).

entirely concentrated in the core and it has not a preferred path for flowing. The effect of the finite value of the permeability can be considered through the introduction of the coupling factor.

2.5 Losses

Magnetic components such as inductors as well as transformers are not ideal, since they suffer from losses. There are several types of losses. First of all there are the losses due to winding losses (DC and AC), and then there are the losses due to the core like the hysteresis losses and eddy current losses (both AC).

2.5.1 Winding losses - Resistance

The first source of losses in an inductor/transformer is given by the Joule heating of the conductor because of the finite value of the conductance. The electric resistance of a coil is given by the well-known formula:

$$R_{Coil} = \frac{l_{Coil}}{\sigma_{Coil} A_{coil}} = NR_{turn}$$
(2.24)

Equation (2.24) states that the higher number of turns, the higher the resistance. R_{turn} is the resistance of a single turn, and N is the number of turns wrapped around the core. Since the inductance value is proportional to the square number of the turns, apparently it seems that the number N can be increased with no limit, in order to increase also the (low-frequency) quality factor of the inductor $Q_L = 2\pi f_0 L/R_{DC}$. We will see later, through an example that this is not possible, because rather the number of turns, what is really important is the linear turn density n=dN/dx.

Average losses (W) due to the resistance are given by:

$$P_{R_{Coil}} = R_{Coil} \left(I_{DC}^2 + I_{eff}^2 \right),$$
 (2.25)

if we assume that the current flowing into the inductor is given by the following expression:

$$I_{TOT} = I_{DC} + \sqrt{2I_{eff}} \sin(2\pi f_0 t)$$
 (2.26)

2.5.2 Winding losses – skin effect

Another source of losses in the windings is given the so called skin-effect. The skin effect is a phenomenon that occurs at a certain critical frequency f_c , beyond which the current starts to flow significantly at the borders of the conductor, instead of flowing in a uniform way along the entire conductor cross section. In general the bigger the cross section, the lower will be f_c . Thus, increasing A_C would produce lower DC resistance, but at a certain frequency, the increased resistance because of the skin effect would be much higher, thus losing all the benefits due to a bigger cross section.

The conductor skin depth δ_W , defined as the depth below the surface of the conductor at which the current density has fallen to 1/e (about 37%). Its mathematical expression is given by [1]:

$$\delta_W = \sqrt{\frac{1}{\pi \sigma f_{op} \mu_0 \mu_r}} \tag{2.27}$$

 f_{op} is the frequency at which the inductor/transformer is working. Looking at (2.27) it is clear that the higher the conductivity of the material constituting the coil, the lower

the skin depth. If δ_W is higher than the material thickness, then the skin effect is pretty negligible. Furthermore (2.27) refers to a mono-dimensional skin effect, that is for example, like the one occurring in a metal stripe in which the width W is much bigger than the thickness t_W . In this case the shorter dimension is the one subject to the skin effect. A way instead to mathematically estimate the resistance of a flat conductor, in which the $W >> t_W$, subject to the skin depth is the Dowell equation [1] [25]:

$$R_{ac} \cong R_{dc} \left[1 + \frac{5N_l^2 - 1}{45} \left(\frac{t_W}{\delta_W} \right)^4 \right] , \qquad (2.28)$$

in which R_{dc} is the DC resistance and N_l is the number of parallel layers.

Figure 2.7 presents the numerical plots of (2.28) the normalized resistance for various conductors with $N_l = 1$, for thicknesses doubling from 10µm to 160µm. Thicker conductors, even if present a lower DC resistance, have a cross-over frequency much lower compared to thinner conductors. Furthermore, beyond this cross-over frequency, the AC resistance of thicker layers becomes higher than that of thinner ones. The choice of the right conductor thickness becomes extremely important in order to design properly magnetic components.

Figure 2.8 shows a picture of a FEM simulation of the normalized resistance of a cylindrical (copper) conductor of length 100μ m and diameter of the cross section 50 μ m. To cite an example, at 100MHz, the effective resistance has almost doubled because of the skin effect. **Figure 2.9** shows FEM simulation of the longitudinal current density at four different frequencies 1MHz, 10MHz, 100MHz and a 1GHz. It can be noted at 1GHz the current is flowing almost at the conductor border.



Figure 2.7: Numerical Simulation of normalized resistance of a metal stripe for $W >> t_W$, for various thicknesses.



Figure 2.8: FEM Simulation of the normalized resistance of a cylindrical conductor (copper) of length 100μm and diameter of the cross section of 50μm, versus frequency.



Figure 2.9. FEM simulation of skin effect on round-section conductor of 50µm of diameter.

2.5.3 Other sources of losses in the winding– Proximity effect

The proximity effect refers to the inducted current in a conductor due to the AC magnetic field produced by the flowing current in a parallel conductor close to the first conductor. The inducted current flows in the opposite way with respect to the conduction current, hence it is an effect pretty similar to the skin effect. **Figure 2.10** shows the ratio between the AC resistance and DC resistance due to skin depth F_P , the ratio between the AC resistance and DC resistance due to proximity effect F_R of only two parallel conductors, and the sum of them $F_S = F_P + F_R$, as a function of the ratio between the winding thickness and skin depth. Hence, the proximity effect can be as important as the skin effect. However, Dowell's equation (cfr. (2.28)), already takes into account the proximity effect.

2.5.4 Core losses: eddy current losses

Core losses can be divided in two types: hysteresis losses and eddy current losses. In general the last ones are the predominant in soft magnetic materials (materials with a small hysteretic behavior). The main factor of the eddy current losses is the resistivity ρ_C of the core, because in an ideal magnetic material, $\rho_C \rightarrow \infty$. The current flowing in the winding produces a magnetic field H according to Ampère's law, which in turn induces some currents (eddy currents) in the core, if ρ_C is finite. The higher the resistivity of the core, the better it is. This means that thicker cores will suffer more losses because of the presence of eddy currents.

For dielectric materials, in example, the Ampère-Maxwell law can be written in a differential form:

$$\nabla \times \mathbf{H} = j\omega\varepsilon \mathbf{E} + \sigma \mathbf{E} = j\omega\varepsilon \left(1 + \frac{\sigma}{j\omega\varepsilon}\right) \mathbf{E} = j\omega\varepsilon \left(1 - \frac{j\sigma}{\omega\varepsilon}\right) \mathbf{E} = j\omega\varepsilon_c \mathbf{E}$$

$$= j\omega\varepsilon \left(1 - \frac{j\sigma}{\omega\varepsilon}\right) \mathbf{E} = j\omega\varepsilon_c \mathbf{E}$$
(2.29)

This means that it is possible to introduce a complex dielectric constant ε_c given by:

$$\varepsilon_c = \varepsilon_0 \varepsilon_r \left(1 - j \frac{\sigma}{\omega \varepsilon_r} \right) \tag{2.30}$$



Figure 2.10: AC resistance to DC resistance ratio due to skin depth and proximity effect

The (negative) imaginary part of the dielectric constant will produce an exponentially decreasing solution for the Helmotz equation, thus representing the losses of the material. It is possible to demonstrate [1] that the magnetic permeability as well can be written as follows:

$$\mu_c(f) = \mu_r(f) - j\mu_{im}(f) \tag{2.31}$$

Hence, using (2.31) the impedance of an inductor becomes:

$$Z_{IND}(f) = j2\pi f \mu_c L_0 = j2\pi f \mu_r(f) L_0 + 2\pi f \mu_{im}(f) L_0 \qquad (2.32)$$

thus the imaginary part produces a real positive (frequency dependent) part in the impedance of the inductor, like a resistance, that will dissipate energy via Joule heating. L_0 is the value of the inductance normalized against the low-frequency magnetic relative permeability $\mu_{r0}=\text{Re}\{\mu_c(f=0)\}$.

Unfortunately, the Maxwell-Faraday equation of electromagnetic induction is not perfectly dual to the Ampère-Maxwell one, since there is not any term proportional to the magnetic field intensity and electric conductivity. However, it can be demonstrated [1] [40] that the imaginary part of the magnetic relative permeability for amorphous or nanocristalline materials can be written as follows:

$$\mu_{im}(f) = \mu_{r0}\left(\frac{\delta_{C}}{t_{C}}\right) \frac{\sinh\left(\frac{t_{C}}{\delta_{C}}\right) - \sin\left(\frac{t_{C}}{\delta_{C}}\right)}{\cosh\left(\frac{t_{c}}{\delta_{C}}\right) + \cos\left(\frac{t_{C}}{\delta_{C}}\right)}.$$
(2.33)

The dependence on the frequency is expressed by the fact that the core skin depth δ_C is dependent on the frequency (cfr. 2.27). The real part can be modelled instead as follows:

$$\mu_{r}(f) = \mu_{r0} \left(\frac{\delta_{c}}{t_{c}}\right) \frac{\sinh\left(\frac{t_{c}}{\delta_{c}}\right) + \sin\left(\frac{t_{c}}{\delta_{c}}\right)}{\cosh\left(\frac{t_{c}}{\delta_{c}}\right) + \cos\left(\frac{t_{c}}{\delta_{c}}\right)}$$
(2.34)

The imaginary part has a second order bandpass filter behavior whereas the real part has a first order low pass filter with cutoff frequencies equal to [40]:

$$f_T = \frac{4}{\pi \sigma t_c^2 \mu_0 \mu_r}, \qquad (2.35)$$

that is the frequency at which $\delta_C = t_C/2$.

As matter of fact, (2.34) can be approximated by [1]:

$$\mu_r(f) \cong \frac{\mu_{r0}}{\sqrt{1 + \left(\frac{f}{f_T}\right)^2}}$$
(2.36)

Figure 2.11 [40] shows the typical behavior of some nanocristalline or Co-based amorphous materials as a function of the frequency, as well as some ferrites.

Once the imaginary part of the magnetic relative permeability is known, the following step is to calculate the losses due to the skin depth in the core. For electric circuits we already know that these can be estimated through the formula $S_{electr} = \frac{1}{2}V \cdot I^* = \frac{1}{2}Z \cdot I \cdot I^* = \frac{1}{2}Z |I|^2$ For magnetic circuits we can do pretty the same thing, through (2.4) and (2.5), in fact we have that:

$$S_{magn} = \frac{1}{2} \Re \cdot \Phi_{M} \cdot \Phi_{M}^{*} = \frac{1}{2} \Re \cdot \left| \Phi_{M} \right|^{2}$$
(2.37)

But if we analyze (2.37), we find that

$$S_{magn} = \frac{1}{2} \frac{N^2}{L} \cdot \left(\frac{L}{N}\right)^2 \cdot |I|^2 = \frac{1}{2} L \cdot |I|^2$$
(2.38)

So (2.38) is the stored energy in the magnetic field. Hence to find the associated power, in phasorial terms, we have that:

$$P_{magn} = \frac{1}{2} j\omega \Re \left| \Phi_{\rm M} \right|^2 \tag{2.39}$$

The only way to have a real value of the power, is that the reluctance must be complex, that is to state that the magnetic permeability must be complex (or that must have an imaginary part). Hence the power lost in Joule heating, is given by:

$$P_{magn} = \frac{1}{2} \omega \operatorname{Im} \{\mathfrak{R}\} |\Phi_{M}|^{2}$$
(2.40)

But the complex reluctance can be written as:

$$\Re = \frac{l_C}{\mu_0 (\mu_r - j\mu_{im})A_C} = \frac{l_C (\mu_r + j\mu_{im})}{\mu_0 (\mu_r^2 + \mu_{im}^2)A_C} = \frac{l_C (\mu_r + j\mu_{im})}{\mu_0 |\mu_C|^2 A_C}$$
(2.41)

Hence substituting the imaginary part of (2.41) in (2.40) we have:

$$P_{diss} = \frac{1}{2} \frac{\omega \mu_{im} V_C}{\mu_0 |\mu_C|^2} |\mathbf{B}|^2$$
(2.42)

In $(2.42)V_C \cong A_C \cdot l_C$ is an approximation of the volume of the core. The losses per unit volume then are given by:

$$p_{diss} = \frac{1}{2} \frac{\omega \mu_{im}}{\mu_0 |\mu_c|^2} |\mathbf{B}|^2 = \frac{\pi f \mu_{im}}{\mu_0 |\mu_c|^2} |\mathbf{B}|^2$$
(2.43)

The value given in (2.43) is the same given in [40].



Figure 2.11: Behaviour of magnetic relative permeability of nanocristalline and amorphous materials as well as ferrites as a function of the working frequency [40] (© 1997 Elsevier Science).

Before, we have discussed about the benefits of introducing an air gap in an inductor/transformer, which acts like a "feedback" for the magnetic permeability. The main benefit was to make the effective permeability independent from all the causes that could make the real magnetic permeability to change. Another benefit is going to be showed. As for opamps, the introduction of a feedback in the system, makes the closed loop gain independent from the open loop gain, mainly the opamp's gain, which in turn is dependent from bias, temperature, process variations, etc., but increases the system bandwidth as well. This is what happens when an air-gap is introduced in a magnetic core: the bandwidth is increased as well at a cost of a lower effective permeability due to the demagnetization. In **Figure 2.12** it is shown, by a numerical simulation, how the permeability changes, for the Vitrovac 6025Z from Vacuumschmelze, when air gap length–core length ratio equal to 1/1000 is introduced. In **Figure 2.13** it is depicted the Matlab simulation of the normalized skin depth versus frequency in the no air gap case and air gap case of the Vitrovac.



Figure 2.12: Matlab plot of the effective permeability of Vitrovac 6025Z from Vacuumschmelze when air gap is introduced.



Figure 2.13: Matlab plot of the normalized skin depth with and without an air-gap in the Vitrovac.

Without air-gap the skin depth equals the material thickness t_c (25µm) at about 6kHz [41] [42]. With an air gap this frequency is shifted at around 600kHz.

2.5.5 Lowering the core losses - lamination

We have seen thicker cores produce higher losses, however the value of the low frequency inductance is also proportional to the core thickness. So a way to maintain thick cores, but at the same time reducing the losses is through *lamination*. Lamination (**Figure 2.14**) consists in dividing the core thickness in several *m* electrically isolated slices whose thickness is $t_C'=t_C/m$ In this case the core will have the same global equivalent cross section but with skin depth properties of a much thinner layer. This means L_0 remains the same and that in (2.33) and (2.34), t_C ' should be used instead of t_C . Furthemore, according to (2.35), f_T is shifted at much higher frequencies, since it is proportional to the square of the core slice thickness. Of course, combining both air gap and lamination, can give benefits from both techniques.

2.5.6 Core losses- Hysteresis

Hysteresis losses represent the power lost used to align the magnetic moments of the core material. The area enclosed by the hysteresis curve represents the work required to take the magnetic core through the whole hysteresis cycle [1]. **Figure 2.15** shows the difference between the inbound power and the released power. At each cycle some of the energy is kept and dissipated through heating because of the hysteresis loop. An ideal soft magnetic material should have a hysteresis loop as small as possible. However in a properly designed device, hysteresis losses are generally negligible compared to winding losses and eddy currents in the core.



Figure 2.14: Lamination of the core.



Figure 2.15: Hysteresis losses

2.6 Core saturation – minimum working frequency

Before we have talked about the core losses and about the cutoff frequency f_T beyond which the skin depth starts to be comparable to the core thickness and the losses start to be important. In order to have still acceptable quality factor, the maximum working frequency, as rule of thumb, should not exceed $f_T/4$. However both inductors and transformers as well, have a minimum working frequency in order to avoid the core saturation. Let's assume a turn subject to a sinusoidal time-varying magnetic flux density field at the frequency f_0 . The voltage of the electromotive force induced across the inductor terminals is given by:

$$\left|V_{m}\right| = \frac{d\lambda_{M}}{dt} = \frac{d\left(N \cdot B \cdot A_{C}\right)}{dt} \le N \cdot 2\pi f_{0} \cdot A_{C} \cdot B_{S} \cos\left(2\pi f_{0}t\right)$$
(2.44)

this means that the maximum voltage swing is limited by the saturation value B_S of the magnetic flux density field. Hence the amplitude of the voltage should not exceed the following value:

$$\left|V_{m}\right| \leq N \cdot 2\pi f_{0} \cdot A_{C} \cdot B_{S} \,. \tag{2.45}$$

Thus the minimum working frequency to avoid core saturation is given by:

$$f_{\min} < \frac{|V_m|}{N \cdot 2\pi \cdot A_C \cdot B_S} \tag{2.46}$$

2.7 Demagnetization

The relative magnetic permeability μ_r is referred only to materials in a closed form configuration such as in example a toroid. Let's assume a magnetic permeability discontinuity in the space like a thin magnetic sheet (**Figure 2.16**) in the air and let's assume an incident magnetic flux density H_{ext} on this sheet. Maxwell equations state that the component of magnetic flux density B normal to the discontinuity surface must be continuous, while the tangent components of magnetic field H (together with the *magnetization vector M*) must be continuous at the boundary surface. This means that inside a magnetized sample, the H field is oriented in the opposite way of the



Figure 2.16: Cross section of a thin magnetic film. Inside the sample the H field is opposed to the incident one.

vector B. Let's call this field H_d . Furthermore, due to the similarity of the B field and D field of a two electric charges placed close each other, it is possible to model two *magnetic charges* at each boundary [35].

The relation for closed magnetic circuits is:

$$B = \mu_0 (H + M) = \mu_0 (H + \chi_r H) = \mu_0 (1 + \chi_r) H = \mu_0 \mu_r H, \quad (2.47)$$

where $\chi_r = \mu_r - 1$ is the *magnetic susceptibility*. For open magnetic circuits, (2.47) is rewritten as:

$$B = \mu_0 \left(H + \chi_r \left(H - dM \right) \right) = \mu_0 \left(1 + \chi_r \right) H - \chi_r dM$$
(2.48)

where *d* is the *demagnetization factor*.

Furthermore, along the *z* axis we can write:

$$\dot{H}_{int} = \dot{H}_{ext} + \dot{H}_d \Longrightarrow H_{int} = H_{ext} - H_d \tag{2.49}$$

But, given that $H_{d,z}$ =- $d_z M_z$, then (2.49) is rewritten as:

$$H_{int,z} = H_{ext,z} - H_{d,z} = H_{ext,z} - d_z M_z$$
(2.50)

So it holds that:

$$\chi_r H_{int,z} = \chi_r H_{ext,z} - \chi_r d_z M_z = M_z$$
(2.51)

So at the end, we can write:

$$\frac{M_z}{H_{ext,z}} = \chi_{eff,z} = \frac{\chi_r}{1 + d_z \chi_r}$$
(2.52)

Equation (2.52) shows that in a particular direction there's an *effective susceptibility*, due to the fact that the magnetic circuit is not a closed form configuration. Furthermore (2.52) is similar to (2.7) for the effective relative permeability: in fact the ratio between the gap length and core length is a measure of the demagnetization of the material. In (2.52) if $d_z\chi_i >>1$ then $\chi_{eff,z} \approx 1/d_z$.

The strength of H_d ando so d, dipends on the geometry of the sample, i.e. for a thin sheet with sides length $L_x \approx L_y \gg L_z \Rightarrow d_x \approx d_y \ll d_z$, so in the z direction there is not any real amplification or concentration of the magnetic flux density.

Furthermore, for every magnetic material it holds that:

$$d_x + d_y + d_z = 1 (2.53)$$

If for simplicity we consider a magnetic sphere with $\mu_r \gg 1$, given that the sphere has not any preferential direction, it must be that $d_x = d_y = d_z = 1/3$. So if $d_z \chi_r \gg 1$ then χ_{eff} in any direction is equal to 3.

It is worth to note that $\chi_{eff} \neq \mu_{eff} - 1$, but if $\chi_r \gg 1$, then $\mu_{eff} - \chi_{eff} \cong \frac{1}{1 + d\chi_r}$, where d

refers to the particular direction of interest. Intuitively, the demagnetization field H_d , acts like the internal electric field of a parallel plates capacitor. If the magnetic layer is thicker, the distance between the positive and negative *magnetic charges* is higher and so the strength of H_d is lower. This is why the long solenoidal inductor formula is similar to the toroidal inductor. The longer the solenoid, the weaker the internal demagnetization field it is.

2.8 Snell Magnetic law

A consequence of the demagnetization is the reflection law of the magnetic flux density. Rays theory, states that an incident ray passing from a low refractive index medium (or dielectric permeability) to a higher refractive index medium, is divided in two other rays: the reflected one which follows the Descartes' law (angle formed with the perpendicular to the interface is the same of the incident ray), and the reflected one which follows the classic Snell's law:

$$n_1 \sin \theta_1 = n_2 \sin \theta_2 \Longrightarrow \frac{n_1}{n_2} = \frac{\sin \theta_2}{\sin \theta_1} , \qquad (2.54)$$

where θ_1 is the angle between the perpendicular to the incident surface and the incident vector, whereas θ_2 is the angle formed between the perpendicular to the incident surface and the refracted ray.

So given that $n_1 < n_2$, it holds that $\frac{\sin \theta_2}{\sin \theta_1} < 1$, and hence $\theta_2 < \theta_1$: the refracted ray is

closer to the perpendicular to the incident surface, with respect to the incident one.

Concerning the magnetic field, when an incident magnetic flux density passes from a low permeability medium μ_1 to a higher permeability medium μ_2 , we have that:

$$\mu_2 \tan \alpha = \mu_1 \tan \beta \Longrightarrow \frac{\tan \alpha}{\tan \beta} = \frac{\mu_1}{\mu_2}$$
(2.55)

where α is the angle between the perpendicular to the incident surface and the incident magnetic flux density and β is the angle formed between the perpendicular to the incident surface and the transmitted magnetic flux density.

So given that $\mu_1 < \mu_2$, it holds that $\frac{\tan \alpha}{\tan \beta} < 1$ and hence $\alpha < \beta$: the refracted ray is

farther from the perpendicular to the incident surface with respect to the incident one, that is to say that the magnetic flux density is bended and amplified along the boundary. So thin magnetic sheets, cannot be used to amplify a magnetic flus density perpendicular to the surface, but it can be used to make magnetic amplifier for integrated Hall sensors [43].

Figure 2.17 shows the duality between classic Snell's law and magnetic Snell's law.



Figure 2.17: Differences between classic Snell's law and Magnetic Snell's law.

2.9 Overview on Magnetic Transformers

Magnetic transformers are essentially two-port systems made by two inductors coupled via a magnetic core (**Figure 2.18**). The equivalent circuit of the ideal magnetic transformer is made by two dependent generators (**Figure 2.19**) depending on the particular representation. The factor *n* is the turn ratio, that is the ratio between the current turns at the secondary side N_2 and the current turns at the primary N_1 , that is $n = N_2/N_1$. In an ideal transformer, both primary and secondary inductors share the same magnetic flux Φ_M , because the reluctance \Re of the core is ideally zero. Furthermore, the surrounding environment has a "reluctance" $\Re_{ENV} < \infty$. This reluctance is parallel to that of the core, acting like a leakage.

The turn ratio *n* can be expressed by:

$$n = \frac{N_1}{N_2} = \frac{v_2}{v_1} = \frac{i_1}{i_2}$$
(2.56)

Equation (2.56) is demonstrated given that in a loss-less transformer, there is not any power loss, hence $p_1=i_1\cdot v_1=i_2\cdot v_2$. So if v_2 is *n* times v_1 , i_1 should be *n* times i_2 .



Figure 2.18. Magnetic transformer and its electric symbol.



Figure 2.19. Hybrid parameters representation of a magnetic transformer.

Since the magnetic transformer is a two-port system, we can write down the relations at the port number 1 and port number 2:

$$\lambda_{1} = \Phi_{11} + \Phi_{12} = L_{11}i_{1} + L_{12}i_{2}$$

$$\lambda_{2} = \Phi_{21} + \Phi_{22} = L_{21}i_{1} + L_{22}i_{2}$$
(2.57)

The quantity λ is the *magnetic flux linkage* that is the whole magnetic flux crossing the winding.

If we apply a voltage at the primary, this voltage will induce a magnetic flux inside the core, which in turn will produce a voltage at the secondary. The

electromotive force, according to the Maxwell equations, will produce another flux which be coupled with the primary.

Since $n\lambda_1 = \lambda_2$, because the primary and secondary winding share the same total magnetic flux, and $L_{22} = n^2 L_{11}$ because we are considering the loss-less case, it holds that:

$$n\lambda_{1} - \lambda_{2} = nL_{11}i_{1} + nL_{12}i_{2} - L_{21}i_{1} - L_{22}i_{2} = 0$$

$$\Rightarrow nL_{11}i_{1} + L_{12}i_{1} - L_{21}i_{1} - n^{2}L_{11}\frac{i_{1}}{n} = 0$$
(2.58)

That is:

$$nL_{11}i_{1} + L_{12}i_{1} - L_{21}i_{1} - nL_{11}i_{1} = 0$$

$$\Rightarrow i_{1}(L_{12} - L_{21}) = 0$$

$$\Leftrightarrow L_{12} = L_{21} = M$$
(2.59)

M is called *mutual inductance* and represents the amount of flux linkage produced in one of the two coils, when a unit current is applied to the other coil. Of course it holds that:

$$M = \frac{N_1 \Phi_{12}}{i_2} = \frac{N_2 \Phi_{21}}{i_1} = \frac{N_1 N_2 \mu_0 \mu_r A_C}{l_C} = \frac{N_1 N_2}{\Re}$$
(2.60)

 Φ_{ij} with i,j=[1,2] with $i\neq j$ in (2.60) is the flux produced in the *i* coil, when a current is applied in the *j* coil.

In an ideal transformer $F_{MM}=N_1i_1+N_2i_2=0$ [43], because for the core $\Re \rightarrow 0$. But in a real case, \Re is finite, because it keeps part of the applied F_{MM} (like a resistance keeps part of the voltage provided the generator), hence we have:

$$\Phi_{c} = \frac{N_{1}i_{1} + N_{2}i_{2}}{\Re}$$
(2.61)

Thus the electromotive force, due to the flux linkage related to the core, at the primary is given by:

$$e_{1} = N_{1} \frac{d\Phi_{C}}{dt} = \frac{N_{1}^{2}}{\Re} \frac{d\left(i_{1} + \frac{N_{2}}{N_{1}}i_{2}\right)}{dt}$$
(2.62)

The term $L_{m1}=N_1^2/\Re$ is called *magnetizing inductance* [44] referred to the primary side. Combining both (2.60) with the expression of the magnetizing inductance, we have:

$$M = \frac{N_1 N_2}{\Re_C} = \frac{N_1}{N_1} \frac{N_1 N_2}{\Re_C} = \frac{N_2}{N_1} L_{m_1}$$
(2.63)

As said before, in a real transformer, the surrounding environment acts like a leakage reluctance, which is in parallel to the one related to the magnetizing inductance. This is to say, that the *leakge (self) inductance* L_{σ} related to surrounding environment is placed in series with the magnetizing one. The leakage inductance comes from the fact that not the all the magnetic flux generated by the coil is contained inside the core, but *leaks* outside, because the surrounding environment has a kind of finite "reluctance".

The leakage inductance $L_{\sigma 1}$ at the primary is given by [43]:

$$L_{\sigma 1} = \frac{N_1 \Phi_{\sigma 1}}{i_1}, \qquad (2.64)$$

whereas the leakage inductance L_{σ^2} at the secondary side can be written as [43]:

$$L_{\sigma_2} = \frac{N_2 \Phi_{\sigma_2}}{i_2}.$$
(2.65)

The magnetic fluxes $\Phi_{\sigma 1}$ and $\Phi_{\sigma 2}$ are the leakage fluxes not linked to the core.

The self-inductance L_{11} of (2.57) seen at the primary port is given by:

$$L_{11} = L_{\sigma 1} + L_{m1} = L_{\sigma 1} + \frac{N_1}{N_2}M = L_{\sigma 1} + \frac{M}{n}$$
(2.66)

whilst the self-inductance L_{22} seen at the secondary port is given by:

$$L_{22} = L_{\sigma 2} + \left(\frac{N_2}{N_1}\right)^2 L_{m1} = L_{\sigma 2} + \left(\frac{N_2}{N_1}\right)^2 \frac{M}{n} = L_{\sigma 2} + nM$$
(2.67)

The two leakage inductances are evaluated through the formulas:

$$L_{\sigma_1} = (1 - k_1) L_{11}$$

$$L_{\sigma_2} = (1 - k_2) L_{22}$$
(2.68)

In which k_1 and k_2 are called *winding coupling factors* of the primary and secondary respectively. The parameters k_1 and k_2 represent the ratio between the flux linked to the core and that linked to the whole coil. In general these two factors are not equal because they depend on how the each winding is wrapped around the core. However we can write:

$$k_i = \frac{M}{L_{ii}} [i = 1, 2]$$
(2.69)

The average *coupling factor k* of the magnetic transformer is defined as:

$$k = \sqrt{k_1 k_2} = \frac{M}{\sqrt{L_{11} L_{22}}} \tag{2.70}$$

However for simplicity we can assume for both windings the same coupling factor k given by (2.70).

In an ideal magnetic transformer the *turn ratio* n and the *step-up ratio* n_{su} have the same value. In a real transformer the step-up ratio n_{su} is given by:

$$n_{su} = n \cdot k = \sqrt{\frac{L_{22}}{L_{11}}} \cdot k$$
 (2.71)

Equation (2.71) comes from the fact, that the magnetizing inductance referred to the primary and the primary leakage inductance make a voltage divider whose transfer function is equal to k.

Figure 2.20 presents the electromagnetic model of a real magnetic transformer. It is made up of an ideal magnetic transformer, plus the magnetizing inductance L_{m1} referred to the primary and the two leakage inductances $L_{\sigma1}$ and $L_{\sigma2}$.



Figure 2.20: Complete model of a magnetic transformer, in which all the inductors are considered lossy.

Concerning the losses in magnetic transformers, these are the same seen for the inductors.

2.10 Self-resonant frequency

Inductor and magnetic trasformers as well, have a self-resonant frequency, beyond which the inductance starts to behave like a capacitor of value C_p . This frequency is given by the following formula:

$$f_{sr} = \frac{1}{2\pi\sqrt{LC_p}} \tag{2.72}$$

This effect is due to the capacitive coupling of the various turns of the winding: at very high frequencies, the electric current prefers to jump from one turn to the next one in the form of displacement current instead of electric current. Generally, there is not any general expression for the estimation of the capacitance, which is strictly dependent on the geometry and also the way how the various turns are wrapped around the core. In [1] more details can be found.

2.11 Summary

This chapter has presented a review on the mathematical model of integrated inductors, together with the losses which can occur in a magnetic device. Particular emphasis has been given to the winding losses and core losses: as a matter of fact, some particular techniques (like LIGA processes) can allow the deposition of very thick metal layers. The working frequency of the device should always be kept in mind, and exploiting the maximum thicknesses allowed by the process, cannot necessarily be the best choice for the purpose, because of the skin effect in the winding and eddy currents in the core. Furthermore a new relation giving a more accurate estimation of the magnetic path length was presented. This allows evaluating more correctly the reluctance and hence the inductance value of an integrated square inductor, without the aid of time consuming FEM (Finite Element Methods) simulations.

Chapter 3

Optimization of square integrated planar core inductors

In the first chapter, various types of micro-inductors or transformers presented in literature were reviewed. In each work, the main task was to maximize the performance of the inductor given a certain footprint area. However, very few works show devices which have a square footprint area, which is the most suitable shape for on-chip integration. Furthermore, a lot of papers discuss about the possibility of using such inductors for power conversion without any type of investigation concerning the core saturation due to, for example, to the limited cross section of the core, as we have discussed in Chapter 2. In addition, the choice of some important parameters, like a certain number of current turns or width and thickness of the core is never justified analytically, In general, specific methodologies for the optimization of the shape of the magnetic device are still relatively missing in literature. This chapter describes an optimization technique for square integrated inductors and investigates the optimum design for on-chip square shaped toroidal inductors for a certain fixed footprint area. Although the upper part of current turns is assumed to be made by bond-wires, the presented analysis can be applied independently on the technique used to close the current turns, e.g. with flip-chip packaging techniques, as long as the linear turn density is kept constant and the same for all analyzed geometries.

Furthermore, a new serpentine shape is presented, which allows going beyond the limits of a normal square toroidal inductor.

3.1 The L/R_{DC} ratio

One of the main performance parameters to classify the quality of a micro-inductor is through the inductance-dc resistance ratio L/R_{DC} [2] [22]. The L/R_{DC} ratio of an infinitely long solenoid has a boundary limit that cannot be exceeded and has the following value [22]:

$$\frac{L}{R_{DC}} \le \frac{\mu_0 \cdot \mu_r \cdot t_C \cdot t_M}{2\rho_M}$$
(3.1)

where, t_C is the core thickness, whereas t_M and ρ_M are the metal thickness and metals electrical resistivity. Equation (3.1) assumes that the cross section of the metallization is rectangular, and that the thickness does not scale simultaneously with the width W_C , as it happens for example in flip-chip or lithographic processes. In addition, if performances comparable to those of commercial wire-wound inductors are desired (up to several tens $\mu H/\Omega$ [45]), from (3.1), it may seem that the maximization of inductance L or the low frequency quality factor can be obtained only by technology improvements, such as higher conductive metals and higher number of laminations (improving t_c , without affecting the AC performance), or greater permeability core materials. Furthermore, (3.1) indicates that the L/R_{DC} ratio does not depend on the whole number of turns. As a matter of fact, if a constant linear turn density n is considered, increasing the turns number N leads to an apparent increase of the L/R_{DC} ratio proportional to N, since the inductance value is proportional to N^2 whereas R_{DC} is proportional to N. Nevertheless, the inductance magnetic length l_c , which does not appear in (3.1) also affects L which is also proportional to N if the width and spacing of the turns are kept constant; so that actually L/R_{DC} is unchanged, but the footprint area has increased. On the other way, if the core footprint area is kept constant, the width of the turns should be lowered in order to increase N and the linear turn density should be increased, thus R_{DC} is N^2 times higher (N times due to a total length proportional to N, and an additional factor N because of the width scaling for keeping

the inductance total length to a constant value). Hence, L/R_{DC} can always experience a maximum or saturation, Figure 3.1 illustrates this concept.

Generally, on-chip planar-core MEMS inductors make use of rectangular or square toroidal geometries instead of solenoid geometries. In [23], open and closed core toroidal inductors are presented with the target to minimize the footprint area. In [20], an integrated DC/DC boost converter with on-chip micro-machined planar core inductor is presented, with rectangular toroidal core geometry. To the best of our knowledge, there is not any design flow or mathematical model that gives hints in order to optimize area usage for planar square-shaped toroidal core (SSTC) inductors (Figure 3.2). Furthermore, although infinite length solenoids and toroids share the same formula for the inductance value and parasitic DC resistance, (3.1) cannot be applied to toroids since they are different from long solenoids: an infinite length solenoid has its core length much higher than the core thickness and width, but in toroids, the core length and the available space for turns distribution depend on the core width: for instance in Figure 3.2, increasing the core width W_C up to $L_B/2$, brings to lower the available space for turns, thus decreasing L/R_{DC} . As a matter of fact, the turns distribution is allowed only along the internal perimeter (red line in Figure 3.2) of the toroid and not along the magnetic length (green line in Figure 3.2). On the other side, in toroids, decreasing W_C can bring to an increase of the number of turns, but L is also proportional to the core cross section, so intuitively there must be a balance between magnetic length and W_C , and hence an optimum value of W_C .

In addition, as it will be shown in the next sections, the SSTC geometry may be not the best geometrical configuration in terms of performances and area usage for inductors whose core can be patterned by photolithographic techniques or, more in general, with high resolution processes.

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Top views of fractions of a square toroid (racetrack core) inductor

Figure 3.1. Side view of a SSTC inductor. Left: reference. Centre: the number of turns is doubled whereas the metal width is kept constant Right: the number of turns is doubled and the width is halved to keep the footprint area constant. All the current turns are in series. If the footprint area is maintained constant, there is an increase of the inductance, but it is not possible to increase the quality factor at a certain frequency, by acting only on the windings shape [36]. (© 2015, IEEE)



Figure 3.2. Top view of an on-chip bond-wire SSTC inductor with N = 3 turns; blue lines are the onchip metal lines, and the yellow lines are the gold bonding wires. The green line is the mean magnetic path length, whereas the red line marks the internal perimeter [36]. (© 2015, IEEE)

3.2 Square Shaped Toroidal Core (SSTC)

Figure 3.2 shows a SSTC inductor. The external side of the core is L_B and the core footprint area is given by L_B^2 ; the core width is $W_C = (L_B - L_A)/2$ and thus the internal side can be written as $L_A = L_B - 2 \cdot W_C$.

The internal perimeter is $P_A=4\cdot L_A$, and the external perimeter is $P_B=4\cdot L_B$.

A constant turn density per unit length n_0 (turns/m) is considered in order to maximize the inductance value given that the footprint area is considered fixed.

In general, a way to find the magnetic path length is to simply make the arithmetic average between the internal and external perimeters. Nevertheless this is not correct since this operation assumes that the magnetic flux density is uniform along the core cross section. In addition, in a square toroid, the effect of the folded structure is summed up to magnetic non-uniformity and this is the predominant effect at small W_C as it has been shown in the previous chapter. In addition, in [37] [38] [39] there are simple mathematical expressions which allow to take into account the folding effect of the core and hence to calculate the corner reluctance. So, by following [37] [39] it descends that, when $W_C \rightarrow 0$, for a square magnetic circuit, the actual *MPL* is:

$$MPL = 4 \cdot (L_B - 2 \cdot W_C + 0.56 \cdot W_C) = = 4 \cdot (L_B - 1.44 \cdot W_C) = P_B - 5.76 \cdot W_C$$
(3.2)

Using (3.2), we can calculate the reluctance of the core:

$$\Re = \frac{MPL}{\mu_0 \mu_r A_C} \tag{3.3}$$

where $A_C = t_C W_C$ is the core cross section. In case of air-gap core inductors, the effective permeability should replace the relative magnetic permeability as seen in the previous chapter (cfr. also [1]). Nevertheless, given that the presented method is based on the optimization of the area usage, we can normalize against t_C every parameter that is dependent from the core thickness. Referring to **Figure 3.2**, if the turns are tightly wrapped, the inductance is given by:

$$L = \frac{N^2}{\Re} = \frac{\left(n_0 \cdot P_A\right)^2}{\Re} = \frac{n_0^2 \cdot \left(P_B - 8 \cdot W_C\right)^2}{\Re}$$
(3.4)
where $N = n_0 P_A$ is the whole number of current turns, that is proportional to the length of the internal perimeter P_A , which in turn depends on W_C , given that L_B is maintained constant. If N is low or μ_r is not adequately high, the way the turns are wrapped around the core can affect the inductance value: as a consequence the magnetic flux density leaks outside the core and starts to flow in the air surrounding each turn, thus a leakage inductance L_σ appears in series to that given by (3.4) as seen in the previous chapter. In this case finite elements method (FEM) simulators should be used to make a more precise evaluation of the coupling factor between the turns and in order to find a more accurate value of the inductance. Nevertheless, for comparison purposes, the same coupling factor for all the geometries will be considered.

From (3.3) and (3.4) it entails that L is directly proportional to A_C and N^2 , but inversely proportional to *MPL*. The upper limit of the inductance L, combining (3.2), (3.3) and (3.4) can be simply written as follows:

$$L < \frac{4n_0^2 \left(L_B - 2 \cdot W_C\right)^2 \cdot t_C \cdot W_C \cdot \mu_0 \cdot \mu_r}{\left(L_B - 1.44 \cdot W_C\right)}$$
(3.5)

From (3.5) it entails that $\partial L/\partial W_C = 0$ gives the highest value of inductance for a certain core footprint area L_B^2 of the device. $\partial L/\partial W_C$ is a cubic function of W_C , thus the optimum width W_{opt} , solving the previous mathematical expression, considering the solution $0 < W_C < L_B/2$, is given by:

$$W_{opt} = \frac{5}{24} L_B \cong 0.208 \cdot L_B$$
 (3.6)

Hence, by substituting (3.6) in (3.5), the maximum obtainable inductance for unit area is given by:

$$\frac{L_{\max}}{L_B^2} < 0.509 \cdot n_0^2 \cdot t_C \cdot \mu_r$$
(3.7)

where both $t_{\rm C}$ and L_B are expressed in meters whilst L_{max} in μ H. Equation (3.5) has the implicit constraint that $n_0 \cdot (L_B - 2 \cdot W_C)$ is an integer number. As seen in the previous chapter later, (3.5) to (3.7) apply only if $W_C < 0.4 L_B$, however from (3.6),

 $W_{opt} < 0.4 L_B$. In addition, R_{DC} , if upper and lower metals have the same structure, can be approximated by the following relation:

$$R_{DC} \approx 4 \left\lfloor n_0 \cdot \left(L_B - 2W_C \right) \right\rfloor \left[\rho_M \cdot \frac{2 \cdot \left(W_C + t_C + 2t_M \right)}{W_M \cdot t_M} + R_c \right], \qquad (3.8)$$

where $4 | n_0 \cdot (L_B - 2W_C) |$ is the integer number of turns, and W_M is the metal width; whilst the term $2 \cdot (W_C + t_C + 2 \cdot t_M)$ is the length of a single turn. More in general, for integrated devices, t_C and t_M are much smaller than W_C . For square-shaped toroidal inductors, the ratio between (3.5) and (3.8) gives a better evaluation of the L/R_{DC} ratio instead of (3.1). Furthermore, It is worth to remark that (3.8) takes into account the corner and constriction contact resistances R_c [46], due to the fact that the current density is not uniform in proximity of the contact surface, e.g. between the bond pad and the metal stripe, and it is not normal to this surface as shown in [46]. These effects lead to a small change of the total DC resistance of the winding, according to the "aspect ratio" t_l/t_W where t_l is the contact length and t_W is the thickness of the conductors (in case of two slabs with same current direction). Nevertheless, because of the high ratios between the wires length and thickness (hundreds of μm of length vs. few μ m of thickness) in such type of inductors, the intrinsic DC resistance given by each turn is predominant compared to the distorted resistance given by the contact (bond ball over the pad), and so the corner and constriction resistances can be neglected. This is also confirmed by a FEM simulation of a 1mm long, 200µm wide, and 4µm thick aluminium metal stripe connected to a 32µm gold bond wire, assumed to be semi-circular with diameter equal to the metal stripe length. A 100µm bond ball was also simulated. The resistance obtained by summing the resistance given by the two pieces is about 76m Ω , whereas the FEM simulation gives about 72m Ω . However the constriction effect can be much more evident if the ratio between the conductor length and thickness is decreased.

Figure 3.3 shows a plot of $L = L(W_C)$, for $t_C \mu_r = 0.1$ m, $L_B = 4$ mm, and $n_0 = 5 \cdot 10^3 \text{m}^{-1}$, which means a turn every 200µm. Unless otherwise noted, from now on the above values of L_B , n_0 , and $t_C \mu_r$ will be used for all the analyzed geometries in order to have a numerical reference for comparison purposes. In addition, given that the L/R_{DC} ratio is usually expressed in µH/Ω, the chosen values allow to have inductances in the range of µH and resistances in the range of Ω, hence providing a



Figure 3.3. *L* versus W_C (SSTC geometry) for a square footprint area of 16mm² and fixed linear turn density: the maximum is achieved for $W_{opt} = 0.83$ mm and $L = 20.2 \mu$ H [36]. (© 2015, IEEE).

more convenient and fast comparison. Furthermore, toroidal micro-inductors are more indicated for frequencies under 10MHz [2]: as a matter of fact below this frequency the side (or square root) of the footprint area is at least of 3-4mm [2]. Through (3.6) $W_{opt} = 0.83$ mm a corresponding to a maximum obtainable inductance value of 20.2µH. The number of current turns in optimum condition can be found through inversion of (4) (rounded towards the nearest lower integer multiple of 4). Given that once L and W_C are known, L_A is known too, in this case N = 46.4. This value should be rounded to to $N_{SSTC} = 44$, because it must be a multiple integer of 4. With $N = N_{SSTC} = 44$ the target value of the inductance is $L = 20.2 \cdot (44)^2 / (46.4)^2 = 18.16 \mu$ H. Although this is the maximum value for a SSTC inductor, it is not the maximum achievable for the given footprint area.

3.3 Serpentine Toroidal Core

In **Figure 3.4**, a serpentine toroidal core is illustrated. The mathematical relations between the parameters shown in the figure are:

$$A = \frac{L_B - (K/2 - 1) \cdot G}{(K/2)}$$
(3.9)

$$B = L_B - G - 2 \cdot W \tag{3.10}$$



Figure 3.4. Top view of the layout of a serpentine toroidal core: the green line represents the external perimeter, while the red line marks the internal perimeter. The footprint area is assumed to be square. The light grey part indicates the distribution of current turns. Blue squares are the bond pads, and yellow lines the gold bonding wires. The pads can be in a gig-gag configuration to allow a bigger pad pitch [36]. (© 2015, IEEE).

$$W = (A - G) / 2 \tag{3.11}$$

So *B* is dependent on *W*, which is in turn dependent on *A*, that is a function of the even integer number *K*, indicating the number of encountered parallel arms (along *y* direction) producing the serpentine geometry, whereas the parameter *G* is the distance (gap) between two consecutive parallel arms. To cite an example K = 2 corresponds to a SSTC (B = 0 and $A = L_B$). As usual, the inductance *L* is given by the following equation:

$$L < \frac{\left(\int_{0}^{P_{T}} n(x) dx\right)^{2}}{\Re} = \frac{\left\{n_{0} \cdot \left[P_{T} - 4 \cdot \left(K / 2 - 1\right) \cdot W\right]\right\}^{2}}{\Re}$$
(3.12)

where n(x) is the linear density of the current turns along the inductor length and P_{IT} is the internal perimeter (function of *A*, *B* and *W*). Referring to **Figure 3.4**, the function n(x) assumes the value n_0 in light grey areas, and 0 elsewhere. In our case we

have considered $n_0 = 5 \cdot 10^3 \text{m}^{-1}$, that is a turn every 200µm as stated before.

In order to find the magnetic path length to put in the reluctance expression in (3.12), the simplified relations given in [37] can be used, since the serpentine presents more or less the two limit cases presented in [37]. Looking at **Figure 3.4**, we can write down the *MPL* taking into account the corner reluctances:

$$MPL \cong (K-2) \cdot (B-W) + 3 \cdot (L_B - 2 \cdot W) + + (K-1) \cdot G + 2 \cdot (K-1) \cdot 0.47 \cdot W + 2 \cdot 0.56 \cdot W$$
(3.13)

In (3.13) the fourth and fifth terms of the sum represent the augmented lengths due to the corners effect with respect to the internal perimeter [37].

Figure 3.5 shows the plot of the obtained inductance *L* versus the core width *W*. The maximum obtained inductance is about 26.6µH, with W = 0.325mm. The number of current turns in optimum condition is $N_{SER} = 142$, in this case the subscript *SER* refers to *Serpentine*. The gap *G* was fixed to 200µm (hence G = 1/20 of L_B), that is a value that allows sufficient space to put two bond pads in zig-zag configuration. With the serpentine core, an increase of more than 35% of the maximum obtainable inductance value has been achieved, if compared to the SSTC inductor. In addition, there is a further degree of freedom, given that the parameter *G* has been fixed, but by changing the value of *G*, the value of the W_{opt} changes as well, and it can be demonstrated that lower values of the ratio G/L_B can give higher values of L_{max} for serpentine toroidal cores. Nevertheless, the boundary value of *G* is constrained by the particular technology used to pattern the core or the metal stripes, in addition the value of *G* must be sufficiently high in order to allow the turns closure.

3.4 Comparison of the two geometries

In this chapter, a comparison between the two geometries will be made, considering the maximum achievable inductance value for both (in optimum condition). In addition the comparison is made considering the same coupling factor between the coils and the magnetic core for both geometries, however in the serpentine configuration, the leakage flux between two parallel cores should be better evaluated in order to better assess the confinement of the field [47].



Figure 3.5. Inductance *L* versus core width *W* (serpentine toroidal geometry) in a core footprint area of 4mm×4mm, obtained with $G = 200 \mu$ m, $W_{opt} = 0.325$ mm and $L = 26.6 \mu$ H [36]. (© 2015, IEEE).

3.4.1 Peak saturation current

A useful parameter that allows to assess the quality of a magnetic core inductor is the peak saturation current I_m . For closed core inductors it is given by:

$$I_m = \frac{MPL \cdot B_s}{\mu_0 \mu_r N} \tag{3.14}$$

where B_S is the core saturation magnetic flux density.

In a serpentine core inductor, both the parameters MPL and N are higher compared to a SSTC inductor, but as N is more or less proportional to the mean magnetic path length (since n_0 is a constant), the two geometries have approximately the same saturation current.

For a SSTC inductor, normalizing (3.14) against B_s , and assuming for example $\mu_r = 10^4$ (typical permeability of permalloy [48], and recalling that $t_{C'}\mu_r = 0.1$ m, hence $t_C = 10\mu$ m and that $L_B = 4$ mm, it comes from (3.6) that $W_{opt} = 0.83$ mm, thus $L_A = L_B - 2 \cdot W_{opt} = 2.34$ mm, and from (3.2) that MPL = 11.2 mm, and $N = 44 = N_{SSTC}$, thus the normalized peak saturation current from (3.14) is $I_{m,SSTC} = 20.3$ mA/T.

For a serpentine core, with G = 0.2 mm, $W_{opt} = 0.325$ mm, $N = 142 = N_{SER}$, it comes from (3.13) that MPL = 31 mm, whereas the normalized peak saturation current

from (3.14) would be $I_{m,SER} = 17.4$ mA/T. From (3.14), if the same saturation current is wanted for both geometries, the serpentine core should have a number of turns equal to $N_{I,SER} = N_{SER} \cdot (I_{m,SER} / I_{m,SSTC}) = 142 \cdot (17.4 / 20.3) = 122$ and its inductance would be 19.7µH instead of 26.6µH, that is the same saturation current for both geometries, but an 8% higher inductance in the serpentine geometry with respect to the 18.16µH of the SSTC geometry. Thus $N = N_{I,SER} = 122$ is the value that can be used as a reference for comparison purposes if both geometries have to share the same saturation current.

3.4.2 *L*/*R*_{DC} ratio

In general, the quality of inductors is evaluated also with the normalized inductance with respect to the DC parasitic resistance, R_{DC} , as stated at the beginning of the chapter. Given that AC losses are not directly dependent on the geometry, as they are related to the skin depth (t_c and μ_r are assumed to be the same for both geometries), they are not taken into account. However, the relative permeability is a function of the operating frequency and it can be expressed as a complex quantity: the real part has a first order low-pass filter, with a cutoff frequency f_T , whereas the imaginary part has a second order band-pass filter, with resonance centered at f_T as seen in the previous chapter: the equivalent AC series resistance of the core R_{ACC} , that takes into account the core magnetic losses (but not hysteresis losses, that can be neglected for soft magnetic materials), is given by (2.32). The AC resistance of the winding is related to the dimension of the cross section with respect to the skin depth, but the cross section is assumed to be same in both geometries. Obviously, a higher inductance has a higher R_{ACC} , but as long as this resistance is much lower than the winding R_{DC} , it can be neglected. For further details, in [49] a good modelling of AC losses of the core is presented. Figure 3.6 shows the plot of normalized inductance against the R_{DC} from (3.8) for both geometries: for the serpentine core the ratio is higher, 7.8μ H/ Ω in the maximum achievable inductance condition, against the 6.9μ H/ Ω of the SSTC core. Considering the serpentine core with $N = N_{I,SER} = 122$, the L / R_{DC} ratio would have been 7.8 $\cdot (N_{I,SER} / N_{SER}) = 6.8 \mu H/\Omega$, that is approximately the same ratio of the SSTC inductor in optimum conditions and same core footprint area.

For the assessment of the DC parasitic resistance, the values shown in **Table 3.1** were considered.



Figure 3.6. Comparison of the ratio between inductance and DC resistance for both geometries. For the serpentine core the ratio is more than 10% higher at the point of maximum inductance [36]. (© 2015, IEEE).

TABLE 3.1

Parameter	Value		
Core Width W_C	W_{opt} (at $L_B = 4$ mm)		
Metal conductivity σ_M	3.25·10 ⁷ S/m		
Metal thickness t_M	3.2µm		
Metal Width W_M	180µm		
Metal stripe Length I_M	W_C		
Metal spacing s	20µm		
Bonding wire diameter	32µm		
Bonding wire conductivity σ_G	4.5·10 ⁷ S/m		
Bonding wire length l_{BW}	$\pi W_C / 2$		
Two bond wires in parallel for each metal stripe			

VALUES FOR R_{DC} EVALUATION

Table 3.1: Values used to calculate the R_{DC} in both square-shaped and serpentine toroidal core geometries [36]. (© 2015, IEEE).

3.4.3 Minimum work frequency

Another parameter which depends on the geometry is the minimum frequency required to prevent core saturation, as already seen in the previous chapter. It is worth to recall that this frequency must verify the following expression:

$$f_{\min} > \frac{V_{\max}}{2\pi \cdot N \cdot B_s \cdot A_c} \,. \tag{3.15}$$

The f_{min} is an important parameter for thick or non-laminated cores with very high permeability, given that as the amplitude of the induced voltage increases, this frequency increases too.

Besides, we recall also the cutoff frequency of the real part of the permeability, determined by the skin effect, is given by [40]:

$$f_T = \frac{4\rho_c}{\pi\mu_0\mu_r t_c^2} \tag{3.16}$$

where ρ_c is the core resistivity. At this frequency an inductor experiences poor quality factors, because at f_T the imaginary part is in the same order of magnitude of the real part. The maximum usable frequency corresponds as rule of thumb, approximately to $f_T/4$, since this is the frequency where the skin depth equals the material thickness. In (3.16) the permeability μ_r can be replaced by the effective permeability for magnetic cores with air-gaps.

To cite an example, considering a very high permeability material such the Vitrovac 6025 from Vacuumschmelze used in [30], we have $\mu_r \approx 10^5$, $t_c = 25 \mu m$, $\rho_c \approx 140 \mu \Omega \cdot cm$. Hence, from (3.16) we have that $f_T \approx 20$ kHz, so the maximum usable frequency is approximately 5-6kHz, as stated in [30] and it follows that $f_{min} \ll f_{H}$, otherwise the inductor is not usable for any application.

At 1V of amplitude, using Vitrovac 6025, whose saturation is $B_S \approx 0.5$ T, and assuming $N_{SER} = 142$ (serpentine inductor with footprint area $L_B^2 = 4 \text{ mm} \times 4 \text{ mm}$), (3.16) gives $f_{min, Vitrovac} \approx 276$ kHz, that is about fifty times greater than f_H . In this case laminations or air-gaps should be used in order to increase the maximum frequency, or the maximum amplitude of the induced voltage across the inductor terminals should be decreased in order to decrease f_{min} , thus limiting the field of application of the device.

Furthermore, if the inductor voltage is not sinusoidal, such as a square wave instead, as it is the case in power buck/boost switching DC/DC converters, the factor 2π in (3.16) can be substituted by 4 if the duty cycle is 50% [1]. In a buck or boost converter, for example, the maximum applicable voltage is related to the amplitude of input and output voltage. Hence, for f_{min} , what is extremely important is the $N \cdot A_C$ product.

Now the two geometries will be compared considering the minimum frequency.

For the serpentine core, normalizing (3.16) against B_S , with $L_B = 4$ mm, $N_{SER} = 142$, $W_C = 0.325$ mm, $t_C = 10\mu$ m (thus $\mu_r \approx 10^4$) and $V_{max} = 1$ V, we have $f_{min} = 348$ kHz·T; whereas for the SSTC we have $f_{min}=436$ kHz·T: another advantage of the serpentine geometry has been proved. If the serpentine core inductor with $N = N_{I,SER} = 122$ is assumed, in order to have the same saturation current of the SSTC inductor, the minimum frequency in this case is $f_{min} = 401$ kHz·T, which is still lower than that of the SSTC inductor.

3.4.4 Surface energy density

The last parameter that allows comparing inductors is the stored magnetic energy E_M normalized to the core footprint area $L_B^2[2]$:

$$e_{M} = \frac{E_{M}}{L_{R}^{2}} = \frac{L_{\max} \cdot I^{2}}{2L_{R}^{2}} . \qquad (3.17)$$

For us e_M represents the surface magnetic energy density in the maximum obtainable inductance condition.

For a SSTC geometry the value of e_M in correspondence of the maximum achievable inductance is 236pJ/mm² (calculated at L_{max} and $I = I_m$), whereas for the serpentine core $e_M \approx 251$ pJ/mm² (calculated at L_{max} and $I = I_m$), that is a 7% more. For the serpentine core, putting $N = 122 = N_{I,SER}$, does not change the value of (3.17), because it is not dependent of the number of turns. Substituting (3.4) and (3.13)-(3.14) in (3.17) we have:

$$e_{M} = \frac{A_{C}B_{S}^{2}MPL}{2\mu_{0}\mu_{r}L_{B}^{2}} = \frac{H_{S}^{2}}{2}\frac{t_{C}\cdot W_{C}\cdot MPL}{L_{B}^{2}} = \frac{H_{S}^{2}}{2}\cdot t_{C}\cdot \eta$$
(3.18)

where $H_S = B_S / (\mu_0 \mu_r)$ is the saturation magnetic field strength, and $\eta = W_C \cdot MPL/L_B^2$ is the fill factor, that is the percentage of footprint area covered by the magnetic core. Equations (3.17) and (3.18) show that the serpentine core inductor has a higher surface magnetic energy density compared to a SSTC inductor despite the higher inductance. As a matter of fact, in general, lower inductances can have higher magnetic energy density due to the lower permeability (*e.g.* air-gap core) or higher *MPL*. Thus (combining (3.14) and (3.17)), it is possible to demonstrate that the magnetic energy density is inversely proportional to magnetic relative permeability.

TABLE 3.2 COMPARISON OF GEOMETRIES FOR $L_B = 4$ mm, $G = 0.2$ mm, $B_S = 1$ T, $\mu_r = 10^4$ AND $t_C = 10$				
Parameter	Geometry			
	SSTC	Serpentine		
L _{MAX}	18.16µH	26.6µH	19.7µH	
I_m	20.3mA	17.4mA	20.3mA	
<i>f_{min} @</i> 1 V	436kHz	34 kHz	401kHz	
L_{MAX} / R_{DC}	6.9μΗ/Ω	7.8μΗ/Ω	6.8μΗ/Ω	
e_M	236pJ/mm ²	251pJ/mm ²	251pJ/mm ²	
W _c	0.83mm	0.32 mm	0.325mm	
N	48	142	122	

Table 3.2. Comparison of two geometries. Despite a loss in the saturation current, the global performances of the serpentine inductor are better than the inductor based on a square-shaped toroidal core. The enhancement of maximum inductance value is about 35% [36]. (© 2015, IEEE).

The serpentine core has the main benefit of a more efficient use of the core footprint area, because since the core has a lower width, the magnetic flux density is "forced" to be more uniform along the entire cross section. On the contrary, in classical square-shaped toroids, the magnetic flux density is concentrated near the internal perimeter, whereas the external boundary of the core gives less contribution for the flowing of the magnetic flux density, as seen in the previous chapter. **Table 3.2** summarizes all the performances of both geometries.

As stated before, in [22] the parameter L/R_{DC} is used to compare the performances of the presented inductor with respect to prior works. By assuming the following values, core footprint area $L_B^2 = 5.6$ mm × 5.6mm (as in [22]), core width $W_C \approx 2.05$ mm, core thickness $t_C \approx 16$ µm, metal conductivity $\sigma_M = 5.8 \cdot 10^7$ S/m, metal thickness $t_M = 20$ µm, metal width $W_M \approx 450$ µm, metal stripe length $l_M = W_C$, metal spacing $s \approx 20$ µm, number of turns N = 12, relative permeability $\mu_r = 900$, then the total inductance of a SSTC inductor, using (3.3) and (3.4) is about 503nH, whereas the inductor DC series resistance, calculated from (3.8) is approximately 95m Ω , that are approximately the values given in [22]. Using (3.6), (3.7) and (3.8) it is possible to find that $W_{opt} \approx 1.165$ mm and $L_{max} \approx 1.05$ µH, whereas $R_{DC} \approx 144$ m Ω , and the total number of turns is $N_{SSTC} = 28$. We have an increase of +110% of the inductance despite an increase of +50% of the R_{DC} . Thus the inductance can be increased,



Figure 3.7 Values of estimated inductance, DC resistance and L / R_{DC} ratio for the inductor of [10] with a serpentine core geometry design [36]. (© 2015, IEEE).

showing also an increased L / R_{DC} ratio even without making any modifications to the original SSTC geometry.

Figure 3.7 presents the plots of inductance, DC resistance and L/R_{DC} with the serpentine core design applied to a same core footprint area $L_B^2 = 5.6$ mm × 5.6mm and gap $G = 0.2\mu$ m, with all other parameters being equal to the last SSTC case.

As shown in **Figure 3.7**, the maximum inductance obtained at $W_{opt} = 0.525$ mm, is $L = 1.46\mu$ H, $R_{DC} \approx 144$ m Ω , and $L/R_{DC} \approx 10\mu$ H/ Ω (at L_{MAX}) against the 5.25 μ H/ Ω (0.5 μ H / 95m Ω) obtained in [22], thus an increase of more than 80% of the ratio (+45% increase in the inductance value with respect to the SSTC optimum condition). Finally, the total number of turns is $N_{SER} = 81$. From (3.17), it is possible to note that the energy capability of the inductor increases, due to a more efficient use of the footprint area.

Furthermore, it is also worth making an addition consideration about the comparison between the two geometries: the serpentine shape can be the best geometrical configuration for core materials showing uniaxial anisotropy, given that in this case the magnetic flux density should be perpendicular to the hard-axis (or parallel to easy axis), for high inductance values, or perpendicular to the easy axis

(parallel to hard axis) to limit the core losses (as it was done in [41]), thus the presented serpentine geometry allows a square footprint area (which is the shape most suitable for on-chip integration), whilst the turns are mostly located along the direction of preference; while in anisotropic SSTC, the turns should be located in both axis.

3.5 Summary

This chapter has presented a way to maximize and optimize the inductance value once the footprint area has been fixed. The optimization of the square inductor originated from simple considerations on the magnetic flux density behavior inside a closed magnetic core. Furthermore, a new example of geometry, the serpentine core, was introduced: spreading the core all over the surface, with a narrower width, allows to have a more uniform magnetic flux density inside, hence there's less "waste" of used area, since every portion of the core contributes in the same way for the global reluctance value, compared to the classic square shape where the external borders give less contribution to the flowing of the internal magnetic field. The serpentine geometry can be used in processes where high resolution techniques are available.

Chapter 4

Piezoelectric materials and applications

In the previous chapters we have analysed the magnetic materials, properties and applications mostly focusing on the perspective of integration for ultra-low power purposes. In addition to magnetic materials, same functions can be achieved through the help of piezoelectric materials, which in perspective can be highly interesting since a lot of piezoelectric materials can be processed via standard IC techniques. In addition, piezoelectric materials have quality factors (Q) much higher than magnetic materials: this means that the piezoelectric transduction is less lossy compared to the electromagnetic transduction. Thus piezoelectric materials are more suitable in the field of application of energy harvesting as well as ultra-low power or autonomous systems. However, as previously done for magnetic materials, an overview on the piezoelectric effect, materials and applications is needed in order to better understand and predict the behaviour of systems in which they are used.

4.1 **Properties of piezoelectric materials**

The piezoelectric effect is a physical property existing in many materials in nature. The word is composed by two parts; *piezo*, which comes from the Greek word for *pressure*, and *electric* from electricity. Thus the name suggests that a piezoelectric material can provide *electric charge* if subject to a *mechanical pressure*. This is known as the *direct piezoelectric effect*. On the other side, if a voltage is applied to the same material a change in the mechanical dimensions of the sample can be obtained. This is known as the *indirect piezoelectric effect* [50].

Several ceramic materials have been described as presenting a piezoelectric effect. Among these we can find lead-zirconate-titanate (PZT), lead-titanate (PbTiO₂), lead-zirconate (PbZrO₃), barium-titanate (BaTiO₃). Nevertheless, these materials are not really piezoelectric but rather present a *polarized electrostrictive* effect (a quadratic dependence of the strain from the electric field [51]). Other materials like the zinc oxide (ZnO) or Aluminum-nitride (AlN) are truly piezoelectric. The main difference between piezoelectric materials and electrostrictive materials, is that in the formers, the sign of the strain changes according to the polarity of the applied voltage, whereas this does not happen in electrostrictive materials [51]. Furthermore, a material must be formed as a single crystal to be piezoelectric, whereas ceramic materials are made up by a multi crystalline structure composed of a great numbers of randomly orientated crystal grains. The random orientation of the grains results in a net cancellation of the effect. As a consequence, ceramic materials must be polarized to align a majority of the individual grain effects (known as *poling*), whereas this is not necessary on truly piezoelectric materials. However, the term piezoelectric is nowadays used to indicate both materials exhibiting a polarized electrostrictive effect and piezoelectric effect in most works in literature [50].

4.2 Electric and mechanical properties of materials

Piezoelectric materials are essentially dielectric materials with piezoelectric properties. In order to better understand the properties and behaviour of such materials, it is worth to recall some basic relations regarding dielectric materials. The capacitance (F) of two parallel metallic plates capacitor can be expressed as:

$$C_d = \frac{A_0 \varepsilon_0 \varepsilon_r}{x_0} = \frac{A_0 \varepsilon}{x_0}$$
(4.1)

where $\varepsilon_0=8.854\cdot 10^{-12}$ F/m, is the vacuum *dielectric permeability*, ε_r is the relative dielectric permeability of the medium, A_0 is the surface of the metallic plates, and x_0 is the distance between the plates. Roughly $x_0 \ll A^{1/2}$, otherwise the fringing flux determines a value of the capacitance slightly different from that given by (4.1). Equation (4.1) resembles the equation of the permeance of a magnetic core, showing complete duality between dielectric and magnetic materials.

The charge Q(C) placed on one of the two parallel plates is expressed as:

$$Q = C_d \cdot V = \frac{A_0 \varepsilon V}{x_0} \tag{4.2}$$

where V is the potential difference between the two plates. The quantity V/x_0 is the electric field E (V/m) between the two plates and the quantity $\varepsilon V/x_0$ is the *electric displacement field D*. Like the magnetic flux density $B=\mu H$, the relation $D=\varepsilon E$, gives a hint of the amplification of the electric field inside the material due to the relative dielectric constant. Hence (4.2) can be rewritten as:

$$Q = A_0 \cdot D \tag{4.3}$$

The previous presented relations can be applied only to all isotropic dielectric materials. "Piezoelectric" ceramic materials are isotropic only in the non-polarized state, but they become anisotropic in the polarized (or poled) state. This entails that a necessary condition for a material, in order to present a piezoelectric effect, is that it must be anisotropic. In this kind of materials, the relation linking the electric field *E* and electric displacement *D* is represented by a 3×3 matrix. This is a direct consequence of the reliance of the dielectric constant upon the orientation of the plates of the capacitor to the poled axes. In this case, the relation between *E* and *D* is represented by:

$$D_{1} = \varepsilon_{11}E_{1} + \varepsilon_{12}E_{2} + \varepsilon_{13}E_{3}$$

$$D_{2} = \varepsilon_{21}E_{1} + \varepsilon_{22}E_{2} + \varepsilon_{23}E_{3}$$

$$D_{3} = \varepsilon_{31}E_{1} + \varepsilon_{32}E_{2} + \varepsilon_{33}E_{3}$$
(4.4)

For most of ceramic materials, like PZT, only ε_{11} , ε_{22} and ε_{33} are non-zero. Furthermore it holds that $\varepsilon_{11} = \varepsilon_{22}$.

Axis number	Axis function
1	x
2	V
3	z (poling)
4	shear around x
5	shear around <i>y</i>
6	shear around z
7	radial vibration

Table 4.1 Convention between axis number and function.

Concerning piezoelectric materials, the most used convention in literature (and also by FEM simulators by default) is that the z axis is the poled one. The used convention in literature is shown in **Table 4.1**.

In addition to electric properties, it is also worth reviewing the elastic properties of the materials. All materials, within their linear boundaries, follow the Hooke's law or fundamental law of elasticity. Hooke's law, states that the strain (or relative elongation) $\lambda = \Delta L/L_0$ is proportional to the stress Σ (applied force over the surface):

$$\lambda_i = Y_{ij} \cdot \Sigma_j \tag{4.5}$$

where Y_{ij} is the so called *Young modulus*. Equation (4.5) is assumed for anisotropic materials. The Young modulus and *stiffness constant* k_E , in the simplest case of a straight beam, with one side fixed and the other subject to a uniform stress, are linked by the following relation:

$$k_{E} = \frac{A_{0} \cdot Y}{L_{0}} = \frac{1}{C_{E}}$$
(4.5)

where A_0 and L_0 are the cross section and length at rest of the sample. By looking at (4.5) it can be noted that k_E resembles a dielectric capacitance or magnetic permeance if the Young modulus is modelled as a dielectric constant or magnetic permeability constant. Be γ the material density, then the mass m (kg) can be represented by the following equation:

$$m = \gamma \left(A_0 \cdot L_0 \cdot W_0 \right), \tag{4.6}$$

As stated before, piezoelectric devices, are essentially electromechanical vibrators, this implies that some of the parameters of their lumped electric circuit come from some mechanical properties. It is worth to review the electromechanical analogies

Ele	ectrical unit	Mec	chanical unit
V	voltage (V)	F	Force (N)
Ι	Current (A)	v	Velocity (m/s)
Q	Charge (C)	S	Displacement (m)
C_{El}	Capacitance (F)	C_E	Compliance (m/N)
L	Inductance (H)	т	Mass (kg)
R	Resistance (Ω)	υ	Viscosity (N·s/m)
Z_E	Impedance (Ω)	Z_M	Mech. impedance
	V=LdI/dt		v = ds/dt
	I=dQ/dt	F=Mdv/dt	

 Table 4.2 Analogies between electric quantities and mechanical quantities.

shown in **Table 4.2**. It can be understood that a generic mechanical linear system can be represented by its equivalent electric circuit through the proper substitution of the mechanical quantities with the respective electrical one, given that the structure of the differential linear equations describing both systems are the same [52].

As stated before, in order to produce anisotropy, which is a net alignment of the ferroelectric domains causing thus piezoelectric (or electrostrictive) effect in certain ceramic materials, a polarization is strictly required. The application of this voltage is called *poling*. This technique consists of applying a dc voltage across the material of several hundreds of Volts, thus causing a partial alignment of the ferroelectric domains. The density of the aligned ferroelectric domains depends on the value of this voltage, on the temperature and on the time spent for the poling. During this process, the material increases along the dimension perpendicular to poling electrodes, whilst it decreases in the dimension parallel to the poling electrodes. Figure 4.1 shows some modes of expansion of a piezoelectric material. Generally, a post-poling voltage applied to the electrodes with the same polarity as the initial poling voltage, will provide an additional increase along the dimensions perpendicular to the face of the electrodes, whereas the dimensions parallel to the electrodes will experience a further decrease. On the contrary, if the polarity is reversed, the sample will decrease in the dimension perpendicular to the original poling voltage, whilst the dimensions parallel to the electrodes, will increase. The shear (cfr. Figure 4.1) in piezoelectric materials is obtained if, after the material has been poled, if the former couple of electrodes is removed, and an electric field perpendicular to the poling direction is applied to the sample. Dually, physically applying a shear stress in the sample induces a polarization charge on the new couple of electrodes.



Figure 4.1 Modes of expansions according to the relative orientation between the poling voltage and the applied voltage [50] (© EETIMES 2000).

The dual piezoelectric effect can be obtained by applying a stress Σ in a particular direction: a compressive stress applied parallel to the original poling direction (that is perpendicular to the face of the electrodes) or a tensile stress parallel to electrodes will produce a voltage on the couple of electrodes which has the same polarity as the original poling voltage) or a tensile force parallel to the poling direction results in a voltage generated on the electrodes which has the same polarity as the original poling voltage [50]. Dually, a tensile force that is applied perpendicular to the original poling electrodes or a compressive force applied parallel to the electrodes provides a voltage of opposite polarity with respect to the original poling voltage.

4.3 **Piezoelectric Relations**

As stated before, for dielectric piezoelectric materials, if a stress is applied to the sample, a polarization charge appears on the electrodes (direct piezoelectric effect). On the other side, an application of a voltage, will produce a strain in the sample. Strain and stress are linked by the Hooke's law (inverse piezoelectric effect). Then the piezoelectric equation is defined as:

$$D_i = d_{ij} \Sigma_j, \text{ or }$$
(4.7)

$$\lambda_i = d_{ij} E_j \tag{4.8}$$

where d_{ij} (m/V or C/N) is the *piezoelectric modulus*, that is the ratio between the resulting charge density and the applied stress or the resulting strain and the applied electric field. Combining (4.7) and (4.8) we have:

$$D_i = \frac{\lambda_i}{E_j} \Sigma_j \tag{4.9}$$

Combining, in turn, (4.4) with (4.7) it follows that:

$$\varepsilon_{ij}E_j = d_{ij}\Sigma_j \Longrightarrow E_j = \frac{d_{ij}}{\varepsilon_{ij}}\Sigma_j = g_{ij}\Sigma_j.$$
(4.10)

Equation (4.10) links the generated electric field in a certain direction and the applied stress in the same direction. The parameter g_{ij} (m²/C) is known as *piezoelectric constant*. In order to exploit the correspondence reported in **Table 4.2**, the relation between the voltage and the force is mandatory. From (4.10), referring to the straight beam (**Figure 4.2**), which oscillates at the 33 mode (that is force applied along the *z* direction, and electric field parallel to the *z* axis)

$$\frac{V_j}{L_0} = \frac{d_{ij}}{\varepsilon_{ij}} \frac{F_j}{A_0} \Longrightarrow V_3 = g_{33} \frac{L_0}{A_0} F_3$$

$$(4.11)$$

Conversely, the relation between force and voltage, is obtained through inversion of (4.11):

$$\frac{V_j}{L_0} = \frac{d_{ij}}{\varepsilon_{ij}} \frac{F_j}{A_0} \Longrightarrow \frac{F_3}{V_3} = \frac{A_0}{g_{33}L_0} = N_1$$
(4.12)

A generic piezoelectric actuator can be represented by a dielectric capacitance with a parallel parasitic resistance (see (2.29) and (2.30)) due to the finite electric conductivity σ_d of the dielectric, an ideal transformer 1: N_1 , with N_1 representing the conversion ratio between the resulting force and voltage (cfr. (4.12)), a spring of compliance C_M and a mass m, plus a mechanical resistance due to the "damping" of the material, that is a friction force proportional to the velocity. Due to the correspondence in **Table 4.2**, it is possible to replace the compliance with a capacitor C_M , the mass with an inductance L_M , and the damping with an electrical resistance R_M . (cfr. **Figure 4.3**). The electric capacitance C_{IN} can be represented by (4.1), whereas the dielectric parasitic resistance is:



Figure 4.2: Straight beam subject with one fixed side and subject to a uniform stress Σ .



Figure 4.3: Electro-mechanical model of a simple piezoelectric actuator.

$$R_{IN} = \frac{1}{\sigma_d} \frac{L_0}{W_0 \cdot T_0}$$
(4.13)

Obviously, a *piezoelectric transducer* (which converts a stress into a charge or electric signal), can be obtained by simply switching *A port* with *B port*.

In order to simplify the model of **Figure 4.3**, it is possible, exploiting the properties of transformers, to carry L_M , C_M and R_M at the left side of the transformer, and getting rid of it. It entails that $L_M = L_M '/N_1^2$, $R_M = R_M '/N_1^2$ and $C_M = C_M \cdot N_1^2$.

It is worth noting that the simplified model of **Figure 4.3** is valid only in a very small neighbourhood of the mechanical resonance of the system given by:

$$f_{s} = \frac{1}{2\pi\sqrt{L_{M}C_{M}}} = \frac{1}{2\pi\sqrt{\gamma(W_{0}T_{0}L_{0})\frac{L_{0}}{W_{0}T_{0}Y_{33}}}} = \frac{1}{2\pi L_{0}} \sqrt{\frac{Y_{33}}{\gamma}} = \frac{1}{2\pi L_{0}} \frac{v_{s}}{L_{0}}$$
(4.14)

where v_s in (4.14) is the speed of sound inside the material considered. In general, the equations are much more complex, especially for "13" modes or torsional modes. Furthermore the actual model presents rather distributed acoustic impedances which depend on the propagation constant of the acoustic wave, but around the resonance, a lumped model like the one in **Figure 4.3** can be adopted. In [53] [54] [55] a more detailed dissertation of the distributed model can be found.

4.4 Piezoelectric Transformers

Piezoelectric transformers are devices which are obtained by coupling a piezoelectric actuator together with a piezoelectric transducer. For simplicity, we can consider an actuator and a transducer working in the "33" mode (cfr. Figure 4.4). Let's assume that in the the primary side (actuator) there are several interdigitated electrodes, with a number *n* of interdigitated layers, which are electrically in parallel. The length of primary and secondary side are related by the relation $L_1+L_2=L_0$. W_0 and T_0 are the width and depth respectively. The complete electromechanical model of the system, around a resonance frequency is depicted in Figure 4.5. N_M is the mechanical coupling between the primary side and secondary side, in general $N_M\approx 1$ for "33" mode, given that the applied and generated stresses have the same directions. The parameters C_{M1} , L_{M1} , R_{M1} are given by the following expression:

$$C_{M1} = \frac{L_1}{W_0 T_0} \frac{1}{Y_{33}}$$
(4.15)

$$L_{M1} = \gamma \left(L_1 W_0 T_0 \right) \tag{4.16}$$

$$R_{M1} = \frac{2\pi f_s L_M}{Q_M} = \frac{\frac{1}{L_1} \sqrt{\frac{Y_{33}}{\gamma} \gamma \left(L_1 W_0 T_0 \right)}}{Q_M} = \frac{\sqrt{Y_{33} \gamma} \left(W_0 T_0 \right)}{Q_M}$$
(4.17)



Figure 4.4: piezoelectric transformer working in the "33" mode. At the primary there are *n* interdigitated electrodes.



Figure 4.5: Complete electromechanical model of a piezoelectric transformer. N_M is mechanical coupling between primary and secondary.

where Q_M is the mechanical quality factor of the material. The electromechanical parameters at secondary side C_{M2} , L_{M2} , R_{M2} are given by the expression:

$$C_{M2} = \frac{L_2}{W_0 T_0} \frac{1}{Y_{33}} \tag{4.18}$$

_

$$L_{M2} = \gamma \left(L_2 W_0 T_0 \right) \tag{4.19}$$

$$R_{M2} = \frac{\frac{1}{L_2} \sqrt{\frac{Y_{33}}{\gamma} \gamma \left(L_2 W_0 T_0 \right)}}{Q_M} = \frac{\sqrt{Y_{33} \gamma} \left(W_0 T_0 \right)}{Q_M}$$
(4.20)

The total mechanical capacitance C'_{M} , total mechanical inductance L'_{M} and total mechanical resistance R'_{M} are given by:

$$C'_{M} = \frac{1}{\frac{1}{C_{M1}} + \frac{1}{N_{M}^{2}C_{M2}}} \cong W_{0}T_{0}\frac{Y_{33}(L_{1} + L_{2})}{L_{1}L_{2}} = W_{0}T_{0}L_{0}\frac{Y_{33}}{L_{1}L_{2}}$$
(4.21)

$$L'_{M} = L_{M1} + \frac{L_{M2}}{N_{M}^{2}} \cong \gamma \left(L_{1} W_{0} T_{0} \right) + \gamma \left(L_{2} W_{0} T_{0} \right) = \gamma \left(L_{0} W_{0} T_{0} \right)$$
(4.22)

$$R'_{M} = R_{M1} + \frac{R_{M2}}{N_{M}^{2}} \cong 2 \frac{\sqrt{Y_{33}\gamma} \left(W_{0}T_{0}\right)}{Q_{M}}$$
(4.23)

The equivalent electromechanical circuit, after this transformation is depicted in Figure 4.6a.

The parameters N_1 and N_2 are respectively given by:

$$N_1 = \frac{nW_0 T_0}{g_{33}L_1} \tag{4.24}$$

$$N_2 = \frac{W_0 T_0}{g_{33} L_2}.$$
(4.25)

In (4.24) the length of the generated field is L_1/n .

The input capacitance C_{IN} and input resistance R_{IN} are given by the following expressions:

$$C_{IN} = n \frac{W_0 T_0 \varepsilon_0 \varepsilon_{33}}{L_1 / n} = n^2 \frac{W_0 T_0 \varepsilon_0 \varepsilon_{33}}{L_1}$$
(4.26)

$$R_{IN} = \frac{1}{n} \frac{L_1 / n}{\sigma_d W_0 \cdot T_0} = \frac{1}{n^2} \frac{L_1}{\sigma_d W_0 \cdot T_0}$$
(4.27)

Instead, the output capacitance C_{OUT} and input resistance R_{OUT} are given by the following expressions:

$$C_{OUT} = \frac{W_0 T_0 \varepsilon_0 \varepsilon_{33}}{L_2}$$
(4.26)



Figure 4.6: Electromechanical circuit of the piezoelectric transformer, after each transformation.

$$R_{OUT} = \frac{L_2}{\sigma_d W_0 \cdot T_0} \tag{4.27}$$

The parameters C'_M , L'_M and R'_M can be brought at the left port of the ideal transformer 1: N_1 , thus obtaining the following relations (cfr. **Figure 4.6b**):

$$C_{M} = C'_{M} N_{1}^{2} = W_{0}T_{0}L_{0} \frac{Y_{33}}{L_{1}L_{2}} \left(\frac{nW_{0}T_{0}}{g_{33}L_{1}}\right)^{2}$$
(4.28)

$$L_{M} = L'_{M} N_{1}^{2} = \left(\frac{nW_{0}T_{0}}{g_{33}L_{1}}\right)^{2} \gamma \left(L_{0}W_{0}T_{0}\right)$$
(4.29)

$$R_{M} = R'_{M} N_{1}^{2} = \left(\frac{nW_{0}T_{0}}{g_{33}L_{1}}\right)^{2} \frac{2\sqrt{Y_{33}\gamma}(W_{0}T_{0})}{Q_{M}}$$
(4.30)

At the end the turn ratio N, of the transformer can be written as:

$$N = N_M \frac{N_1}{N_2}$$
(4.31)

Thus the final circuit of the piezoelectric transformer is depicted in **Figure 4.6c**. In this case the vibrational node, of the fundamental node is placed in the mechanical centre of the structure.

4.5 Other applications of piezoelectric materials

Piezoelectric materials are used not only for the fabrication of transformers, but also for sensors and transducers. To cite an example they can be used in place of thermal heaters in printers. As a matter of fact, they can be placed in the chamber filled of ink, behind the nozzle: when the controlling voltage is applied, the piezoelectric material changes shape, generating a pressure which forces a droplet of ink from the nozzle. Furthermore they are used in lighters for the ignition of the gas.

Other applications include harvesting energy from environmental vibrations (for example in trains), in order to transform mechanical energy into electrical energy. Other types of applications include mechanical resonators for use in oscillators (quartz oscillators) or detectors for real-time evaluation of fruit firmness [56], as well as detection of viscosity [52].

4.6 Summary

This chapter has presented a brief overview on the physical properties of piezoelectric materials. Particular emphasis was given to the lumped equivalent electro-mechanical circuit of the piezoelectric transformer, showing the major parameters of interest which can be useful in a design phase.

Chapter 5

Piezoelectric transformers for ultra-low voltage applications

This chapter discusses the SoA (state of art) of solutions for stepping-up the ultra-low DC voltage (tens of mV) coming from harvesters like photovoltaic cells or thermoelectric generators. Certain approaches are based on custom integrated solutions coupled with an initial amount of energy (pre-charged capacitor or battery) that serves as essential "initial condition" to perform the boost of the voltage. Other approaches rely on the use of MTs in the so-called Armstrong oscillator. However, the solutions presented in literature are not suitable for compact and integrated performant systems in the application field of EH systems and ultra-low voltage and ultra-low power systems. This chapter presents a novel step-up oscillator based on PTs, which are generally used for high voltage applications. Generally, piezoelectric devices suffer lower losses compared to magnetic devices, and their performance (quality factor) is not directly linked to the thickness of metallizations, as it obviously happens in magnetic devices. Hence, PTs are more suitable for on-chip integration compared to MTs.

This novel step-up oscillator has been used also in a EH scheme, and it serves as kick-starter for a classic boost switching DC-DC converter which, once started, is able to perform a more efficient power conversion.

5.1 State of art of EH systems

Technology scaling in IC processes has allowed a relentless reduction of the power required by electronic circuits for performing given tasks [57], which is an essential feature in order to increase life of mobile, wearable, implantable devices supplied by electrochemical or biofuel cells [58] [59]. Nevertheless, battery replacement would require a lot of maintenance effort if ubiquitous sensor networks or pervasive implantable sensors were deployed. It would be very helpful if these systems could be fully autonomous by scavenging the energy available in the environment in several forms, e.g. light, heat, vibrations, etc. A great challenge for engineers and circuits designers is to exploit the ultra-low output voltage (down to few tens of mV) provided by energy scavenging transducers, and to pump it to an enough level (at least 0.6-0.8V) suitable to overcome the threshold voltage of semiconductor devices, so that a switching converter can be successfully activated. The most frequently used energy transducers are piezoelectric transducers, photovoltaic cells, thermoelectric generators (TEGs), and rectennas for RF (Radio Frequency) energy. Generally, the power density provided by the source to be harvested is in the range of $10-100\mu$ W/cm² [60]. Besides, for example, thermoelectric generators (TEGs) provide output voltages of several tens of mV/K [61], whereas indoor solar cells can provide down to 200mV in low illumination conditions [62]. Unfortunately, these values are not enough to control in an efficient way the gate of power devices in switching DC/DC converters, or to exceed the diode threshold voltage in voltage multipliers, e.g. Greinacher topologies, which also require a transistor-based oscillator for operating. Currently, many works in literature presenting power converter systems for ultra-low voltage energy scavenging purposes do not face the problem of battery-less kick-start, and generally need a supply voltage still higher than that available from the source: to cite an example in [63] and [64] tens of mV can be exploited, but an initial amount energy (like the voltage in a pre-charged capacitor or battery) is mandatory to make a power conversion. A first technique to pump ultra-low voltages consists in the use of capacitive charge pumps, like in [65] and [66]. Even though some circuit approaches [67] [68] can improve the performance, unfortunately the minimum activation voltage is still comparable to the threshold voltage of the semiconductor devices, and hence too much high for

handling the output voltage provided by TEGs. With a threshold voltage adjustment, the minimum activation voltage can be lowered down to 95mV [69]. Another approach is the use of a motion-activated switch to initially drive a boost converter [70], which allows input voltages as low as 35mV. In addition, ultra-low activation voltages are provided by boost oscillators based on magnetic transformers (MTs), a circuit topology known for long [71], re-proposed in literature [72], and now used also in commercial products [73]. In such systems (Figure 5.1), an amplifier stage based on a low threshold voltage transistor is put in a feedback loop together with a MT. The amplifier should achieve a sufficient gain in order to start oscillation when biased by the ultra-low voltage provided by the harvester. Once oscillation is started, a conventional passive voltage multiplier can further boost and charge a storage capacitor. Putting several MTs in cascade [74] can further lower the minimum required activation voltage at the expenses of system dimensions. Furthermore, the MT can also be re-used in a conventional DC/DC converter after the kick-start [75]. The main drawback of this approach is that MTs are difficult to shrink, since a high turn ratio is required for managing the low output voltage of TEGs. Besides, MTs suffer from frequency limitations, core losses and saturation [32].

In general, micro-fabricated magnetic transformers (MTs) are suitable for signal or power isolation [76] and not for voltage boosting purposes, hence they have low turns ratio (generally 1-2), low voltage gain (lower than 0dB) and low magnetizing inductances (lower than 1 μ H). Nevertheless, miniaturized MTs based on bonding wires [33] for voltage boosting purposes [34] [77] have been recently reported. In these cases, the device miniaturization significantly limits the quality factor. Alternatively, transformers based on silicon micro-mechanical resonators and piezoelectric materials have been already proposed [78], hence facilitating the possibility of a package-level integration of mixed microelectronic and MEMS systems. Generally, power conversion in piezoelectric transformers (PTs) can be much more efficient than in MTs, due to their greater quality factors (more than one order of magnitude compared to the magnetic counter-part). This is mainly due to the low mechanical losses in MEMS oscillators. In fact, the quality factors (Q) of piezo-ceramics may be greater than 1000 [79].



Figure 5.1. Schematic of a traditional MT based boost oscillator.

This chapter presents a novel battery-less PT voltage boost oscillator suitable for kick-starting, from fully discharged states, an efficient power conversion system based on TEGs subject to low temperature gradients or photovoltaic cells in indoor environment (Figure 5.2) [80] [81]. The main task of this system is to initially give a sufficient voltage to start an external self-sustaining efficient power converter. Then, the main target is to achieve a start-up voltage as low as possible, and not necessarily an efficiency as high as possible. The presented system is compatible with an inductor-less implementation. Furthermore, the system is compatible with microelectronic and MEMS implementations integrated at package level. In addition, it will be shown that lower start-up voltages can be obtained through the insertion of a small inductor in the input stage. In this specific implementation, based on a commercial PT designed for Cold Cathode Fluorescent Lamps (CCFL) or Liquid Crystals Displays (LCD) backlight (hence high-voltage applications), hence not optimized for ultra-low voltage step-up purposes, the system can boost voltages down tens of mV up to voltage levels useful to control the power devices of a DC/DC converter.



Figure 5.2. Block diagram of an energy harvesting system, lacking a battery.

5.2 Piezoelectric transformers and equivalent electromechanical circuit

The main purpose of this section is to briefly summarize the operation of the PT and to recall the equivalent electromechanical circuit used in circuit analysis. PTs are resonant devices exploiting the direct and inverse piezoelectric effect of certain materials producing polarization charge on their electrodes when subject to a mechanical stress. A typical PT like the step-up Rosen transformer [53] [54], is built by cascading a transverse mode actuator at primary side (that is stress perpendicular to electric field and polarization) with a longitudinal mode transducer [83] at secondary side (that is stress parallel to electric field and polarization): when PTs vibrate at a frequency close to their resonance, an acoustic standing wave is produced with the generation of nodes and antinodes, so that a lumped electromechanical equivalent circuit [54] can be used. Figure 5.3 represents the equivalent circuit of a PT driven in proximity of a particular resonant frequency: C_{d1} is the input electrical capacitance, and in multi-layer transformers it is the parallel of the capacitance of each layer; the series of C_M , L_M and R_M represents the mechanical impedance; N is the equivalent turn ratio related to the stress ratio from input to output; and C_{d2} is the output electrical capacitance, which, for commercial PTs, is generally several orders of magnitude lower than C_{d1} because the distance between the electrodes is higher. Furthermore, PTs are very load-dependent devices [84], in addition their electrical resonance does not correspond to the mechanical resonance. This means that, a



Figure 5.3. Lumped equivalent electro-mechanical circuit of a PT around a certain resonance.

vibrating force at a particular frequency causing the maximum displacement will not generate the maximum output voltage, not even in an open circuit certain configuration because of the intrinsic output capacitor C_{d2} . Considering the input impedance $Y_{IN}(\omega)$ of a piezoelectric device, the resonance frequency f_S is very close to the frequency f_r where $\text{Im}\{Y_{IN}(\omega)\} = 0$, and to the frequency f_M where $|Y_{IN}(\omega)|$ is maximum. These three frequencies cannot be distinguished in a Bode plot [52]. Besides, manufacturers usually insert PTs in a plastic case becoming part of the resonant system, with the PT placed on rubber supports which allow it to vibrate regardless of the mounting. Then, the best way to choose a particular resonant mode without theoretically affecting performance [55] is to mechanically clamp a node.

5.2.1 Identification of the lumped equivalent circuit

In order to better control the system behaviour, a characterization of the PT electro-mechanical parameters is mandatory, given that the actual lumped parameters may somewhat be different from those provided by the manufacturers. There are two main approaches to experimentally identify the PT electromechanical circuit, one is in the time domain [85] and the other one is in the frequency domain [86]. The time domain approach rely on the measure of the decay time constants and the natural resonance frequency, requiring standard instrumentation like signal generators and oscilloscopes [85]. On the other way, frequency domain measurements are based on the admittance circle method [86], and the only necessary equipment is an LCR meter. The admittance circle method basically rely on the similarity of a PT to the Butterworth-Van Dyke lumped circuit for the quartz, when the PT input or output terminals are shorted (**Figure 5.4**). For a quartz crystal, plotting $\text{Im}\{Y_{IN}(\omega)\}$ vs. $\text{Re}\{Y_{IN}(\omega)\}$ yields to a circle (**Figure 5.5**). This implies that for PTs the same



Figure 5.4. PT equivalent circuit with output shorted (top), and input shorted (bottom). Both circuits share the same structure of the impedance of a quartz crystal.



Figure 5.5 Simulated magnitude and phase (left) and admittance circle (right) for the second mode of the SMMTF55P4S80 PT from Steiner & Martins Piezo with a quality factor of Q=452. Y_{IN}=G+iB. Although the three lower frequencies are clearly separated in the circle, they cannot be clearly distinguished in a Bode plot.

definitions used for quartz can be used (e.g. resonance-antiresonance frequency, etc.) At very low frequencies, such 500Hz, or 1kHz (low frequency means a frequency as far as possible from the resonance), since the mechanical quality factor Q of ceramics materials is extremely high [81] as stated before, the impedance of the inductor L_M and that of the resistance R_M are negligible, compared to that of capacitor C_M . So the total measured input capacitance is:

$$C_P = C_{d1} + C_M \tag{5.1}$$

If a frequency sweep around the expected mechanical resonance is made, two phase changes in the LCR meter display can be seen: the lower frequency where the first change of phase occurs is the resonance frequency (or series resonance, the input admittance shows a maximum) f_S , the higher is the anti-resonance (or parallel resonance, the input admittance shows a minimum) f_P .

At the resonance, the impedance of the inductor L_M cancels out with that of the capacitor C_M , so the input admittance of the PT is :

$$Y_{IN}(2\pi f_s) = 1 / R_M + j 2\pi f_s C_{IN}$$
(5.2)

The real part of input admittance, measured at the resonance frequency gives the information about the mechanical resistance. Retrieving the parameters of the piezoelectric transformer by means of the input impedance is more complicated since $\operatorname{Re}\{Y_{IN}\}\neq\operatorname{Re}\{Z_{IN}\}^{-1}$. In **Figure 5.5**, the horizontal diameter of the circle is mechanical conductance. The value of the input capacitance C_{d1} cannot be deducted from the imaginary part of the input admittance at the resonance frequency since around this frequency (and the anti-resonance), the imaginary part shows a steep discontinuity.

Being more precise, the frequency where the input admittance shows a maximum f_M is a little different from the resonance frequency f_S that is the frequency where the real part of the input admittance shows a maximum; since for a second order system it holds that $f_M^2 = f_S^2 \cdot (1 - (2Q)^{-2})$, and these two frequencies are different from the frequency f_r where $\text{Im}\{Y_{IN}(2\pi f_r)\}=0$. This happens also in the anti-resonance where we have three distinct frequencies (frequency where the admittance magnitude is minimum, a frequency where the real part is minimum, and a frequency where the imaginary part experiences a second change of phase). But given that for discrete PTs $Q \ge 400$, it holds that $f_M \cong f_s \cong f_r$. As R_M goes down in value, the major axis of the circle of **Figure 5.5** tends to the line whose equation is $\text{Im}\{Y_{IN}(f)\}=0$.

Since for a quartz crystal, the (series) resonance frequency is:

$$f_s = \frac{1}{2\pi} \sqrt{\frac{1}{L_M C_M}} \tag{5.3}$$

And the anti-resonance (or parallel resonance) frequency is:

$$f_{p} = \frac{1}{2\pi} \sqrt{\frac{1}{L_{M} \frac{C_{M} C_{d1}}{C_{M} + C_{d1}}}}$$
(5.4)

When dividing (5.3) by (5.4), and squaring we obtain:

$$C_{d1} = \left(\frac{f_s}{f_p}\right)^2 \cdot \left(C_{d1} + C_M\right) = \left(\frac{f_s}{f_p}\right)^2 \cdot C_p \tag{5.5}$$

where C_P refers to (5.1).

The mechanical capacitance is given by:

$$C_{M} = C_{P} - C_{d1} \tag{5.6}$$

The inductor L_M is given by:

$$L_{M} = \frac{1}{\left(2\pi f_{s}\right)^{2} \cdot C_{M}}$$

$$(5.7)$$

The only parameter left is the turn ratio N of the ideal transformer of Figure 5.3. We open the output port of the PT, and we short the input. We do the same measures done with the output shorted, since the circuit is structurally the same.

By looking at **Figure 5.3**, the turn ratio *N* is given by:

$$N = \sqrt{\frac{L_{M2}}{L_M}} = \sqrt{\frac{N^2 L_M}{L_M}}$$
(5.8)

where L_{M2} is the inductance calculated from the output port (input shorted) through (5.7).

Table 5.1 shows the parameters obtained with the admittance circle approach for the second resonant mode of the adopted PT sample (SMMTF55P4S80 PT from Steiner & Martins Piezo) using an Agilent E4980A LCR meter, together with other characteristic parameters of the system.

According to the model in **Figure 5.3**, for an unloaded PT the electric resonance frequency is:

Parameter	Value	
C_{d1}	231 nF	
C_M	11 nF	
R_M	363 mΩ	
L_M	0.247 mH	
C_{d2}	19.2 pF	
N	47.2	
\mathcal{Q}	453	
$C_{GS} + C_{GD}(f = 100 \text{ kHz})$	9 - 11 pF	
V_P	$\sim -0.85 \text{ V}$	
$R_{DS} (V_{DS} = 0.1 \text{ V})$	720 Ω	
$g_m (V_{DS} = 0.1 \text{ V}, V_{GS} = 0 \text{ V})$	163 µA / V	
I _{DSS}	$\sim 590 \ \mu A$	
$I_{leakage} (V_{DS} = 0.1 \text{ V}, V_{GS} = V_P)$	< 1 µA	
$\beta_n = 2I_{DSS}/V_P^2$	$\sim 1.63 \text{ mA} / \text{V}^2$	
Cschottky	~ 3 - 4 pF	
C_{PUMP}	470 pF	
C_{STORE}	4.7 μF	

TABLE 5. 1: CIRCUIT SMALL SIGNAL PARAMETERS

 Table 5.1: Linear and small-signal parameters involved in the mathematical model, useful to find minimum activation voltage of the converter [81].

$$f_s = \frac{1}{2\pi\sqrt{L_M C_{eq}}},\tag{5.9}$$

where $C_{eq} = C_M (N^2 C_{d2}) / (C_M + N^2 C_{d2})$. The (electric) anti-resonance frequency is:

$$f_P = \frac{1}{2\pi \sqrt{L_M C_{eq2}}},$$
 (5.10)

where $C_{eq2} = C_{eq} \cdot C_{d1} / (C_{eq} + C_{d1})$.

If the PT is loaded with a capacitor, in (5.9) and (5.10), the capacitance C_{d2} should take into account the total equivalent capacitance at the PT's output port.

5.2.2 Entire system schematic and behaviour

The topology of the proposed voltage boosting circuit is depicted in **Figure 5.6**. A part from the TEG source there can be distinguished: a common source (CS) stage made of (n + m) n-channel JFETs (*MMBFJ201* from Fairchild Semiconductors) working in deep-triode (linear) region, the piezoelectric transformer, and a voltage moluplier (doubler) made up of a 470pF pump capacitor C_{PUMP} , BAS70 Schottky


Figure 5.6. Circuit schematic together with theoretical waveforms. The output of the PT goes directly into the gate of the amplifier JFET J_A , while the voltage doubler boosts and rectifies the amplified oscillation at the PT's output. The DC voltage of the oscillation at node B depends on the used transistor: in case of JFET, this is lower than 0 V, in case of depletion MOSFET it is around 0V [81]. (© 2015, Elsevier).

diodes D_{1,2}, and a 4.7 µF low-leakage storage capacitor C_{STORE} . The JFETs J_A and J_L have a finite trans-conductance even when their drain to source voltage is few tens of mV. The resistor R_F (\approx 140 M Ω) is required for draining part of the current at the output out from the gate of the JFETs, given that if the amplitude of oscillations reach at least ~0.5 V, the gate to source pn junction can partially turn on causing the gate to lose its control over the channel, and consequently the transistor effect will be lost. R_F is also required to discharge any possible bias charge on the gate capacitance of J_A causing the transistor to be completely off. Simultaneously, R_F must be enough high in order not to produce load effects at the PT output port, and not to lower its voltage gain. The resistor R_T models the internal series resistance of the low voltage source V_{IN} .

Only at the beginning of the oscillation, when node B almost at 0 V, the load effect of the voltage doubler can be modelled as a linear impedance, made up by the intrinsic capacitances $C_{SCHOTTKY}$ of the Schottky diodes (less than 3pF/diode) because the parallel differential resistance of the diodes ($\approx 10 \text{ M}\Omega$), C_{PUMP} , and C_{STORE} present higher impedance at the working frequency. Thus, the cascade connection of more Schottky devices can reduce the load effects at the PT output port. In this particular implementation, each Schottky diode in **Figure 5.6** represents the series connection of four diodes: this configuration can partially affect the steady-state voltage at C_{STORE} ;

nevertheless, due to the low currents involved (in general less than 100nA), the voltage drop caused by each diode is slightly less than 100mV, so the number of series diodes comes from a trade-off between minimum activation voltage and steady-state output voltage. In addition, when the oscillation is in steady state, small signal analysis is no more valid because of the significant nonlinearities of rectifier diodes.

Figure 5.6 also shows the theoretical waveforms involved in the system: when V_{IN} reaches the minimum input voltage $V_{IN,MIN}$ satisfying the Barkhausen gain criterion, the oscillation is triggered. Before the starting of the oscillation, V_A follows V_{IN} with a scaling factor due to the voltage divider composed by the *n* amplifier JFETs (nJ_A) and the *m* load JFETs (mJ_L), whereas during oscillation, V_B is almost in opposition of phase with respect to V_A . The steady-state DC voltage of V_B depends on the type of transistor used in the CS stage. In case of JFETs, this DC voltage is few hundreds of mV under 0 V, given that the system can oscillate only if the gate-source p-n junction of the JFETs is not forward biased; in case of depletion MOSFET, this DC value is extremely near to 0 V. V_{OUT} starts growing exponentially until the oscillation at node B reaches steady-state. After this, V_{OUT} follows the typical charging law of a RC circuit.

For the determination of the oscillation condition, it is worth performing a small-signal analysis. In the initial condition, the DC voltage V_A depends on the number of amplifier and load JFETs, respectively n and m: $V_A = m / (n + m) \cdot V_{IN}$. It can be found out that the transconductance g_{mA} of each amplifier JFET is: $g_{Ma} = \beta_n V_A = g_m \cdot m / (n + m)$, where $g_m = \beta_n V_{IN}$ is assumed as a reference value, and β_n is the current gain factor of the JFET. For JFETs we have that $\beta_n = 2I_{DSS} / V_P^2$, where I_{DSS} is the drain current at zero gate voltage and V_P is the negative *pinch-off* (or threshold) voltage. The transconductance g_{mL} of each load JFET is: $g_{mL} = \beta_n (V_{IN} - V_A) = g_m \cdot n / (n + m)$. The output conductance g_{dsA} of each amplifier JFET is $g_{dsA} = \beta_n (-V_P - V_A) \cong -\beta_n V_P$, under the real assumption that $|V_P| >> V_{IN}$, as it happens in this case. The output conductance g_{dsL} of each load JFET is: $g_{dsL} = \beta_n (-V_P - V_I) \cong -\beta_n V_P$. A unique symbol g_{ds} , defined as $g_{ds} = g_{dsA} = g_{dsL}$, can then be used. In addition, all the JFETs work in their linear region, thus, the small signal output conductance g_{ds} equals the large signal conductance G_{DS} of each device.

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Under the above assumptions, it also holds that $g_{dsA,L} >> g_{mA,L}$. Then, the unloaded voltage gain A_{Vcs0} of the input stage with *n* parallel amplifier JFETs and *m* parallel load JFETs can be expressed as:

$$A_{V_{cs0}} = -\frac{ng_{mA}}{mg_{mL} + ng_{dsA} + mg_{dsL}} \cong -\frac{ng_{mA}}{(n+m)g_{ds}} = -\frac{nm}{(n+m)^2} \frac{g_m}{g_{ds}} = -\frac{nm}{(n+m)^2} \frac{V_{IN}}{V_P}$$
(5.11)

In (5.11) the effect of R_T (typically few Ω in TEGs) is not considered, given that it is generally significantly lower than the typical output resistance $1/G_{DS}$ of the load JFETs. Furthermore, in large signals behaviour, R_T does not affect significantly the differential parameters. From (5.11), it also descends that the maximum unloaded gain occurs when n = m.

In case of a value of R_T not negligible, two effects should be taken into account: the voltage drop across the R_T , which decreases the effective bias voltage for the common source stage, and the decreased output conductance of the common source stage. In this case (5.11) has to be rewritten as:

$$A_{VCS0} \cong -\frac{ng_{mA}}{ng_{ds} + \frac{mg_{ds}}{1 + mg_{ds}R_T}} \frac{1}{1 + (n + m)g_{ds}R_T}$$
(5.12)

The gain A_{VCS} of the loaded input stage can be obtained considering that the input impedance $Z_{PT}(s)$ of the PT, loaded by the gate capacitance of the *n* amplifier JFETs, is connected in parallel to the output resistance of the CS stage:

$$A_{VCS} \cong -\frac{ng_{m1}}{(n+m)g_{ds} + 1/Z_{PT}(s)} = A_{VCS0} \cdot \frac{Z_{PT}(s)}{r_{out} + Z_{PT}(s)} = A_{VCS0}A_{L}(s), \quad (5.13)$$

where $1/r_{out} = (n + m)g_{ds}$, and $A_L(s)$ is the fractional term in (5.13).

The whole capacitance C_{OUT} at the output port of the PT is $C_{OUT} = C_{d2} + n \cdot C_G + C_{VD}$, where C_{VD} is the global small-signal capacitance of the voltage doubler, and C_G is the total input capacitance of a single amplifier JFET. C_G is the sum of the gate-source capacitance C_{GS} and the gate-drain capacitance C_{GD} due to the Miller effect. C_{OUT} can be also transported into the primary section with a scaling factor N^2 and the ideal transformer can be replaced by a voltage controlled voltage source of gain equal to N. Then, the voltage step-up ratio of the PT is:

$$A_{VPT}(s) = \frac{C_{eq}}{NC_{out}(s^2 L_M C_{eq} + sR_M C_{eq} + 1)},$$
(5.14)

where $C_{eq} = N^2 C_{OUT} C_M / (N^2 C_{OUT} + C_M)$. The loop gain A_{VT} is the product of the gain A_{VPT} and the gain A_{Vcs} . The Bode plots of the involved voltage gains are shown in **Figure 5.7**.

The Barkhausen phase criterion establishes that the phase shift must be 360° around the loop in order to obtain a possible oscillation. The inverting CS stage gives an initial phase shift of 180° (see (5.11)). Looking at (5.14) it is possible to note that the PT behaves like a second order system: as a matter of fact in a very small neighbourhood of the anti-resonance frequency f_P the phase shift introduced is slightly less than 180° due to its very high Q factor. The remaining few degrees to reach 360° around the feedback loop are given by $A_{L}(s)$ in (5.13), which introduces an additional negative phase shift at a frequency extremely close to f_P . In order to find the oscillation frequency f_{OSC} , it can be observed in Figure 5.7 that in proximity of f_P , the phase diagram of the loop gain has a very steep slope: for the adopted sample the slope is about 0.21°/Hz around anti-resonance f_P , which occurs beyond 100 kHz. At f_P the phase shift of A_{VPT} , from numerical computations, is about 178°. In order to reach 180°, the remaining few degrees are given by A_L . Hence, the 360° required by the Barkhausen phase criterion do not occur precisely at f_P . It can be verified numerically that f_P and f_{OSC} are shifted by $(180 - 178)^{\circ}/(0.21^{\circ}/\text{Hz}) = 10$ Hz. For this reason, and since at f_P the phase of the loop gain is almost 360°, the safe approximation $f_{OSC} \cong f_P$ can be made. Besides, it follows that $(f_P - f_{OSC})/f_{OSC} < 0.1\%$.



Figure 5.7. Simulated Bode diagrams of the PT input impedance and of the voltage gains involved in the feedback loop. The oscillation frequency f_{OSC} is extremely close to the parallel resonance.

With (5.10) and (5.14), the modulus of the PT step-up ratio at f_{OSC} is easily found as follows:

$$|A_{VPT}(f_{OSC})| \cong |A_{VPT}(f_P)| = \frac{C_{eq}}{NC_{OUT}} \left| -\frac{C_{eq}}{C_{d1}} + j\frac{R_M C_{eq}}{\sqrt{L_M C_{eq2}}} \right|^{\cong}$$

$$\cong \frac{C_{eq}}{NC_{OUT}\sqrt{\left(\frac{C_{eq}}{C_{d1}}\right)^2 + \frac{1}{Q^2}}} \cong \frac{C_{d1}}{NC_{OUT}},$$
(5.15)

in the previous expression $Q = \omega_s L_M / R_M$, and $\omega_s = (L_M C_{eq})^{-1/2}$ is the electric resonance pulsation. The approximation made in (5.15) is valid if $Q^2 >> (C_{d1} / C_{eq})^2$, which is generally verified in multilayer PTs thanks to their extremely high quality factor. In our case, Q^2 is almost three orders of magnitude higher than $(C_{d1}/C_{eq})^2$. Thus, the PT voltage step-up ratio at f_P does is independent from the quality factor.

The PT input impedance $Z_{PT}(s)$ can also be calculated:

$$Z_{PT}(s) = \frac{1}{sC_{d1} + \left(sL_M + R_M + (sC_{eq})^{-1}\right)^{-1}} = \frac{s^2L_M C_{eq} + sR_M C_{eq} + 1}{s(C_{d1} + C_{eq})(s^2L_M C_{eq2} + sR_M C_{eq2} + 1)},$$
(5.16)

that is the same mathematical expression of the impedance of the Quartz.

From (5.16), it is possible to note that the poles are very close to the zeros since $C_{eq2} \cong C_{eq}$. By switching (5.16) to the frequency domain by putting $s = j2\pi f$, we find out that the modulus of $Z_{PT}(s)$ is maximum when $(s^2L_MC_{eq2}+sR_MC_{eq2}+1)$ is minimum and this happens at a frequency extremely close to $f_P=1/2\pi \cdot (L_MC_{eq2})^{-1/2}$. Hence, given that $C_{eq} \cong C_M$, and that the quality factor is very high, from (5.16) it can be found that $|Z_{PT}(s)|$ is maximum when $Z_{PT}(s)$ is almost a real quantity (see also Figure 5.7):

$$\left|Z_{PT}(f_{P})\right| \cong \left(\frac{QC_{eq}}{C_{eq}+C_{d1}}\right)^{2} R_{M} \cong \operatorname{Re}\left\{Z_{PT}(f_{P})\right\}$$
(5.17)

By using (5.10), (5.13), (5.15), (5.17), the whole loop gain $A_{VT}(f)$ at f_{OSC} is easily determined as follows:

$$A_{VT}(f_{OSC}) \cong A_{VT}(f_{P}) \cong \frac{V_{IN}}{|V_{P}|} \cdot \frac{n \cdot m}{(m+n)^{2}} \cdot \frac{C_{d1}}{NC_{OUT}} \cdot \frac{Z_{PT}(f_{P})}{Z_{PT}(f_{P}) + 1/[(n+m)g_{ds}]}$$
(5.18)

At this point a further clarification should be done. Being more precise, through (5.18) we are not evaluating the loop gain, but the so called *return-ratio*, that is essentially the one-way gain that an injected signal experiences within the loop. This method assumes that all blocks constituting the system are unilateral, but in general this could not correspond to the reality given that in the return ratio, the effect of the dependent voltage or current generator (according on how the port system is modelled) driven by the output voltage or current in the input port is neglected in the common source, whilst in the PT the dependent current or voltage generator is neglected in the output port (see **Figure 5.8**).



Figure 5.8. Two port representation of the system. Calculating the return ratio assumes to neglect the effect of the dependent current generators $g_{12}I_2^{CS}$ and $h_{21}I_1^{PT}$.

By looking at **Figure 5.8**, we can state that $g_{11}=s \cdot (nC_G)$, $g_{21}=A_{VCS0}$, $g_{22}=1/(n+m)g_{ds}$, $h_{11}=1/s \cdot (C_{d2}+C_M/N^2)$, $h_{12}=A_{VPT}(f_{OSC})$, $h_{22}=Z_{PT}(f_{OSC})$. For a common source stage we can state that $g_{12}=0$. Given that the PT is a reciprocal system, we can state $h_{12}=-h_{21}$.

We only need to find h_{11} . This parameter is obtained by putting V₂=0, hence the equivalent circuit of the PT becomes the one in **Figure 5.4b**, and the mathematical expression is:

$$h_{11}(s) = \frac{s^2 L_M C_M + s R_M C_M + 1}{s \left(C_{d2} + \frac{C_M}{N^2} \right) (s^2 L_M C_{eq3} + s R_M C_{eq3} + 1)}$$
(5.19)

In (5.19) $C_{eq3}=C_{d2}C_M/(N^2C_{d2}+C_M)$. Equation (5.19) should be evaluated at $s=j\omega=j(L_MC_{eq2})^{-2}$ Since $C_{eq2}>> C_{eq3}$, the antiresonance of h_{11} is placed at frequencies much higher than f_{OSC} . Hence (5.19) can be rewritten as:

$$h_{11}(f_{osc}) \approx \frac{s \frac{C_M}{C_{eq2}}}{\left(C_{d2} + C_M / N^2\right)} \approx \frac{j2\pi f_{osc}}{\left(C_{d2} + C_M / N^2\right)}$$
(5.20)

Hence this output impedance behaves like an inductor at f_{OSC} . However at this frequency the impedance of this inductor is much lower than that given by g_{11} , so

there is not any load effect from the common source stage to the PT.

From (5.15) and (5.17) it is possible to note that a high value of C_{d1} is preferable to achieve a high gain. Nevertheless, simultaneously, a lower value of C_{d1} increases the PT input impedance and lowers the load effect on the previous stage. This implies that, if a PT with an extremely high Q (i.e. around 1000) were used, the connection of an external capacitor in parallel to C_{d1} would decrease Z_{PT} according to (5.17), without affecting too much A_L in accordance to equation (5.13), and would enlarge A_{VPT} according to (5.15). In this particular implementation, the value of (5.18) can be maximized through a proper selection of the capacitance value of this additional capacitor.

If $|A_{VT}(f_{OSC})| \ge 1$, the oscillation is then triggered in accordance with the Barkhausen gain criterion. By solving (5.18) for V_{IN} , the minimum input voltage required to trigger the oscillation is found to be:

$$V_{IN,MIN} > \frac{(m+n)^2}{m \cdot n} |V_P| \cdot \frac{NC_{OUT}}{C_{d1}} \cdot \left[R_M + \frac{1}{(n+m)} \frac{|V_P|}{2I_{DSS}} \frac{1}{Q^2} \left(1 + \frac{C_{d1}}{C_{eq}} \right)^2 \right]$$
(5.21)

It is worth to remark that the both Barkhausen criteria were exploited in order to find the oscillation condition. However, these criteria have not a general validity, given that they give only necessary but not sufficient conditions [31]. As a matter of fact, they assess the oscillation condition from steady state response, and not from transient response. In fact, there are many linear systems that satisfy both Barkhausen criteria but do not oscillate [87]. These systems are called *conditionally stable*. Hence, a more rigorous method, such as root locus, Routh criterion or Nyquist plots, have to be adopted. In this specific implementation, the mathematical model of the system was implemented in Matlab, and the root locus showed two complex poles in the right half plane if $V_{IN} > V_{IN,MIN}$.

However, an intuitive reason explaining the instability of the system can be found in (5.16): $Z_{PT}(s)$ has zeros extremely near to its poles. Hence, from a stability point of view, they almost cancel each other, as a matter of fact in the root locus the poles are attracted by the nearest zeros. Then, in open loop, the system described by (5.18) is essentially a system with only complex poles that is always unstable in a feedback loop with a proper gain that allows satisfying the Barkhausen gain criterion.

Furthermore, we have shown only the full wave mode. Nevertheless, the

oscillation at the very beginning might occur simultaneously at first and second mode, if the loop gains around the frequencies of both modes are greater than unity and comparable, and if the two modes are approximately separated by an integer number (two in this specific case). For the adopted PT, the first electrical parallel resonance is placed at about 55.117 kHz (accounting for all the capacitive load effects due to the JFETs and voltage doubler), whereas the electrical parallel resonance related to the second mode occurred at about 106.8 kHz. Other modes have little gain and hence were neglected in the analysis. The oscillation, at the beginning, might occur at the first mode, as predicted also also by SPICE simulations performed with the equivalent electromechanical circuit of the PT. Nevertheless, as the amplitude of the oscillation grows up in amplitude, the nonlinearities start to produce a harmonic at a double frequency. Thus, the energy of the first oscillating mode is spread in two bands: the first is centred on the first mode, whereas the second is placed in a band very close to the second mode. Thus, energy is gradually removed from the first mode, and injected into the second mode that gains more and more excitation. At the end of the transient, the system will be locked at the second mode. Generally, Barkhausen criteria are not valid if they are satisfied in more than one point, and hence Bode plots become useless. Placing a filter in the loop, or mechanically clamping some nodes, allows selecting the desired mode of oscillation.

The values of the components of the lumped circuit of the PT and of the other devices used in the calculations are reported in **Table 5.1**. Each value of the parameters of the JFETs was extracted from a single random selected device sample.

Furthermore, if the parameters change because of environmental variations the circuit will always self-lock extremeley close to the actual anti-resonance frequency. This circuit is devised for ultra-low power energy scavenging applications (tens of μ W) and thus, heat dissipation is not necessarirly an issue. However, it is worth to note that temperatures above 110°C might shift both f_S and f_P , and worsen the overall quality factor, because of parameters variations of the PT. At these temperatures, JFETs as well experience parameter variations, and hence $V_{IN,MIN}$ increases. Besides the adopted PT, as well as commercial devices, is intended to handle power levels in the order of several Watts (e.g. backlight for LCD), with maximum input voltages of 18 V (rms) and maximum output voltages of 1800 V (rms). Thus it is not devised for ultra-low voltage and micro-power applications, given that the presented

implementation is not a typical application of PTs. A custom PT design might present a better performance in a smaller volume. Besides, the adopted JFETs are intended for audio applications and so there is not any voltage limitation due to these devices.

5.3 Measurements on the implemented demonstrator

Figure 5.9 shows the implementation of the system used for model validation. An Agilent E3631A power supply was initially used instead of a real TEG, in order to control in a proper way the input voltage. Data were recorded with a Tektronix MSO2024 oscilloscope. The optimum values of *n* and *m*, 3 and 5 respectively, were numerically found with the analytical model implemented in Matlab. An external resistor $R_T = 2.4\Omega$ was used to emulate the parasitic resistance of a Multicomp MCPE-071-10-15 TEG source. Nevertheless, this is a worst case assumption, given that TEGs with parasitic resistances lower than 1 Ω [61] are commercially available. The current drained by R_T was measured with an Agilent 34401A digital multimeter, and the voltage drop was found to be less than 0.5mV for $V_{IN} = 69$ mV. This very low, voltage drop does not affect either the JFET small signal parameters or the bias point. Hence the safe assumption of neglecting R_T in the mathematical expressions is reasonable. In addition, the DC current at start-up was found to be less than 200µA.

The measured waveforms during the kick-start of the system for [n = 3, m = 5] are reported in **Figure 5.10a**. The input voltage V_{IN} was increased like a slowly rising ramp in order to emulate a TEG subject to a slowly varying temperature gradient. The oscillation is triggered when $V_{IN} \cong 69$ mV, whereas (5.21) predicts 70mV. However, if different samples of JFETs are used, $V_{IN,MIN}$ can increase up to about 81mV due to the variations in the discrete device parameters. To cite an example, among the tested devices, R_{DS} was found to be in the range $663 \Omega - 731\Omega$. The storage capacitor is charged to about 1.5V when there is not any load connected. Texas Instruments LMC6482A operational amplifiers were used in a buffer configuration in order to not have load effects. The JFET parameters used in the equations (**Table 5.1**) were extracted from measures performed on the selected samples.



Figure 5.9. Picture of the experimental setup.



Figure 5.10. Measured start-up waveforms with [n = 3, m = 5] obtained with: (a) a power supply with a series connected resistance of 2.4 Ω ; (b) a Multicomp MCPE-071-10-15 TEG source [81].

Figure 5.10b shows the waveforms obtained during the system kick-start with a Multicomp MCPE-071-10-15 TEG source in the same optimum configuration. The TEG was placed close the air vent of a laptop computer. The environmental temperature was about 26 °C, and the temperature at the air vent output was about 52 °C. C_{STORE} started being charged when the TEG voltage reached 79mV, which is comparable with the previously obtained measurements. However, it is worth to say that a different set of JFETs was used with the TEG.

When the transient has expired, the minimum voltage able to maintain the system in oscillation was found to be about 56mV, which is lower than the start-up voltage. This occurs because in steady-state the gate signal at node B (see Figure 5.11) falls below the JFET threshold voltage ($V_P \simeq -0.85$ V), thus the device current is zero for a large portion of the switching period, hence the input stage is more efficient. The measured average current drained by the common source in steady state drops to about 117 μ A. Figure 5.11 compares the measured voltage signals of V_A (PT input port) and V_B (PT output port): the phase shift of about 178° proves that the PT is oscillating at a frequency extremely close to the parallel resonance f_P , as discussed before and as depicted in Figure 5.7. The oscillation frequency is 105.3kHz, somewhat different from model predictions. There are two main causes: (i) the model is valid when the oscillation is starting and not in the steady state; (ii) the few additional pF of the probes have a load effect at the PT output port (V_B) , increasing C_{OUT} , and thus lowering f_{OSC} . Without probes at node B, f_{OSC} is measured (at node A, where there is little load effect) to be about 106.4kHz against the 106.8kHz predicted by the mathematical model.

Figure 5.12 shows a comparison between (5.21) and measurements, with different values of n and m. It can be noticed that all the mismatches between the mathematical model predictions and measurements are within 15%.



Figure 5.11. Measured steady-state voltage signal of V_A (PT input port) and V_B (PT output port). The measured phase shift is $\Delta \varphi = -178^{\circ}$ [81].



Figure 5.12. Corner analysis compared to model predictions and measurements [81]. (© 2015, Elsevier).

In addition, in order to evaluate the behaviour of the system subject to variations in device parameters, corner simulations were performed with the assumption that V_P , β_n and C_G can experience relative variations of $\pm 10\%$ with respect to their values assumed as reference. The best condition in terms of minimum V_{IN} (*bc curve*) occurs when C_G is 10% lower, whereas $|V_P|$ and β_n are 10% higher. Dually, the worst condition (*wc curve*) occurs when C_G is 10% higher, while $|V_P|$ and β_n are 10% lower. As can be seen from **Figure 5.12**, the curve obtained from measurements (*meas* *curve*) always lies between the *bc* and *wc* curves. The reference curve (*ref*) was obtained considering for the JFET parameters the values shown in **Table 5.1**. Besides, a main reason producing the mismatches has to be found in the fact that certain particular configurations of *n* and *m* partially invalidate the first assumption of deep triode region for the JFETs. Given that $|V_P| = 0.85$ V and that V_{GS} is assumed 0V for both load and amplifier JFETs, for the optimum configuration (n = 3, m = 5) we have that $V_{DS1} = V_{IN}(m/(n+m)) = 44$ mV and $V_{DS2} = V_{IN}(n/(n+m)) = 36$ mV (both calculated at $V_{IN} = 70$ mV), so the relation $V_{DS1,2} << |V_P|$ is verified.

Nevertheless, to cite an example, configurations such as [n = 1, m = 5] are out of the mathematical model: given that the mathematical model predicts a minimum activation voltages of 179mV, the two drain to source voltages of amplifier and load JFETs are $V_{DS1} = 149$ mV and $V_{DS2} = 30$ mV. The *n* amplifier JFETs and *m* load JFETs do not anymore make a voltage divider because only the load JFETs are in the linear region. Dually, for a configuration like [n = 5, m = 1] only the amplifier JFETs are biased in the linear region. The previous considerations can be applied also to other configurations. Generally, the presented mathematical model cannot be applied to configurations which deviate from the optimum in terms of minimum input voltage, given that in these cases either the amplifier or load JFETs are not polarized in their linear region. In these cases the values predicted by the mathematical model are higher than the measured, given that the devices are closer to the pinch-off region where the transconductance and output conductance values are higher with respect to the linear prediction. So the mismatch between model and measurements is minimized around the optimum condition for n and m, because the activation voltage is at its minimum and the JFETs make a linear voltage divider. In addition the mathematical model correctly indicates the direction towards which n and m should be changed in order to reach the optimum configuration.

Even though for configurations like m = 1 it may seem that there is a lack of qualitative fit between measured curves and mathematical model, it is worth saying that both mathematical model and measurements predict the point of minimum kick-start voltage located at n = 3. For other configurations, the eventual lack of qualitative fit is due to the random positioning of devices, given that each sample is slightly be different from the other.

Figure 5.13a depicts the voltage of the storage capacitor as a function of the input voltage for various values of load resistance ranging from 10 M Ω to 1 G Ω (which can be considered the open circuit condition). The 10 M Ω load can be considered the one due to an ultra-low power voltage monitor circuit [65] [88] made with discrete components, which starts the main power converter when a sufficient voltage is reached. Higher value load resistances are achievable by integrated circuits. With the minimum voltage, at steady-state $V_{OUT} = 1.5$ V in the open circuit case, and drops to 0.55V with 10M Ω . As it can be noticed, the behaviour is nearly linear with an average slope ranging from 18.3mV/mV ($10M\Omega$ load) to 25.6mV/mV ($1G\Omega$ load). Hence, in order to obtain a 100mV increase in V_{OUT} , the TEG voltage should be increased of about 4-5mV in all cases. The comparison between the output power P_{OUT} with the maximum TEG power P_{MAX} and with the actual TEG power P_{TEG} is helpful to evaluate the overall performance. P_{OUT} can be written as $P_{OUT} = P_{MAX} \cdot \alpha \cdot \beta$, where $\alpha = P_{TEG}/P_{MAX}$, and β is the electric efficiency of the circuit. It follows that $0 < \alpha < 1$, $0 < \beta < 1$, and $P_{MAX} = V_{IN}^2 / (4R_T)$. In the condition $V_{IN} = 69$ mV, before the oscillation is triggered, the DC power related to the common source is $P_{TEG} = 12.76 \mu W$ whereas the current is $I_{TEG} = 180 \mu A$ (with n = 3, m = 5, $R_T = 2.4 \Omega$, and $R_{DS} \cong 720\Omega$ for each JFET). In steady-state, I_{TEG} drops to about 125µA, and P_{TEG} to about 8.7μ W, thanks to the higher efficiency of the input stage. Figure 5.13b depicts the output power as a function of the load, for various values of the input voltage.

The power is monotonically decreasing with the input voltage; thus, the optimum load resistance is obviously lower than 10M Ω . However, load values under 10M Ω were not considered because the corresponding V_{OUT} is not sufficient for the purposes of the presented system. At the minimum input voltage, P_{OUT} ranges from tens to hundreds of nW, and $P_{MAX} = 495 \mu$ W. This entails that $\alpha \cong 2\%$. Nevertheless, α is necessarily low: it is obligatory that the loaded TEG provides the minimum operating voltage required by the circuit.



Fig.ure 5.13 (a) Measured steady-state output voltage V_{OUT} as a function of source voltage V_{IN} for various loads. (b) Measured output power P_{OUT} as a function of R_{LOAD} for various V_{IN} [81]. (© 2015, Elsevier).

Hence, if the open-circuit voltage of the TEG is slightly higher than the minimum kick-start voltage, the TEG should be necessarily biased in an almost open-circuit condition, that far from its maximum power point (MPP). A TEG biased in the MPP would provide only half of its open-circuit voltage. Generally, α can be increased if higher TEG voltages are available. Nevertheless, in this case, start-up circuits can be considered not necessary. For the presented implementation, it can also be verified that $\beta \cong 1\%$, and that the bias current of the input stage is the main reason of power losses. Generally, step-up oscillators are not easily tuned on the MPP. For this reason, dual architectures are usually proposed, as in [73]. In this specific case, the boost circuit is used only for the kick-start from a fully discharged state and, from then on, the main converter should remain active. Nevertheless, this might prevent all applications where a fast recovery time from long power outages is required. In order to lower the recovery times, energy scavenging systems with separate differently-sized capacitors for the power converter and the load have been recently reported [89].

5.4 Lowering the activation voltage

Given that the main target of the present start-up system, was to be compatible in perspective with IC processes and MEMS technologies, PTs were primarily used in this implementation instead of MTs. In the boost Armstrong oscillator based on a MT (**Figure 5.1**) voltage source biases directly the amplifier JFETs, whose g_m is proportional to V_{DS} . As a matter of fact, in DC the primary side of the MT is a short circuit, whereas JFETs used in this implementation act like a voltage divider. In order to introduce the previous mentioned advantage of the MT-based solution, the load JFETs can be substituted by an inductor L_S as shown in **Figure 14a**. Even though this deviates from the primary target of achieving an inductor-less solution, it may still be acceptable in certain applications due to the relatively low value of the required inductance. Furthermore the size of the required inductor is still much smaller than that of the conventional MTs (several mm²) used in step-up oscillators. Tiny inductors can be also potentially integrated at package-level as seen in the first chapter.

From (5.11), for case n = m, it follows that the unloaded voltage gain of the CS stage is a quarter of that of the same stage with same value of n with an inductive load of proper value in place of the load JFETs: in DC the inductor acts like a short and then amplifier JFET is fully biased by the low voltage source; thus, the overall g_m is doubled; furthermore, the output conductance of the CS stage is halved, since this is only ng_{ds} and not $(n + m)g_{ds}$. Nevertheless, in order not to alter the system behaviour at f_{OSC} , it is mandatory that at this frequency L_S has already resonated with the PT input capacitance C_{d1} . Hence, the following relation should be verified:

$$L_{s} > \frac{1}{\left(2\pi f_{osc}\right)^{2} C_{d1}}$$
(5.22)

At the measured f_{OSC} of 106.4kHz, with $C_{d1} = 231$ nF as reported in **Table 5.1**, according to (5.22) it entails that $L_S > 10\mu$ H, so that, roughly even 30 - 40 μ H can be enough. If the quality factor of the inductor is high, at f_{OSC} the phase shift introduced by the first stage is always 180°; thus, the oscillation will be triggered at f_P . If the quality factor Q_L of the inductor is low, the equivalent resistance of L_S will introduce losses, lowering the output resistance of the input stage, and shifting f_{OSC} far from f_P .



Figure 5.14. a) Replacement of the load JFETs with a generic lossy inductor L_S . b) Equivalence of the series series $L_S - R_S$ circuit with the parallel $L_P - R_P$ at a given frequency [81]. (© 2015, Elsevier).

In the case of inductive load in the CS stage, the series resistance R_T of the TEG cannot be neglected anymore. The effect of R_T can be considered together with the equivalent series resistance of L_S and call this global resistance R_S . In addition, it can be demonstrated that the series combination of L_S and R_S can be modelled at a particular frequency, e.g. f_{OSC} , as a parallel combination of an inductor L_P and a resistor R_P , as depicted in **Figure 5.14b**:

$$L_{p} = L_{s} \left(1 + Q_{L}^{2} \right) / Q_{L}^{2}$$
(5.23)

$$R_{P} = R_{S} \cdot \left(1 + Q_{L}^{2}\right) \tag{5.24}$$

where $Q_L = 2\pi f_{OSC}L_S /R_S = R_P / (2\pi f_{OSC}L_P)$. Thus R_P is a frequency dependent resistor. Nevertheless, R_S as well can be frequency dependent (as seen in the second chapter), because of eddy currents and hysteresis losses in the core and of the skin depth and proximity effect in the winding. Thus, the proper choice of the inductor should not be based only on its DC resistance. As rule of thumb, if $Q_L > 4$, then $L_P \cong L_S$ and $R_P \cong R_S Q_L^2$. In order for R_P to be negligible in the calculations, it is necessary that $R_P >> 1/(n \cdot g_{ds})$. Hence, R_S should verify the following relation:

$$R_{\rm S} \ll \left(2\pi f_{\rm OSC} L_{\rm S}\right)^2 \cdot ng_{\rm ds} \tag{5.25}$$

If (5.25) is verified and L_S is high enough, in first approximation A_{Vcs} is not dependent on *n* if this parameter is chosen as high as possible. Nevertheless, as an upper limit, the *n* parallel gate capacitances of the amplifier JFETs should not increase too much the PT output capacitance C_{OUT} , which affects A_{VPT} according to (5.18). Then if *n* is too high, the value of A_{VPT} starts to decrease. Increasing *n* as well relaxes the condition about R_S . The same occurs with L_S , if R_S is mainly due to the TEG. The mathematical model can be adapted according to the following mathematical expression:

$$A_{V_{CS}} = -\frac{g_m}{g_{ds}} \frac{Z(s)}{Z(s) + (ng_{ds})^{-1}},$$
(5.26)

where g_m and g_{ds} are the transcondutance and output conductance of a single JFET and $Z(s) = (1/Z_{PT}(s) + 1/R_P + 1/(sL_P))^{-1}$. If (5.22) and (5.25) are verified, the effect of L_P and R_P can be safely neglected.

Figure 5.15a depicts the simulated Bode plots of the loop gain obtained with $V_{IN} = 70 \text{mV}$ (that is about the voltage required to start the inductor-less system) in different configurations: the loop gain with n = 3 and m = 5 reaches exactly 0dB at 0° of phase shift. When $L_S = 37\mu$ H and $R_S = 3.05\Omega$, a maximum gain of about 4.8dB is achieved when $4 \le n \le 6$ at the same V_{IN} . This implies that $V_{IN,MIN}$ can be decreased from 70mV down to about 40mV, since $20\log_{10}(40 / 70) \cong -4.8$ dB. In experimental measurements, as it can be noticed from Figure 5.15b, with n = 4 the minimum kick-start voltage drops to about 40mV, if a Multicomp MCPE-071-10-15 TEG with ~ 2.4 Ω internal resistance, and a 37 μ H inductor with ~0.65 Ω series resistance at 106kHz are used. In this specific case the TEG was placed close to the AC/DC adapter of a laptop, whose external temperature was measured to be around 42°C. In these cases as well, if the measurements are repeated with a random choice of the namplifier JFETs, the variations in $V_{IN,MIN}$ are somewhat higher than the deviations from the theoretical values. In this specific case, measurements show that $32\text{mV} \le V_{IN,MIN} \le 35\text{mV}$ with n = 3 and $R_S \ge 0.65\Omega$, whereas with n = 6 and $R_s \cong 1.2\Omega$, the measurements show that $34\text{mV} \leq V_{IN,MIN} \leq 36\text{mV}$. Experiments performed with n = 3 and $R_S \approx 1.2\Omega$ showed that $V_{IN,MIN}$ can range from 48mV up to 52mV with a random choice of JFETs. However, this also proves that if *n* is increased, higher values of R_s can be tolerated as predicted by (5.25). Generally, higher value of R_{s} , considering the same value of n, could be very critical for the minimum activation voltage.



Figure 5.15. (a) Simulated loop gain at $V_{IN} = 70$ mV and $R_T = 2.4\Omega$ with the load JFETs in the optimum condition (n = 3, m = 5) and with the use of the inductor ($L_S = 37\mu$ H, and 0.65 Ω of parasitic series resistance) for different values of n. In the reference case with load JFETs, the loop gain is exactly 0dB. In case of an inductive load in place of the JFETs, at the same V_{IN} a maximum gain of about 4.8dB is achieved, implying that V_{IN} can be proportionally decreased to about 40mV. (b) Measured kick-start signals obtained with a Multicomp MCPE-071-10-15 TEG source with an inductor of 37μ H and 0.65 Ω of parasitic series resistance [81]. (© 2015, Elsevier).

Figure 5.16a plots the linear trend of V_{OUT} versus V_{IN} with an inductive load and n = 4. The resulting slope is 35mV/mV, being higher than that achieved in the inductor-less case. In this specific case, $R_S = 0.65\Omega$ is the limit value under which is not possible for $V_{IN,MIN}$ to be further lowered, given that ng_{ds} is dominating the output



Figure 5.16. (a) Measured steady-state output voltage V_{OUT} as a function of source voltage V_{IN} with $L_S = 37\mu$ H $R_S = 0.65\Omega$: the slope is 35.3mV/mV, higher than the one obtained with load JFETs. The system can start from 32mV. Lowering R_S has not any effect since the output conductance of the CS stage is being dominated by ng_{ds} . (b) Measured V_{OUT} and P_{OUT} as a function of R_{LOAD} , with $V_{IN} = 32$ mV, $L_S = 37\mu$ H, $R_S = 0.65\Omega$. The optimum load resistance maximizing P_{OUT} is lower than 1M Ω , whereas higher load resistances maximize V_{OUT} [81]. (© 2015, Elsevier).

conductance of the CS stage. **Figure 5.16b** plots V_{OUT} measured with $V_{IN} = 32$ mV, n = 4, and an inductor with $L_S = 37\mu$ H and $R_S = 0.65\Omega$, for various values of load resistance ranging from 1M Ω to 50M Ω . A maximum voltage of about 800mV is achieved with a 50M Ω load. The output power decreases if the load resistance increases and, once again, the optimum load is shifted towards lower values of load resistance.

Considering the inductor, it is worth noting that it has a smaller size than the MTs adopted in conventional boost oscillators. To cite an example, the Coilcraft XFL2006 and LPO3010 series of inductors achieve inductances up to 100 μ H with package dimensions of 2×2×0.6 mm³ and 3×3×1 mm³, respectively. The Coilcraft LPR6235, one the the smallest available MTs with turn-ratios up to 1:100 has a 6×6×3.5 mm³ package. Furthermore, a single external inductor may be shared between the proposed boost oscillator and the main switvhing DC-DC converter. In addition, at higher packaging costs, a small inductor might be integrated at package level, as in power-supply-in-package (PwrSiP) devices [2]. Finally, miniaturized TEGs with footprint area as low as 2 mm² are also available [90].

5.5 Summary on the presented boost oscillator

The principal advantage of the presented model is the possibility of evaluating and sizing system components in the initial phases of system design, once the thermal gradients and the TEG charateritics are known. Furthremore, the model allows to optimize design parameters and to define the requirements for oscillation. To cite an example, it predicts lower start-up voltages if PTs with higher quality factors are used. The influence of variations of transistor parameters on the start-up voltage was found to be limited, and comparable with the mismatch between model predictions and measurements. However, these variations can be avoided with a custom IC design, leading the way towards the system integrability. In perspective, package-level integration of mixed microelectronic circuits and MEMS PTs can be devised. MEMS PTs can be implemented in areas as low as few mm² [91] [92]. Nevertheless, it is mandatory to place storage capacitors in the order of μF off-chip. For this purpose, thin film supercapacitors are already available for package-level integration [93] [94]. Conventional tiny SMD packages would also have a limited impact on area. The current requirements of the particular application put some constraints on the choice of the value of the storage capacitor. Generally, to cite an example, in order to sustain a single packet transmission of a wireless node, i.e. roughly tens of mA for tens of ms, several µF are necessary. Another critical component for integrability could be the inductor, however, in this specifica case a small inductance of few tens of μ H is required to improve circuit performance, as well in the external DC/DC converter, and commercial solutions in fooprint area less than 10mm² are already available.

The presented solution should be devised as a single building block of a more complex energy scavenging circuit. However , there are other design issues that designers have to deal with. As a first requirement, a sub- μ A voltage monitor should be implemented, with the purposes of: (i) activating the main efficicient power switching DC/DC converter, similarly to the circuits presented in [65] [66] [88], and (ii) of disabling the boost circuit, which could be accomplished by pulling the gate of the load JFET above its pinch-off voltage. Another challenge would be the design of a MPPT DC/DC converter able to operate with input voltages as low as tens of mV, as in [63]. Finally, in the inductor-based solution, a smart possibility is sharing the inductor with the DC/DC converter.

5.6 Custom Integrated boost oscillators

In perspective of increasing performances and shrinking dimensions, custom integrated boost oscillators were designed and fabricated in a 0.35um microelectronic process by STMicroelectronics. The schematic of the system is pretty much the same of that in **Figure 5.6**. Two different versions of the oscillator were designed: the first one (IC1, **Figure 5.17a**) is made up by an input stage composed by a classic common source stage with n-channel depletion MOSFETs (whose characteristic equations are similar to those of JFETs, given that a n-channel depletion MOSFET has a negative threshold). Both amplifier and load MOSFETs were equally sized, with a W/L =1.5mm/1.5µm. The second designed version (IC2, **Figure 5.17b**) of the oscillator is made up by an input stage composed by a NOT port composed by native (or natural) p-channel (for the pull-up) and n-channel mosfet (for the pull down), with an L=1.5µm and W_{pMOS} =4mm, whereas W_{nMOS} =16mm. Unfortunately the second version is not properly working even though SPICE simulations taking into account the parasitic capacitances and resistances, as well as the effective area of source and drain of all devices, show a perfect system operation.



Figure 5.17a,b: Designed integrated boost oscillators in 0.35µm technology by ST Microelectronics.

Figure 5.18 shows the measured waveforms of the system start-up for IC1. The system is able to self-start at 28mV in *inductor-less mode*, that is without an inductor in place of the load FET in the input stage of the oscillator. The output voltage in no-load condition, using a 4.7μ F capacitor, reaches about 3V which means a step-up ratio greater than 10^2 . This performance is achieved using a PT prototype made by Noliac and the lower capacitances obtained in the system allow to keep the minimum activation voltage at low values, as predicted by the developed mathematical model. Furthermore the high quality factor of the PT, allows using an additional capacitance of 400nF in parallel to its input port in order to increase its voltage gain without affecting its input impedance, thus validating the former assumptions concerning the optimization of the input capacitance.

Figure 5.19 shows the schematic of the oscillator IC2. The common source stage is replaced by a NOT port made up of native MOSFETs (that is without a doped channel, hence they have a lower threshold voltage compared to enhancement MOSFETs). The only external components are C_{PUMP} and C_{STORE} .

The main difference of IC2 compared to IC1 is that because of its higher loop gain, the output oscillation of the input stage can reach the linear dynamics of the NOT port, hence the oscillation can be more similar to a square wave instead of a sinusoid. Since the following PT acts like a band-pass filter, part of the energy can be filtered out. This implies that even though the open loop gain can be higher at higher input voltages for IC2, the output voltage across the storage capacitor can be lower, given that driving a PT with a square-wave is not an optimum solution.



Figure 5.18 Measured start-up waveform of output voltage vs. input voltage of IC1. The system self-starts at 28mV in inductor-less mode. The PT used is a Noliac prototype, furthermore a 400nF capacitance was used in parallel to the PT input port to increase its voltage gain without affecting the input impedance.



Figure 5.19 Schematic of the IC2 system. The common source is replace by a NOT inverter made up of natural MOSFETs.

The advantages of having a custom IC are many. First of all, the reduced value of the parasitic capacitances allows obtaining better performances in terms of minimum start-up voltage. As a matter of fact, IC1 (with no magnetic components) is able to start from a voltage that is lower compared to the same obtained with an implantation made up of discrete devices.

In addition the reduced size of the IC (few mm²), allows in perspective an integrated SoC if a MEMS PT is used. In this case, the kick-start system might be, in perspective, fully integrated together with the main power converter and the ultra-low power voltage monitor.

In addition an IC gives more design flexibility in terms of tuning of the ratio of the transconductances of the amplifier and load FETs in the common source stage.

5.7 A PT based oscillator circuit for energy harvesting applications

This paragraph gives an introduction about the utilization of piezoelectric transformers oscillators (PTs) as main devices for ultra-low voltage boost circuits for battery-less energy harvesting applications. The oscillator is able to start from voltages down to about 16mV, and to pump the output voltage up to 1.32V in a no load condition. Furthermore, the oscillator serves as kick-start circuit for a more efficient power conversion circuit. However, the whole circuit self-starts with an input voltage of about 30mV, and the maximum conversion efficiency referred to the maximum power point (MPP) is higher than 40%, with an intrinsic current consumption down to $1.3\mu A$. Figure 5.20 [95] presents the schematic view of the entire system. In the schematic, five different sections can be distinguished: the ultra-low voltage energy source, which can be a TEG, a photovoltaic cell, or any other low frequency energy source. The second section is PT based oscillator, in which a Noliac prototype with a mechanical quality factor $Q_M \sim 10^3$ has been used. The active device is MMBFJ270 p-channel JFET. In this case a pFET was used instead of a nFET in order to give the additional possibility to disable the oscillator when the main DC/DC power converter is enabled. The third section is the voltage monitor, the fourth section is a DCM (Discontinuous Conduction Mode) boost converter, and the fifth is the control circuit providing the control signal for the main power converter.

A tiny 40µH inductor L_{st} as load of the amplifier stage was used. The resistor connected to the gate of J₁ is then linked to the \overline{EN} signal of the boost circuit, which is maintained low during the whole kick-start phase, and pulled high when the DC/DC converter is enabled so that the pJFET channel is disabled. A voltage doubler made up with standard commercial BAS70 Schottky diodes rectifies and boosts the voltage on the start-up capacitor C_{stu} . The capacitor C_{OPT} increases the overall loop gain without affecting too much the PT input impedance, as we have seen before.

The voltage monitor circuit provides a steep slope voltage variation on its output node when the slowly varying voltage V_{stu} across the start-up capacitor C_{stu} goes beyond a certain threshold. This switching threshold is determined by the threshold voltage of M₂ plus the forward voltage drops of the diodes D₁ and D₂. In this particular implementation, the switching threshold is located in proximity of 1.5V.



Figure 5.20: Schematic of the proposed energy harvesting circuit, with PT-based start-up and power management circuitry [95]. (© 2015, IEEE)

The devices M_3 and M_4 were selected for never being conductive at the same time, at the relative low voltage operating conditions of this circuit. In addition, M_3 and M_4 were chosen in order for the logic threshold of the inverter M_3 - M_4 to be lower than the switching threshold of the voltage monitor. For the same reason, the diode D_3 as well was added.

The capacitor C_{ON} at the beginning has not any stored charge, and hence provides approximately 0V to the inverter M₃-M₄. When V_{stu} increases and exceeds the switching threshold, C_{ON} starts being charged with the same slope of V_{stu}.

As M_2 turns on, the inverter switches afterwards, because of its lower logic threshold. The capacitor C_f gives an additional noise margin immediately after switching, in order to prevent any other unwanted switching phases. As a consequence, the gate of M_1 is pulled down, and M_1 turns on. Given that in the initial phase the signal $\overline{EN} = 0$ V, M_5 is initially on. Then, the supply voltage V_{DD} of the DC/DC converter is enabled. In order for this to happen very quickly, it is necessary that the $C_{DD} << C_{Stu}$. Once the DC/DC converter is enabled, the transistor M_5 is turned off in order to completely exclude the start-up oscillator path.

Concerning the control circuit, it is supplied only when the voltage monitor detects a sufficient voltage on C_{stu} . It is composed of a fixed frequency (1kHz) and duty cycle (50%) square-wave oscillator which provides the PWM signal for the power converter, and of an enable circuit that manages the generation of the \overline{EN} signal. A STMicroelectronics TS881 comparator is used in the multivibrator because of its very low 200nA bias current and of its very low minimum supply voltage down to 1.1V. In addition, in order to reduce the power consumption, all resistors have relatively large values: $R_{1ast} = R_{2ast} = R_{3ast} = 22M\Omega$, $R_{ON} = R_{OFF} = 6.1M\Omega$. The switching hystheresis window is set by R_{1asb} R_{2asb} R_{3ast} , and in the presented implementation ranges from $V_{DD}/3$ to $2 \cdot V_{DD}/3$.

The control circuit also manages the generation of the \overline{EN} signal with the Boost Enable sub-circuit. In particular, it relies on the detection of oscillations on the control signal of the power converter. This is accomplished by a half-wave rectifier built with the diode D_{en} . The MOSFET M_{en} filters away low amplitudes below its threshold voltage. C_{en} is sized in order to provide a fast transition on \overline{EN} . When \overline{EN} changes from low to high, it almost follows V_{DD} . At its high voltage level, the start-up circuit is disabled, the supply of the control circuit is turned on, and the capacitor C_{ON} in the voltage monitor gets discharged, in order to allow the voltage monitor to enable the start-up circuit again, in case of shortage of input power.

In order to reduce the power required for control, the DC/DC converter is a boost switching converter with a constant duty-cycle as said before. This fixed duty-cycle does not represent an important limitation as long as the operating conditions of the low-voltage source are known and well defined: to cite an example, in a thermoelectric energy harvesting application, the available thermal gradients are usually defined, *e.g.* the difference between ambient and air vent temperature in a building, or between ambient and human body temperature. Based on this information, it is possible to correctly size the duty cycle of the converter. This is of course an acceptable trade-off with the intrinsic consumption of the converter, which is minimized.

The Load Enable network controls power distribution to the external application circuits. The load must be supplied only with suitable voltages or, alternatively, disconnected. The p-channel MOSFET M_{store} allows a very fast charge of C_{store} when V_{DD} rises above a minimum threshold voltage.

The presented circuit was characterized with additional measurements in a dual configuration: in the first one the main DC/DC converter is self-supplied and in the second one it was supplied externally. These measurements allow to evaluate the efficiency and the impact of power losses and intrinsic power consumption of control circuits when the power available from the source is in the micro-power range. In a first measurements session, the efficiency of the boost converter supplied externally with $V_{DD} = 5$ V was measured for different input voltages and for variable loads. In this specific case, the efficiency is intended as the ratio of the output power P_{OUT} transferred to an external load, with the power P_{AV} available from the source in the



Figure 5.21. Conversion efficiency of the power conversion circuit externally supplied, defined as the ratio between output power $P_{OUT} = (V_{STORE})^2 / R_{LOAD}$ and maximum available power from the source $P_{AV} = V_S^2 / (4R_S)$, with $R_S = 3.3 \Omega$ for different input voltages and different load conditions ($L_I = 1120\mu$ H, $f_{SW} = 1$ kHz, duty cycle = 50%), a) as function of the output voltage, b) as a function of the load [95]. (© 2015, IEEE).

maximum power point (MPP), where $P_{AV} = V_S^2 / (4R_S)$, with $R_S = 3.3\Omega$ as previously stated. Then, this definition of efficiency takes into account both power losses and inaccuracies in maximum power point tracking (MPPT). For each input voltage, the load was changed in order to have a given set of values of the output voltage. The results of this set of measurements are depicted in **Figure 5.21**. The above data have to be intended as an upper bound for the efficiency, given that the DC/DC converter is driven with a 5V voltage, which generates lower losses in the power MOSFETs than in the normal operation.

The efficiency with respect to the MPP was also measured when the power converter was self-supplied from the stored energy. With respect to the previous case, the higher power losses are due to the lower overdrive of power MOSFETs. Furthermore, intrinsic power consumption is also subtracted for supplying the control



Figure 5.22. Conversion efficiency of the self-supplied power conversion circuit, defined as the ratio between output power $P_{OUT} = (V_{STORE})^2 / R_{LOAD}$ and maximum available power from the source $P_{AV} = V_S^2 / (4R_S)$, with $R_S = 3.3 \Omega$ for different input voltages and different load conditions ($L_I = 1120 \mu$ H, $f_{SW} = 1$ kHz, duty cycle = 50%), a) as function of the output voltage, b) as a function of the load [95]. (© 2015, IEEE).

circuits. The achieved efficiencies are depicted in **Figure 5.22**. The achieved performance is pretty close to that obtained in micro-power harvesting circuits based on discrete components, as reported in the comparison presented in [32], where state-of-the-art converters starting from 20-40mV achieve efficiencies ranging from 40% to 61%.

Finally, the overall intrinsic power consumption P_{INT} of the control circuits during circuit operation was measured when the DC/DC converter was enabled. The results of the measures are depicted in **Figure 5.23**. A very low current consumption I_{INT} up to 1.3µA was observed. The corresponding intrinsic power is $P_{INT} = V_{DD}I_{INT}$. Then, the circuit is fully compatible with micro-power sources such TEGs or indoor photovoltaic cells.



Figure 5.23. Intrinsic power and current consumptions of the complete power management circuit for different values of the voltage on the storage capacitor, which were imposed by connecting a variable loads ($L_1 = 1120 \mu$ H, $f_{SW} = 1$ kHz, duty cycle = 50%) [95]. (© 2015, IEEE)

5.7.1 Summary on the presented harvesting scheme

The feasibility of PT-based start-up circuits was already demonstrated. During the measurements, a low-voltage source like a thermoelectric generator was emulated through a voltage generator with a series connected 3.3Ω resistor, accounting for both the TEG output resistance and DC inductance parasitic resistance. The input voltage was slowly increased starting from few mV until oscillation was triggered. No load was connected to V_{stu} in this set, and all the other circuit blocks were disconnected. The input voltage was increased starting from few mV until the oscillation was started. The circuit is able to oscillate with voltages down to 16mV; however the challenge is designing a power converter able to start to convert voltages down to 20mV.

To cite a comparison, the commercial LTC3108 self-starts from 20mV with a 1:100 MT. One of the key parameters in achieving such low activation voltage with the PT is its very high quality factor, which is $\approx 10^3$ in the reported case. This value is significantly higher than that of MTs used generally in start-up applications. The complete circuit was also fully tested. Once oscillation is triggered, the voltage monitor and the power converter were also found to be fully operational according to design specifications. In the complete circuit with two MMBFJ270 in parallel, given that the voltage monitor draws current from the start-up circuit, the minimum start-up

voltage that generates a sufficient steady-state output voltage (i.e. $V_{DD} > 1.7V$ in this implementation) is slightly increased to $V_{IN} = 30$ mV. However, we have also found that, once the start-up circuit is activated, if the input voltage is decreased oscillations are sustained down to 20 mV, given that the behavior of the oscillator is similar to a class AB amplifier, given that the current drawn by the oscillator is null for a portion of the oscillation period and, as a result, it is more efficient. It is important to remark that a custom integrated solution can allow achieving nanocurrents voltage monitors which imperceptibly affects the minimum required voltage to start an oscillation.

5.8 Summary

The chapter has presented a novel start-up oscillator based on piezoelectric transformer. The minimum activation voltage to trigger an oscillation was determined through the analysis and modelling of the circuit containing the linear model of the active devices and the electromechanical model of the PT around the resonance. The mathematical model was validated through a set of experimental measurements showing a good matching with the developed model.

The chapter presented also the designed ICs in an STM 0.35µm technology, which showed minimum activation voltages down to about 28mV, with output voltages up to 3V (in no load condition) without the aid of an additional inductor.

Furthermore the PT- based oscillator was used in a harvesting scheme (build-up with discrete devices), containing a voltage monitor, an astable multivibrator, and a main power converter with fixed switching frequency of 1kHz and duty cycle 50%. The PT-based oscillator served as kick-start system for the main power converter once a sufficient energy was stored on a storage capacitor, showing efficiencies up to 40%, in line with obtained values in discrete systems for energy harvesting purposes.

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Chapter 6

Design and fabrication of AIN MEMS Piezoelectric Transformers

This chapter presents an overview on the design, simulation and fabrication of AlN MEMS piezoelectric transformers performed in the clean rooms at the Technische Universität Wien (TUW) of Vienna (Austria) during the internship from February 2015 to August 2015.

As already discussed in the previous chapters, PTs are used for high-voltage applications (up to hundreds of V) and medium power applications (up to few W). In perspective of having more and more compact systems (PwrSoC), according to the MtM trend, it is possible to shrink dimensions of piezoelectric devices, without theoretically affecting performances, as instead it occurs in magnetic devices as extensively discussed in Chapter 2. However, MEMS piezoelectric devices, might be more sensitive to air damping, which is not predictable FEM simulations, hence the packaging might play an important role, not only concerning the compactness of the system, but also regarding the performances.

6.1 Theory, design and simulation of AlN PT membranes

The first step is the design aided by FEM simulations. In general, the simulation of high aspect-ratio structures requires a lot of computation and are time consuming. The frequency of the mechanical resonance of a membrane is given by:

$$f_{s,i} = \frac{1}{2\pi} \left(\frac{m_i}{R_2}\right)^2 \sqrt{\frac{K_m}{\overline{\rho}}}$$
(6.1)

where R_2 is the full radius of the membrane and m_i is a coefficient depending on *i*-th mode considered. **Table 6.1** gives the values of *m* for the first three modes. Furthermore K_m is named the *membrane bending stiffness*, it is homogeneous with the product of the Young modulus *Y* by the inertia moment I and generally it is expressed in N·m. K_m depends from both the mechanical constants of the device layer (Si -20µm of thickness) and from the active piezo layer (AlN - <1µm), but in this case, the AlN gives little contribution to the general mechanical properties. In **Equation** (6.1) $\bar{\rho}$ is the membrane equivalent mass given by:

$$\overline{\rho} = (t_{\rm si} \cdot \rho_{\rm si} + t_{\rm AIN} \cdot \rho_{\rm AIN}) \approx (t_{\rm si} \cdot \rho_{\rm si})$$
(6.2)

The approximation in (6.2) holds given that the equivalent mass (the product of the thickness t_{Si} and the mass density ρ_{Si}) of the Silicon device layer is much higher than that of the AlN. An approximation of K_m is given by:

$$K_{m} \cong \frac{Y t_{Si}^{3}}{12(1-v^{2})}$$
(6.3)

Y is the Young modulus, and v is the Poisson's ratio. **Table 6.2** gives some mechanical and piezoelectric properties of some materials. Generic PZT values are reported as well just for comparison purposes.

2

2

Widde	1	2	5
m_i	3.1962	6.3064	9.4395
Table 6.1: val	lues of m_i for the resona	nce of a membrane for the	first three modes
Material	AlN	Si (Isotropic)	PZT
$\rho (\text{kg/m}^3)$	~3300	2300	7800
Y_{33} (GPa)	360	165	50-70GPa
v	0.24	0.22	~0.35
E33	~9	11.9	$\sim 10^{3}$
$d_{33}(\text{pm/V})$	~5.5	-	200-600
$d_{31}(pm/V)$	-1.73	_	-100300

1

Mode

Table 6.2: Electronic, piezoelectric and mechanical properties of AlN, PZT and Si.

The PZT, as it can be noted, is a material with a stronger piezoelectric effect than the AlN, however it is not an IC compliant material because of the presence of the lead. Equation (6.1) allows the simulation of devices with reduced aspect ratio. If the radius R_s of the simulated structure is $10^{1/2}$ smaller, then the obtained resonance frequency, will be ten times higher than the expected.

Six different devices were designed and simulated: the smaller devices such as the TR06, TR07, TR08 and TR09, have a diameter of 3.2mm (hence radius of 1.6mm) were directly simulated in 2D axisymmetric mode. To cite some examples, TR07 means that the radius of the primary electrode is 70% (0.707) of the whole membrane radius, thus input capacitance and output capacitance have the same value. TR08 has the radius which is 80% (0.8) of the whole radius and so on. However TR06, TR07, TR08 and TR09 will have the same mechanical branch (the difference of size of electrodes will affect imperceptibly the mechanical resonance). These devices have only three electrodes as shown in **Figure 6.1a**.

The other two designed devices FCM (Fully Clamped Membrane) and FSM (Free Standing Membrane) have a diameter of 6.4mm (thus a radius of 3.2mm) and have a "segmented" secondary electrode (outer circular crown at bottom electrode level and top electrode level) as shown in **Figure 6.1b** (for simplicity only 4 segments are shown). The segmentation in k parts will provide k output ports. Thanks to the symmetry of the structure, the voltage across each output capacitance is the same; hence they can be connected in series in order to boost the output voltage of k times (the bottom electrode "SEOCOND.2" is in short circuit with the top electrode with the same name)



Figure 6.1: Top view and cross section of the TR devices and FCM (FSM) devices.

The difference between FCM and FSM, is that in the latter, the membrane is anchored via a series of "arms", whereas in the former, the membrane has its whole border anchored.

With a membrane of 6.4mm of diameter (3.2mm of radius), the fundamental mode will have a resonant frequency of 7.83kHz, however this result takes into account, for simplicity purposes, only the resonance frequency of the Silicon. Furthermore the metallizations are not considered in the analysis. However, their impact is in general negligible because of their thickness.

We have seen in the fifth chapter that the output capacitance of a discrete PZT-based PT is in the range of 20pF. As a matter of fact, the lower the output capacitance, the higher the PT output gain we will obtain. But a very low PT output capacitance will be much more sensitive to capacitive loads; hence it was decided to have an output capacitance around 10pF, in order to keep it at least one order of magnitude higher than that of a pad of a custom integrated circuit. 1 mm² of AlN has a capacitance of about $C_{AIN}=80$ pF·µm. In order to have a larger output voltage, we can segment the output electrode, in order to sum *n* times the same voltage. Assuming that the AlN thickness is 1µm and that *n*=12 (hence the output capacitance will be divided by a factor n^2) and that surface is equally divided in two parts (that is to say output capacitance and input capacitance have the same value), we find that the membrane radius has to be around 3.5mm. However, given that the wafers available
for the fabrication were 4-inch diameter wafers, and that they were shared in a MPW (Multi-Project Wafer), in order to have the same die dimensions, and thus simplifying the dicing process, the radius of the membrane was lowered to 3.2mm. Hence in FEM simulations, the radius of the membrane was set to $3.2/10^{1/2}=1.01$ mm, in order to have a lower aspect ratio membrane and hence speeding up the simulation, which was necessary to optimize the size of electrodes.

Figure 6.2 shows the first fundamental mechanical mode of a membrane with $20\mu m$ of device layer, $2.7\mu m$ of AlN and radius of 1.6mm. The electrodes are not modelled. The mode is placed at 38.443kHz, hence the electric resonance will be placed around this frequency.

Generally in literature, the optimization of the electrodes is made according to the sign of the stress in order to maximize the power [90], however in order to maximize the output voltage, the output capacitance should be decreased whereas the input capacitance should be increased has shown in the fifth chapter. Hence the TR09 device intuitively has higher step-up ratios compared to the TR06 device. This is confirmed by FEM simulations as well.

6.2 Other MEMS IC-compatible techniques

6.2.1 Spin coating

The spin coating technique is the most common technique used to provide a coating on the substrates with few ml of photoresist onto the substrates rotating at a speed between 2000 and 4000 rpm. One of the advantages of the spin coating technique is that it provides a very good homogeneity of the resist film thickness over the whole wafer, as well as a very high smooth film surface.

Another advantage is that the film thickness is inversely proportional to the rotating speed of the wafer, hence the film thickness can be modified by properly trimming the rotating speed. One of the main drawbacks of this technique, is that it is not efficient (efficiency less than 5%), this means that most of the deposited resist is lost during the spinning in order to achieve the desired thickness, furthermore it cannot be used on surfaces which are not "flat".



Eigenfrequency=38443.221748+1498.589529i Volume: Total displacement (m)

Figure 6.2: Fundamental mechanical mode of a membrane with 20µm of device layer, 2.7µm of AlN and radius 1.6mm.

6.2.2 Spray coating

The spray coating technique is used to provide a coating on the substrates with via the deposition of millions of μ m-sized resist droplets. These resist droplets are deposited on the substrate by an air stream, where they stick to the surface, and from a thin resist film. The air stream is used given that the free fall in atmosphere would take too much time for the film to be formed.

6.2.3 Etching

The etching is the technique that allows to perform an attack of substrates in order to obtain well defined structures in *bulk micromachining* processes (that are processes in which devices are obtained within the wafer, on the contrary *surface micromachining* processes rely on the production of the devices on the surface of the wafer). There are two types of etching: wet etching and dry (or plasma) etching.

The wet etching technique is a pure isotropic chemical process that is isotropic etch in amorphous materials such as SiO_2 (silicon dioxide) or it can be also anisotropic in crystalline materials such as silicon, depending on the orientation of the crystals. Contaminants in this type of technique are dependent on the chemical purity and chemical system cleanliness. In general, agitation of the wet chemical bath is used to aid the movement of reactants and to speed up the reaction process. Agitation

can be made by simply putting a small magnetic cylinder rotating in the solution while the etchant solution is heated (in order to have a faster attack rate).

Agitation also aids etch uniformity because it removes the eventual presence of gases formed during the heating process. A good wet chemical workbench will have agitation, temperature, and time controls as well as filtration to remove particulate and contaminants.

As previously stated, wet-etching methods can also be used on crystalline materials such as silicon to achieve directional etch profiles. For example, a typical anisotropic etchant for the silicon is the potassium hydroxide (KOH), which etches two orders of magnitude faster in the (100) plane than in the (111) plane. Certain material such as the silicon dioxide or nitride can be used as "etch stops", that is a barrier that will not allow the etching to continue. In fact, in MEMS processes, the BOX (buried oxide) placed between the silicon device layer and silicon handle layer in SOI wafers, stops the front etching. In case there are not any etch stops in a wet etching process, one option to achieve a specific etch depth is a timed etch. However, this requires that the etching rate of the etchant in the particular material that is wanted to be etched, should be well known and defined, furthermore a timed etch is extremely difficult to control accurately.

6.2.4 Evaporation

The evaporation is a deposition technique. In general it is used for deposition of metals. Compared to the sputtering technique (see first chapter) it is slower, but structures present a more defined shape. For the evaporation technique, the wafer is placed in a very high vacuum chamber at room temperature with a melting pot containing the material that has to be deposited. A heating source is used to heat the melting pot which causes the evaporation of the material and condense on all exposed cool surfaces of the vacuum chamber and substrate. The process is typically performed on one side of the substrate at a time. The most diffused sources of heating are: E-beam, Resistive heating, RF-inductive heating. In some systems the substrate/wafer can be also heated during the process in order to alter the composition or stress of the evaporated metal.

6.3 Fabrication of AIN piezoelectric transformers

This paragraph gives in more detail, the fabrication process of AlN piezoelectric transformers at TUW- Vienna.

6.3.1 Photolithography

This Section briefly summarizes the photolithography technique useful for the definition of metal layers.

6.3.1.1 Photolithography in detail

The process starts with the deposition of 1.8ml of AZ5214E (from Microchemicals) image reversal photoresist on the wafer at 3000rpm. The wafer is an SOI wafer with 20µm of device layer and 350µm of handle layer. Between the device layer and the handle layer there is a 1µm thick layer of BOX (buried oxide).

The wafer is then baked at 107° C for 5 minutes. This first baking (prebake) is necessary because the formed film on the wafer's substrate has a remaining solvent concentration. The partial elimination of this solvent by the *softbaking* leads to:

- Avoid the mask sticking to the wafer during the exposition process,
- Improve the resist adhesion to the wafer's substrate,
- Allow multiple coating without having any impact on the previous deposited resist films.
- Prevent the formation of bubbles by the remaining evaporating solvent during the successive high-temperature processes such as evaporation or sputtering of metals.
- Increase the softening point (that is the temperature beyond which the resist profile and edges start to be smoother) of the resist for the subsequent high-temperature processing steps.

After the softbaking, the wafer again is put on the spin coater, and 2ml of AZ Aquatar (from Microchemicals) is deposited on the wafer surface. The AZ Aquatar is a top layer anti-reflective coating. This solution behaves like an optical coating at the interface between the photoresist film and air, improving the image contrast. Multiple reflections within the photoresist are also suppressed. Furthermore the use of

Aquatar lowers the probability of sticking of the mask on the wafer. After the Aquatar deposition, the wafer is put again on the hot plate at 107°C for 30s.

6.3.1.2 Exposure

The processing of the wafer continues with exposition of only 2s at UV light in hard contact mode (this means there is not any gap between the wafer and the mask). In general mask aligners with Hg sources have an emission spectrum between 365nm and 435nm, and the absorption spectrum of the photoresist is matched for this small wavelengths band.

6.3.1.3 Reverse Baking (Hard-Baking) and flat exposure

The subsequent step is the reverse baking at 120°C for 120 seconds. This step is required only for image reversal photoresists. With this hard-baking, the image provided by the mask is reversed, hence the unexposed part of the resist will be developed during the developing process. After the reverse baking a flat exposure under UV light of 30s has to be performed.

6.3.1.4 Developing

The last step of the photolithography is the developing step performed with Nitrogen for 60s. Developers are liquids which eliminate the exposed part of positive photoresists or the unexposed part of negative (or image reversal resists) from the wafers substrate.

Figure 6.3 shows a detail at the optical microscope of the upper part of the piezoelectric transformer after the first photolithography.

6.3.2 Top electrode deposition

Once the pattern is obtained on the wafer after the developing step, the metals constituting the bottom electrode can be evaporated. At this point the choice can be evaporation or sputtering, it would make almost not any difference. Although the sputtering process is much faster than the evaporation (for the evaporation it takes almost 24h in order to create the vacuum inside the chamber), it requires that all the



Figure 6.3: upper part of the lithography for the bottom electrode deposition

needed targets are placed inside the sputtering machine chamber, so the evaporation is preferred.

In our case the bottom electrode is made up of three different layers: 50nm of Chromium as adhesive promoter, 550nm of Copper, and 100nm of gold. Titanium as well can be used as adhesive promoter for the upper metals, but since this metal is used as hard mask for AIN patterning, during the etching process the bottom electrode could be removed by the phosphoric acid (H_3PO_4) and hydrofluoric acid (HF).

6.3.3 Top electrode patterning

After the evaporation is performed, the wafer is put for about 12h-24h in a bath of acetone ((CH₃)₂CO) in order to perform the lift-off of the unwanted parts of metals. After this first bath, then the wafer is put in a second (cleaner) ultrasound acetone bath for few minutes. A third bath of much cleaner acetone is used again for few minutes together with an ultrasound bath. The last step requires a fast bath of isopropanol ((CH₃)₂CHOH) in order to wash away the last residues of resist and acetone. At the end the wafer can be put in the wafer cleaner in order to not make the isopropanol dry on the wafer surface. **Figure 6.4** shows a detail at the optical microscope of the upper part of the piezoelectric transformer after the bottom electrode deposition and patterning.



Figure 6.4: Bottom electrode after deposition and patterning.

6.3.4 Titanium Hard Mask photolithography

The subsequent step is Titanium Hard Mask photolithography using the AZ5214E image reversal photoresist. The AlN is patterned through the lift-off technique. However, if the photoresist is used, because of the very high temperatures involved during the AlN sputtering (temperatures up 130°C), the resist can change its properties and the AlN lift-off would not work properly. So a photolithography is made in order to pattern to titanium that will be used as mask for the AlN lift-off. **Figure 6.5** shows a detail at the optical microscope of the upper part of the piezoelectric transformer after the photolithography for the titanium hard mask.

6.3.5 Titanium evaporation and lift-off

After the photolithography, a layer of 400nm of titanium (AlN inverted mask) is deposited on the wafer through the evaporation process. The choice for the technique of the Titanium deposition falls on the evaporation instead of the sputtering, because with sputtering the titanium adhesion on the wafer is much higher, and the evaporation can avoid some titanium residues on the wafer.

After the Titanium deposition, the wafer is put on the acetone and isopropanol baths in order to pattern the titanium mask. Figure 6.6 depicts a detail at the optical



Figure 6.5: Lithography for the Ti hard mask. The light green shows the area where there is not any resist and hence in that area the AlN will be lift-offed through the TI in order to obtain a FSM device.



Figure 6.6: Ti hard mask patterned with photoresist.

microscope of the upper part of the piezoelectric transformer after the titanium hard mask patterning.

6.3.6 AIN Sputtering

The sputtering machine used for the process is a Von Ardenne LS 730s. The AlN is put on the wafer holder and then inserted into the chamber. The sputtering process takes about 40 minutes for an AlN thickness of 500-600nm. From a theoretical point of view, in order to avoid short circuits between top and bottom electrodes, the AlN thickness should be bigger than that of the bottom electrode. However, by several

tests and five SOI wafers with top and bottom electrode in short circuit, it was found out that neither with a factor two between the bottom electrode thickness and the AlN thickness it was possible to avoid short circuits. With a factor 3.5 (2.5μ m), no short circuit was found. The AlN was sputtered in 4 different steps (900nm, 600nm, 500nm, 500nm) in order to avoid too much high temperatures, which could have caused a bad adhesion and delamination of the AlN film. Furthermore the AlN is transparent. **Figure 6.7** shows a crack of the AlN after the deposition process due to an excessive residual stress in the layer. In general, the higher the thickness, the higher the residual stress. The values of the piezoelectric strain coefficients of the sputtered AlN match pretty well with those given in literature [96].

6.3.7 Titanium protective mask photolithography, sputtering and lift-off

At this point a new photolithography is performed in order to obtain a titanium protective mask of 400nm, after the AlN sputtering and lift-off process, that is the dual of the previous AlN inverted mask. In this case the titanium is sputtered because the sputtering compared to the evaporation has a higher coverage profile, and this can be useful in case of misalignment of the two dual titanium masks. After the photolithography, the titanium is sputtered, and then the lift-off process defines the patterns of the titanium protective mask. **Figure 6.8** depicts a detail at the optical microscope of the upper part of the piezoelectric transformer after the upper titanium mask patterning.

6.3.8 Etching with H₃PO₄ and HF

The following phase is the patterning of the AlN, that can be considered a combination of both etching and lift-off technique. At the beginning, the AlN is attacked by the phosphoric acid (H₃PO₄), which has the task of making the Exposed AlN parts more rough and porous. The H₃PO₄ is heated at temperatures higher than 80°, because the acid attack rate is higher. When, about after 50s-60s, the AlN surface appears "milky", the wafer then is put in a 40% HF for less than 10s, which penetrates through the roughness of AlN caused by the phosphoric acid, and dissolves the titanium beneath the exposed AlN, making the patterning of the AlN via a lift-off



Figure 6.7: AlN crack in a device after the deposition. On the eelctrodes, the AlN has a bad adhesion, hence the probability of crack or delamination in this zone is high.



Figure 6.8: Wafer covered with a second layer of patterned protective Titanium. On the darker brown area, the Ti has been lift-offed, hence the AlN is exposed in this zone.

process. For further details in [97] an extensive explanation of the etching of AlN with H_3PO_4 can be found.

Figure 6.9 shows a detail at the optical microscope of the upper part of the piezoelectric transformer after the AlN patterning.



Figure 6.9: AlN patterned.

6.3.9 Top electrode photolithography, metal evaporation and lift-off

The subsequent step requires the top electrode photolithography, metal evaporation of 50nm of chromium as adhesive promoter, 500nm of copper and 150nm of gold with the litf-off in the acetone and isopropanol baths. In this case as well, the metal evaporation is preferred, because the sputtering requires the contemporary presence of the three targets in the sputtering machine. **Figure 6.10** shows a detail at the optical microscope of the upper part of the piezoelectric transformer after the top electrode patterning.

6.3.10Front etching mask photolithography and front etching

This step requires the use of a positive resist, the AZ6624 (from Microchemicals), because the designed mask was a dark field type (this means the chromium on the mask is placed where we want the resist to remain as a protective layer). The receipt for the photolithography is almost the same as the one of AZ5214E image reversal photoresist, with the exception that there is not the reverse baking. In order to have a very thick protective layer, the AZ6624 is spinned and soft-baked three times, before the 2s UV light exposure. This is because, slowing down the rotating speed of the



Figure 6.10: Top electrode deposited and patterned.

wafer, in order to obtain a thicker layer, would not have produced a homogeneous resist film.

The etching of the silicon device layer, then is performed using the RIE (Reactive Ion Etching) machine. **Figure 6.11** shows a detail at the optical microscope of the upper part of the piezoelectric transformer after the front side etching.

6.3.11Spray coating, backside etching mask photolithography and backside etching.

The subsequent step requires that the wafer is coated with a very thick protective layer of the resist on the top side, where the front etching has been performed. This step is mandatory given that in order to perform the backside etching, the wafer must be placed upside down, with the front side touching the vacuum chuck holder. In this case the spin coating is not usable, because of the deep dig due to the previous front side etching.

After the front spray coating is performed, the wafer is put on the vacuum chuck holder of the mask aligner. In this case, the alignment of the last mask is trickier, because the alignment markers are placed on the top side of the wafer at the bottom electrode level. After the backside etching mask photolithography is performed, the wafer is put on the DRIE (Deep Reactive Ion Etching) machine in order to etch the



Figure 6.11: Front side etching (brown areas).

350µm of the wafer handle layer. After the handle layer etching is performed, the wafer has to be handled with a lot of care, since from now on it is more fragile.

6.3.12 Spray coating, backside etching mask photolithography and backside etching.

The subsequent step requires that the wafer is coated with a very thick protective layer of the resist on the top side, where the front etching has been performed. This step is mandatory given that in order to perform the backside etching, the wafer must be placed upside down, with the front side touching the vacuum chuck holder. In this case the spin coating is not usable, because of the deep dig due to the previous front side etching.

After the front spray coating is performed, the wafer is put on the vacuum chuck holder of the mask aligner. In this case, the alignment of the last mask is trickier, because the alignment markers are placed on the top side of the wafer at the bottom electrode level. After the backside etching mask photolithography is performed, the wafer is put on the DRIE (Deep Reactive Ion Etching) machine in order to etch the 350µm of the wafer handle layer. After the handle layer etching is performed, the wafer has to be handled with a lot of care, since from now on it is more fragile.

6.3.13BOX etching, Backside Spray coating and dicing

Figure 6.12a and **6.12b** show the top and bottom view respectively of the final free standing membrane. Sometimes the copper beneath the gold can oxidize during the last cleaning phase.

In order to obtain the final devices, after the backside etching, at the end of the process the wafer is put in a solution of 5% HF, in order to eliminate the 1µm BOX (buried oxide beneath the device layer), and so having free moving devices. After this, the wafer is put again on the spray coating machine, in order to have a thick protective resist film on both the backside and frontside (the 5% HF eliminated the previous protective film on the wafer top side), in order to protect the devices from the water flux cooling down the dicing machine blade. After the spray coating, the wafer is put in the dicing machine and then diced, so having the final dies. At the end of the process, each device is cleaned in a solution of acetone and isopropanol, in order to eliminate the last residues of protective photoresist. A last cleaning phase requires the oxygen plasma (as known as plasma cleaning) performed in the RIE machine.

Figure 6.13a and **6.13b** show an example of other fabricated devices: the **FC** (Fully Clamped) membrane and the other smaller 3-pin piezoelectric transformer with different ratios between the input and output capacitance (TR06...TR09). The FC and FSM present the same layout with the difference that in the FSM, the membrane is anchored by twelve arms, as stated before. Furthermore in **Figure 6.13b** the primary and secondary segmented electrodes were highlighted.

6.4 Reliability of the process

Some problems arose during the process in addition to the AlN crack in some devices. The process started with six SOI wafers, but only the last wafer showed working devices. A couple of wafers broke during the processing, in particular after the front and backside etching given that the wafers become more fragile.



Figure 6.12a,b: Example of a FSM (Free Standing Membrane) device. The device is anchored to the support through a series of arms. The dashed red square indicates the part depicted in the pictures 6.3 to 6.11.



Figure 6.13a: small 3-pin PTs. The main difference between them is different input and output capacitance. **Figure 6. 13b:** FCM device, "be" stands for bottom electrode, the output capacitance has been segmented in order to achieve a higher output voltage by connecting in series the segmented output capacitances.

The devices of the other wafers, showed systematically short circuits between the bottom and top electrode. Intuitively, in order to prevent such short circuits, the AlN should be theoretically a little bit thicker than the bottom electrode. **Figure 6.14** shows this concept.

During the process a factor two between the AlN thickness and the bottom electrode's one was chosen but this was not still sufficient to prevent short circuit. The short-circuits found had a resistance lower than 4Ω , suggesting that pin-holes (cfr. Figure 6.15, a Scanning Electron Microscope – SEM - image showing one of the small spread holes on the AlN surface) were not the main cause of the



Figure 6.14: The AlN thickness is lower than the bottom electrode's one. The top electrode gets in touch

with the bottom electrode causing a short circuit.



Figure 6.15: SEM image of a pin-hole in AlN layer

short-circuit. This was due to the fact that the AlN profile due to the sputtering is more round in correspondence of the step BE/AlN.

Figure 6.16 shows another SEM image of the step in correspondence of the stack BE/AlN/TE. As it can be observed in the picture, the AlN is not continuous, hence the TE and BE are in touch.



Figure 6.16: SEM image of the step. Left: zone analysed. Right: zoomed image.

6.5 Mathematical models of the fabricated devices

In order to test the fabricated device, the electro-mechanical model had to be extracted. However, because of the lower quality factor compared to discrete PTs, the admittance circle method is not applicable given that there is not any phase inversion of the imaginary part of the device input admittance. So, the values of the input admittance (with output port in short circuit), together with the input capacitance C_{IN} where recorded through an Agilent E4980A LCR meter; then the values of the parameters of the mechanical branch were numerically estimated through several iterations, until the measured and estimated input admittance matched within a certain range. Figure 6.17 shows the measured magnitude and phase of the input admittance, as well as the admittance circle for the TR09 device, together with the numerically interpolated values of $C_M L_M$ and R_M reported in Table 6.3. The value of N was estimated trough the measured PT gain at a certain frequency, whereas the R_P parasitic series resistance was introduced in order to match the phase of the input admittance. Figure 6.18 depicts the equivalent electromechanical circuit of the measured samples (TRxx) around the fundamental resonance. A capacitance C_{PAR} was introduced in order to model the capacitive coupling between the primary and secondary electrode. As it can be observed by the figure, the capacitance C_{PAR} introduces a 3rd resonance in the system, as a matter of fact, the new mechanical branch considering the effect of C_{PAR} shows a maximum at the frequency:

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Figure 6.17: Measured vs. interpolated input admittance for the TR09 device.



Figure 6.18: a) Equivalent electro-mechanical circuit. b) Different representation of the same circuit.

$$f_{p2} = \frac{1}{2\pi \sqrt{L_M \frac{C_M C_{PAR}}{C_M + C_{PAR}}}}$$
(6.4)

Parameter	TR06	TR07	TR09
C_{IN} (pF)	~84.46	~134.44	~136
$C_M(\mathbf{pF})$	0.124	0.1534	0.16
$R_M(\mathbf{k}\Omega)$	540	357	390
$L_M(\mathbf{H})$	131.2576	95.41	99.244
C_{OUT} (pF)	160.95	130.92	57.12
N	1.4	1.52	2
C_{PAR} (pF)	~0.52	~0.4	~0.5
$R_P(\overline{\Omega})$	70	80	90
	1 7 8 0 1	1 . 1	

 Table 6.3: TR06, TR07 and TR09 electromechanical parameters

This means that at f_{p2} the voltage gain shows a minimum due to the presence of the two zeros introduced by the presence of C_{PAR} . The two zeros will produce 0° degrees of phase shift for frequencies slightly higher than the electric resonance of the device, as depicted in **Figure 6.19**. The maximum phase shift of slightly less than 160° in the voltage gain was observed as well, hence validating the presented model. For these devices the quality factor is around 60, that is to say one order of magnitude less than the discrete ones. This is mainly due to the air surrounding the device which increases the damping, lowering the maximum displacement of the membrane.

Figure 6.20 and **Figure 6.21** show the input admittance together with the admittance circle for the TR06 and TR07 devices respectively. Unfortunately there was not any instance of the TR08 device available.







Figure 6.20: Measured vs. interpolated input admittance for the TR06 device.



Figure 6.21: Measured vs. interpolated input admittance for the TR07 device.

In **Table 6.3**, the only parameter that differs from theoretical values is the input capacitance of the TR09 device that should be around 200pF.

Concerning the bigger devices, no working FSM device was available, hence only the FCM device was tested. The tested sample has a poor quality factor, around 12, mainly because a bigger membrane is more subject to air damping compared to a smaller membrane, given that the bigger one has lower frequency resonance.

Figure 6.22 shows the magnitude and phase of the input admittance together with the admittance circle for the first mode. Since the quality factor is poor, the admittance circle does not represent a closed form. The resonance is placed around 7.43kHz as predicted by **Equation (6.1)**, however at this frequency the device behaves almost like a pure capacitance.

Figure 6.23 depicts the input admittance as well as the admittance circle for the 2^{nd} mode, placed at around 36.67kHz (in accordance with theory and FEM simulations), of the tested sample. In this case the quality factor is much higher, around 216, however the matching with a pure Butterworth-Van Dyke network is lower. Intuitively, as it can be seen from the measured graph, it seems that beyond the resonance frequency, the mechanical capacitance doubles, whereas the inductance halves. For this device the voltage gain is pretty low, furthermore the spread capacitances between the primary and each part of the segmented secondary electrode does not allow the classic PT behaviour in terms of phase shift.



Figure 6.22: Measured vs. interpolated input admittance and admittance circle for the 1st mode of the tested FCM device.



Figure 6.23: Measured vs. interpolated input admittance and admittance circle for the 2nd mode of the tested FCM device.

Table 6.4 shows the parameters of the equivalent electromechanical model for both the 1^{st} and 2^{nd} mode of the tested sample.

Parameter	1 st mode	2 nd mode
C_{IN} (pF)	~597	~640
C_M (pF)	0.407	0.5
$R_M(\mathbf{k}\Omega)$	4318.2	40
$L_M(\mathrm{H})$	1121.3	37.49
C_{OUT} (pF)	65.12	65.12
N	4.7	4.7
$C_{PAR}(\mathbf{pF})$	-	-
$R_{P}\left(\Omega ight)$	50	50

Table 6.4: FCM device electromechanical parameters for 1^{st} and 2^{nd} mode.

6.6 Summary on MEMS PTs

This chapter has presented the modelling, design, simulation, realization and characterization of AlN-based membrane Piezoelectric Transformers. For the realization of the PTs on a SOI structure a six mask process was used and 100% compatible with IC techniques.

Among the six processed wafers, only one wafer showed working devices because of short circuits between top and bottom electrodes, and cracks on the AlN.

The lumped equivalent circuit was extracted through iteration and it showed a quality factor of ~ 60 for the TR devices. The low value of the quality factor is affected by air damping. Furthermore the capacitive coupling of primary and secondary port, does not allow reaching 180° degrees of phase shift.

As extensively discussed throughout the dissertation, MEMS PTs, with shrunk dimensions, can be theoretically used in boost oscillators in EH schemes in place of MTs, given that sufficient quality factor (enhanced with a vacuum package) and higher step-up ratio (investigating the possibility of more interleaved layers at the primary side) is provided. DC/DC converters with discrete PTs are possible as shown in [54], however in certain application fields in which the global efficiency is the main target, an inductor might be still necessary because controlling the PT input port with a square-wave is not the optimum solution in terms of efficiency. According to the target output power, PTs can be shrunk down to small volumes (several mm³), without encountering saturation issues as instead it happens for miniaturized magnetic inductors and transformers (cfr. Chapter 2).

Another possible application of MEMs PTS could be resonant step-down converters, which can have higher efficiency thanks to the higher Q factor of piezoelectric devices compared to magnetic components.

Another advantage of MEMS PTs compared to the magnetic counterpart, is that they can provide a true signal or power isolation, without EMI. As a matter of fact, the magnetic field of an inductor might couple with the low-resistance substrate of CMOS technologies, thus inducing currents that can cause also latch-up in the IC and an unexpected circuit operation [31].

The major issue with MEMS PTs, is the air-damping which limits the maximum displacement of devices, and hence the available power. However, this is a limit not linked to the piezoelectric technology (like the saturation in magnetic devices, which limits the linear behavior of the component), but rather a packaging issue (a vacuum package might partially remove the damping due to the surrounding air, improving the overall performance).

Chapter 7

Conclusions and future works

This thesis has faced the problems of miniaturization of magnetic and piezoelectric devices mainly for ultra-low power and ultra-low voltage applications such as EH systems, in perspective of having PwrSoC and PwrSiP.

Thanks to technology improvements, which lead to the decrease of switching frequencies, the miniaturization of magnetic devices is possible, however efficient power systems must always rely on the presence of a magnetic core, even if the value of the inductance required is so low, that even air-core inductors might be theoretically suitable.

Nevertheless, the presence of a magnetic core can significantly limit the working interval of the device, either because of the saturation of the material or because of the minimum working frequency. Furthermore, not all the magnetic materials that can be deposited are fully clean-room compliant because of potential issues of contamination.

Many works in literature present innovative magnetic devices (inductors or transformers), in very small footprint areas, however very few works provide some information in order to assess the effective performances of the device once this is placed as an energy conversion transducer in a power system.

The work in this thesis has shown that for a planar square toroid inductor, there is a maximum value of the achievable inductance per unit area that cannot be exceeded once the thickness of the core, linear turn density, and the material (hence the magnetic permeability) are fixed.

In addition, with the shrinking of dimensions, some very critical parameters must be taken into account and the effect should be further investigated in order to assess how they can affect the operation of device. To cite an example, the minimum working frequency is directly linked to the voltage across the inductor and to the cross section of the core. Generally, the voltage is dictated by the application constraints, whereas the core thickness by the particular technology used to deposit and pattern the magnetic film. This entails that the core width (and hence the footprint area) must have a minimum value in order to fulfil the particular application.

Furthermore the intrinsic presence of the current turns in inductors and transformers as well, is a limit that puts an important trade-off between miniaturization and performance. Miniaturizing a magnetic inductor means also decreasing the cross section of the current turns, thus increasing the DC resistance, lowering the low frequency quality factor.

As a consequence of these considerations, instead of trying to further shrink dimensions of magnetic devices, a better solution might be exploiting the available footprint area as much as possible, by maximizing the inductance value or the performances. Until new magnetic materials are discovered, inductors and transformers cannot be further shrunk, if the particular application constraints of a PwrSoC (power, voltage, efficiency) have to be taken into account. The maximization of the inductance value can be based on optimization of classic shapes such the square toroids, or through the development of new shapes, such as the serpertine toroid as explained in this dissertation.

Concerning the piezoelectric counterpart, the miniaturization provides theoretically minor issues. First of all, in piezoelectric devices, like PTs, the absence of saturation phenomena (in a first approximation when the device is working within the linear range of the Hooke's law) linked to the volume of the device eliminates a major limitation to the miniaturization as it happens for inductors and transformers. Furthermore the absence of current turns can provide more compact systems and lower profiles.

In addition, the electro-mechanical conversion is much more efficient compared to the electromagnetic conversion. This has been extensively demonstrated in Chapter 5, by showing a novel boost oscillator based on a PT, suitable for EH schemes, which is the dual of the Armstrong oscillator based on a MT: using a dedicated IC designed in a 0.35µm technology provided by ST Microelectronics, it was possible to step-up ultra-low voltages down to 28mV, using a Noliac PT prototype, and no magnetic components. Nevertheless, it is worth noting that this value can be further lowered, if the devices in the input stage of the common source are mismatched, as extensively demonstrated through the developed mathematical model. The achieved value is compatible to the one obtained with commercial solutions.

However discrete PTs are designed for handling powers up to few W and output voltages of several hundreds of V, and are not optimized to handle powers in the range of hundreds of μ W and output voltages up to few V. This means that PTs can be arbitrarily shrunk down to fem mm³ with a tailored design, because of the absence of the aforementioned saturation phenomena linked to the volume of the device. This means that potentially with MEMS piezoelectric technologies it might be possible to extend the MtM trend.

However, as already discussed in Chapter 4, the number of interleaved layers at the primary side of a PT, plays the same role of the turns ratio of a MT. Nevertheless, MEMS processes are not intended for the deposition of multiple layers (generally only two levels of metallizations are available, whereas in standard CMOS processes more than six levels are possible) hence the possibility of extending the process to multiple AlN/Electrode layers, in order to enhance the voltage step-up ratio of the transformer, should be further investigated.

Concerning the presented MEMS AIN PTs, the parasitic capacitance between primary and secondary does not allow the PT to reach the 180° degrees of phase shift in the voltage gain, because of the two zeros introduced by such capacitance. However if the quality factor is higher, the phase should be able to reach almost 180° of phase shift before increasing again towards 0°. However, an improved layout should necessarily designed by increasing the distance between the primary and secondary electrode, in order to avoid the aforementioned capacitive coupling between primary and secondary side.

In addition, the presented devices suffer from air-damping which significantly limits the maximum displacement of the membrane, and hence limits the energy conversion capability of the device. Unfortunately the effect of the air-damping is not easily modelled and hence it cannot be predicted even with an extensive FEM simulation. A vacuum characterization of the devices is necessary in order to assess the actual performance of the fabricated components.

An alternative solution to enhance the step-up ratio of the MEMS piezoelectric device could be also spreading a PZT powder (through inkjet printing techniques) on their surface. This approach might boost the performance of MEMS PTs, given that the AlN has not a piezoelectric effect as strong as the PZT (which is rather electrostrictive than truly piezoelectric). As a matter of fact, PTs with different piezoelectric materials at the primary side and secondary side present higher step-up ratios compared to a single-material PT [98]. The spreading of the PZT powder can be thought has a post-processing step, since the PZT is not IC compliant because of the presence of the lead.

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Acronyms

AC	Alternating Current
AlN	Aluminum Nitride
BCD	Bipolar, CMOS, DMOS
CMOS	Complementary Metal Oxide Semicondutor
DC	Direct Current
ЕН	Energy Harvesting
EMI	ElectroMagnetic Interference
FCM	Fully Clamped Membrane
FEM	Finite Element Methods
FET	Field Effect Transistor
FSM	Free Standing Membrane
IC	Integrated Circuit
LTCC	Low Temperature Co-fired Ceramic
MEMS	Micro- Electro-Mechanical System
MPL	Magnetic Path Length
ММРТ	Minimum Power Point Tracking
МТ	Magnetic Transformer
MtM	More than Moore
РСВ	Printed Circuit Board
РТ	Piezoelectric Transformer
PVC	Photovoltaic Cell
--------	---------------------------------
PwrSiP	Power System in Package
PwrSoC	Power System on Chip
PZT	Lead Zirconate Titanate
RF	Radio Frequency
SEM	Scanning Electron Microscope
SER	Serpentine
SoA	State of Art
SSTC	Square Shaped Toroidal Inductor
TEG	Thermo – Electric Generator
WSN	Wireless Sensor Nodes
ZnO	Zinc Oxide

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